

الثاني الثاني الثاني



معهد التراث العلمي العربي جامعة حلب ـ سورية





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محاة ناريخ الماه والجرية

المحسورون

أحملا يوسقه الحسن جامعة حلب ما الجمهورية المربية السورية سامي خلف الحمارته مؤسسة سميئسونيان بواشتطن ــ الولايات المتحدة الامركية ادوارد س. كنسلى مركز البحرث الامريكي بالقاهرة - مصر

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هيئة التعرير

أحمل يوسف الحسن جاءمة حلب _ الجمهورية المربية السورية سامي خلف الحمارته مؤسسة سميئسونيان بواشنطن _ الولايات المتحدة الاميركية وشم واشمه المركز القومي للبعوث الملمية بباريس - فرنسا احمد سليم سعيدان الجامعة الاردثية _ عمان عبد العميد صبرة جامعة هارفارد _ الولايات المتعدة الاسركية

هيئة المعررين الاستشاريسين

صلاح احصف جابعة دنثاق الجنهورية العربية السوزية البرت زكى اسكندر معهد ويلكوم لتاريخ الطب بلندن ـ انكلترا بيتر بأخمان المهد الالماني ببيروت لبنان دافيد بيتجسري جامعة براون - الولايات المتحدة الامركية رينيــــــه تاتـــــون الاتعاد الدولي لناريخ وفلسفة العلوم ـــ قرنسا فسؤاد سركسن جامعة فرائكفورت المانيا الاتعادية عبد السكريم شعادة جامعة حلب _ الجمهورية العربية السورية معمسه عاصمي اكاديسية العلوم في جمهورية تاجكستان ـ الاتحاد السوفياتي توفيق فهسسة جامعة ستراحورغ فرنسا

خوان فرنيه جنيس جاسة برشلونة ــ اسبانيا جسون مسردوك جامعة هارفارد _ الولايات المتعدة الامركية

واينس فابييك معهد تاريخ الطب، جامعة همبولدت، بولين - ألمانيا د. سيد حسين نصر الاكاديسية الامبرطورية الايرانية للفلسفة .. أيران فيسللي هارتستر جامعة فرانكفورت ألمانيا الاتحادية

تصدر مجلة تاريخ العلوم العربية عن معهد التراث العلمي العسربي مرتين كل عام ﴿ فِي فَصَلَّى الرَّبِيسِعِ وَالْخَرِيفَ ﴾ • يرجي ارسال تسختين من كل بحث أو مقسال الى :

معهد التراث العلمي العربي ... جامعة حلب .

توجه كافة المراسلات الخاسة بالاشتراكات والاعلانات والأمسور الادارية الى العنوان نفسه . يرسل المبلغ المطلوب من خارج سورية بالسدولارات الاميركية بسوجب شيكات باسم الجمعية السورية لتاريخ العلوم

اليمة الاشتراك السنوي:

المجلد الاول أو الثاني (۱۹۷۷ ، ۱۹۷۸) لبرة حورية أو ١ عولارات أمبركية 10 بالبريد العادي المسجل: ST

بالبريد الجوي المسجل:

لبرة موزية أفر ١٠ دولارات أسركية المجلد الثالث (١٩٧٩) ١٠ دولازات أسركية بالبريد العادى المسجل: كافة البلدان

18 cellel low بالبريد الجوي المسجل: البلاد العربية والاوروبية آميا وأفريتيا

10 دولارا أسركيا الولايات المتحدة ، كندا واستراليا ١٧ دولارا أسركمة

معت الهٔ في انتظرت الطيب إلى سعت وة لعمت لي بن ونست وان

تحقيق

سئِلان قطت اينه °

نقدم ولأول مرة النص الكامل لمخطوطة « مقالة في التطرق بالطب الى السعادة» لعلي بن رضوان . وهو النص الوحيد المحفوظ حتى اليوم في مكتبة حكيم علي أوغلو باشا ثحت الرقم 791 (٣) - ف ٨٩٤ .

ولقد تفضل معهد المخطوطات العربية بالقاهرة مشكورا ، فأمدّنا بصورة عنها. والمقالة هذه على قصرها تتمتع ببعض الاهمية .

فهي : اولاً تساعدنا على تحديد زمن ولادة علي بن رضوان ، وبالتالي عمره ، فالمعلوم أن تحديد سنة ولادة العلماء القدامي عسير عادة .

وقد ورد في كتاب ؛ عيون الانباء ؛ لابن أبي اصيبعة (١) عن ابن رضوان نُبلًـ من سيرته الذاتية يقول فيها ؛ . . . وكان يفضل عني الى وقبّي هذا ، وهو آخر السنة التاسعة والحمسين . » ويقصد التاسعة والحمسين من عمره .

كما ذكر ماكس مايرهوف (٣) خلال سرده القائمة الكاملة لمؤلفات ابن رضوان. أن ثمة ثلاثة مؤلفات ربما كانت كلها واحدة أو متشابهة وهي :

و كلية الطب -جامعة حلب

ابن أبي أصيعة - عبون الإنباء في طبقات الأطباء - طبعة ميروت - ١٩٦٥ - ص : ١٩٦٠ - ص : 2. - M. Meyeshof, The Medico-Philosophical Controversy between Ibn Butlan of Baghdad and Ibn Ridwan of Catra, Egyptian University - Faculty of Arts Publication No. 13, (Catro 1937) pp. 41-49.

مامان تطاية

- سيرته المذكورة في كتاب عيون الانباء .
- ومقالة في التطرق بالطب الى السعادة .
- ومقالة في سبيل المعادة ، وهي السيرة التي اختارها لنفسه .

فاذا عدنا الى مقالة في التطرق ، رأينا ابن رضوان يقول » . . . وجدنا تاريـــخ الاسكندر الى وقتنا هذا هو سنة ست وثلاثين واربع ماية للهجرة . . » .

فاذًا اعتبرنا هذا التاريخ (اي عام ٣٦٦ ه / ١٠٤٤ م) هو العام الذي بلغ فيه ابن رضوان سن الستين ، استطعنا القول أنه ولد عام ٣٧٦ ه / ٩٨٦ م ، وتوفي عام ٤٥٣ ه / ١٠٦١ م (حسب ابن ابي اصبيعة) أو ٤٦٠ ه / ١٠٦٧ م (حسب القفطي) ، وأنه عاش بين الخمس وسبعين عاما والواحد والثمانين .

ونجد في المقالة نفسها معلومات تلقي بعض الضوء على مفهوم ابن رضوان عن التعليم الطبي الذي اهم به كثيراً وذكره في معظم مؤلفاته . بل كرّس له كتاباً بعنوان « النافع في كيفية تعليم صناعة الطب » ٣٠ .

ولا بد أن منشأ هذا الاهتمام هو تمارسته للتعليم والتدريس في بيمارستانات مصر . والمعلوم أن ابن رضوان اشتهر يقوله بأنه يمكن تعلم الطب بدون استاذ (كما فعل هو نفسه اذ لم يُعرف له شيخا تتلمذ على يديه) ، وانه انتقد كثيراً بسبب ذلك (٤) .

ففي كتاب ه النافع » يدعي بأن التعلّم عن الكتب لوحدها ممكن اتما ضمن شروط خاصة فيقول « وهذه الطريق يقوم لمن لا يجد معلما جيدا مقام المعلم الجيد » كذلك فهو ليس بمقدور الا « ذوي القرائح الجيدة والطبائع الفائقة » .

وفي مقالة « التطرق » يعود فيؤكد هذه الفكرة فيقول « وليس يخلو المتعلم لها (أي صناعة الطب) من أمرين :

٣ - توجد تسختان: واحدة في دار الكتب المصرية بالقاهرة رقم: طب ٤٨٣. والثانية في مكتبة تشستر
 يين في ديلن (رقم: ٢٠٣١) .

٤ - اين الي أصيبة - البود - بيروت - ١٩٦٥ ص ص: ٩٩٣ مـ ١٩٦٥ .

١ – اما أن يجد معلما فاضلا يفهم منه ما في كتب ابقراط فيسرع بذلك تعلمه
 كما أسرع تعليم جالينوس .

 ٢ – واما أن يُعدم المعلم الحاذق فيحتاج أن يتعلم لنفسه من كتب جالينوس فيطول زمان تعليمه ,

ثم يشير الى أن القسم العملي من الطب لا يتم تعليمه الا : ، بمعاينة هذه الاعمال بين يدي أفضل من تعلم عليه من اهلها » .

وهنا تبدو لنا أهمية مقالة ، التطرق ، لآنها تقدم تفاصيل جديدة غير معروفة عنه ، وتجعل فكرته عن التعليم الطبي مقبولة الى حد ما . رغم اعتقادنا الجازم بأنه لا بد من معلم لكل من قسمى الطب : النظري والعملي .

ثم يكرس ابن رضوان الباب الثالث من المقالة لموضوع عنوان المقالة ، فيشرح مفهومه الفلسفي عن مهنة الطب .

وهو مفهوم مثالي مطلق فيقول ۽ قال جالينوس في آخر المقالة الاولى من حيلة البرء : وينهغي لنا أن نتافس وٽباهي الملائكة في فعل الخير ۽ .

والفكرة هذه مشروحة بشكل مفصل في كتابه ، في شرف الطب ، وهو مفهوم ديني مرتكز على أن الطب هو فعل الخير وواسطة لارضاء الله والفوز بالجنان ، ويعترف انه رغم ذلك فان الطب في ايامه (كما في كل زمان وعصر) لم يكن يخلو من الدجل والشعوذة .

ويبدو لنا أنه من الضروري النمييز بين من يختار مهنة الطب عن ايمان ديني عميق لا يريد منه سوى كسب مرضاة الله وهم الندرة . والغالبية التي لا ترى في الطب الا وسيلة لكسب المال والحياة الرغيدة . وهذا ما لم يره ابن رضوان ، أو رآه ولم يعترف يه .

وينتقـــل ابن رضوان في مقالة «التطرق» الى تاريخ الطب قيل الاسلام . ونراه

لا يقدر أو يحترم الا ابقراط وجاليتوس(*) . وخاصة هذا الاخير . اذ يعتبر كتبه فوق كل نقد ، أو شك ، بل ينتقد بقسوة كل من يتعرّض لنقده (كالرازي مثلا) .

و تلك نقطة ضعف في مؤلفاته ، لأن الفكر العلمي يبحث دوما عن الحقيقة . وهو في سبيل ذلك لا يتوانى عن منافشة كل رأي بفكر علمي موضوعي .

ه - شرح ابن رضوان مئة كتب لجاليتوس هي . كتاب الصناعة الصنبيرة حـ كتاب الا مطلسات - كتاب النبض الصنبير - بعض كتاب المزاج - كتاب جاليتوس الى الحلوقن - في التأني الشفاء الامراض - (ابن ابني الصبيعة - العيولة - س : ٩٦٦) .

لِيسْمِ الْمُعْرِالِ عَيْمِ الْمُعْرِالِ عَيْمِ الْمُعْرِالِ عَيْمِ الْمُعْرِيمِ

مقالة على س رضوان في التطرق بالطب الى السعادة وهي ثلاثة ابواب .

ا**لباب الاول** ... في كتب ابقراط.

الباب الثاني ــ في تعريف ابقراط ,

الباب الثالث - في التطرق بالطب إلى السعادة .

الياب الاول في كتب ابقراط

قال علي بن رصوان : قد بينا في كتبا (١) ان انقراط استكمل تعليم صناعة الطب وان جالينوس هدب تعليم انقراط ، قصير صناعة الطب وان جالينوس هدب تعليم انقراط ، قصير صناعة الطب ميدرة سهلة التناول على من زاولها من دوي الطبائع العايمة ، واما عير هاؤلاي فقد نهي انقراط وحاليوس معاً عن تعليم هاؤلاي متى انتحلوها فهم فيها اطباء بالاسم لا اطباء بالفعل ، لتقصير طائعهم عن ادراكها ، ولذلك هم السب في ذمتها ، واوضحنا انه ينبعي ان يكون المتعلم لحا طبيعة مواتية ، ودهن ذكي ، وحفظ جيد ، وحرص شديد ، واحتمال للتعب ، وحب للجميل ،

وان يكون قبل تعلمها قسد تأدّت بالآداب والتعالمسيم فقد ذكر حالينوس(٧) في مقالته في ترتيب قراءة كتبه · انه شرع في تعليم الطب بعد رياضة في التعاليم والآداب ، وقد بلغ في السن المسنة السابعة عشر .

 ٦ – ريما كان يقصد كتاب. ١ النامع في كبعة تعلم صناعه الطب " بشكل حاص و عو محطوط عبر مطبوع ,

۷ Galien ولد حوالي عام ۱۴۰ م بي برعامس في ميسيا وتوبي حوالي سنة ۲۰۰ م ويدعي العص
 انه توبي عام ۲۱۸ م , وهو من اكبر اساء اليونان , وكتبه السنة عشر اشهر من ان تدكر.

وقال في غير هذه المقالة انه وضع كتابا في الاسطقسات ، وهو ابن تسعة عشر سنة . وما كان يصبع دلك الا بعد استكماله تعليم صناعة الطب ، ودلك انه عرف في تفسيره كتاب طبيعة الانسان ليقراط ، وصعه بعد ان وقف على آراء ايقراط ، وفهم ما في كتبه يقراءته اياها على حدّاق المعلمين ، فحصل رمان تعلمه الطب ثلاث سنين فلللك ينبغي (أن) يقتدى به في تعليم هذه الصناعة ، فيتأدب اولا في الاداب، ويرتاض في التعاليم ، ثم يقرأ كتب ايقراط ، ويعهم معانيها . لم يكن احدا قبله هذمها شهديه .

فالحاصل من ذلك انه يمكن تعليم صناعة الطب في ثلاث سنين . وقد اشترط ابقراط في تعييمها شروطاً منها ما دكرته اولا من حال طبعه للتعليم ، ومنها ان يكون حديث الس ، وهو من كان عمره ما بين سن اللوغ وبين خمس وعشرين سنة ، لأن المراج على هذا السن اعدل منه في سائر الاسال ، وقوى النفس تابعه مزاح البدن .

وليس يخلو المتعلم لها من احد امرين :

ان ال يجد معلما فاضلا يفهم منه ما في كتب ابقراط فيسرع بالملك تعليمه
 كما اسرع تعليم جالينوس .

ــ واما أن يعدم المعلم الحادق فيحتاج أن يتعلم لنفسه من كتب جالينوس فيطول زمان تعليمه متى استعمل في تعليمه قوانين المطق .

ولأن صاعة الطب صناعة فاعلة لم يمكن تعليمها خُلُواً من منازلة اعمالها الجزئية. كما بين دلك ارسطوطاليس فيما بعد الطبيعة . ان كل صناعة فاعلة انما تحصل وتكمل بمعرفة قوانينها الكلية ، وبمنازلة اعمالها الجزئية .

قادن . المتعلم لصناعة الطب ، مع قراءته كتب ابقراط ، ينزمه صرورة ال ينازل بنصه اعمالها الجزئية وذلك يتم ممعاينة هذه الاعمال الحزئية بين يدى افضل من تعلم عليه من اهلها . وقد وضع جالينوس لكتبه التي هذب فيها تعليم بقراط ولخصه مهرست(٨) ولقرائتها ترتيب . فالمتعلم يأخد دلك مسن جالينوس . واما كتب بقراط

٨ – كتب على الحاش - فكتبت ال رفيقي مجين بن معند في ذلك فبدائي منه فهرستها

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فلم يقع لي فيما سلف لها فهرست. ذكر أنه ترجمه من البوناقي إلى العربي. فقرأته فوجدت الكتب غير مرتبَّة ، ولم يتفق حصول جمعها عندي فأرتب قراءتها. ودلك انه يعوزني منها نحو اثنا عشر مقالة فرأيت ان أنسخ لي في هذا الموضع ما وصل الي من فهرستها على ١ ظ هيئته , وهذا هو ;

> كتاب الناموس مقاله (٢) كتاب الوصية مقالة كتاب العهد مقالة ه كتاب الفصول سبع مقالات

كتاب تقدمة المرفة ثلاث مقالات

كتاب قاطيطريون ثلاث مقالات

كتاب تقدمة الانذار مقالتان

كتاب تقدمة الانذار المنسوب الى أهل قسو

كتاب الامراض ثلاث مقالات

كتاب تدبير الامراض الحادة و هو كتاب ماء الشعير ثلاث مقالات

كتاب الغذاء اربع مقالات

كتاب التدبير ثلاث مقالات

كتاب استعمال الرطوبات

كتاب الادوية

كتاب الحقن

ه كتاب ابيذيميا سبع مقالات كتاب الاعظم في العلل

كتاب العلل الباطنة

 ٩ - لقد بسب الى ابفراط كتب كثيرة ويقول ابن اي اصبيعة (العيون - ص ١٠٠) * والدي المهى الينا ذكره ووجدنا في كتب ايقراط الصحيحه يكون نحو ثلاثين كنابا واندي يعرس من كنده لمن يقرأ صناعة الطب م اذا كان درسه على اصل صحيح وتر ثيب جيد ، اثنا عشر كناما وهي المشهورة من كتبه " والقدوضيت اشارة ۽ الَّي جانب کل کتاب سي هذه الکتب الاثني عشر ، اورد ذکره ۾ قائمة علي س رضوات

كتاب المرض الكاهبي كتاب الاسابيع مقالة كتاب النفخ مفالة « كتاب الأهوية والبلدان والمياه اربع مقالات كتاب الطب القديم كتاب الصناعسة كتاب البصير كتاب الإخلاط ثلاث مقالات كتاب الورم كتاب الجر أحات القاتلة كتاب خراجات الرأس كتاب النتراع البثور(١٠) كتاب البواسير كتاب النواصير كتاب الكسر والرص كتاب المعاصل كتاب نهايات الامراض كتاب طبيعة الجنين ثلاث مقالات و كتاب طبيعة الإنسان ثلاث مقالات

الم كتاب طبيعة الجنين ثلاث مقالات الله عقالات كتاب طبيعة الانسان ثلاث مقالات كتاب المواضع التي في الانسان كتاب المولودين لسعة اشهر كتاب المولودين لشانية اشهر كتاب المولودين لتسعة اشهر كتاب حبّل على حبّل

١٠ - ي الاصل البثول
 ١١ - ي الاصل: للسر . وي قائمة أبن إني اصبيعة وود أسعه ^{حا}كتاب الكسر والجمر . ويقول هذا (العيون - ص ه ه) " والايتراث ايضا من الكتب ويضها مشعول اليه . . "

كتاب تقطيع الجنيز الميت
كتاب في الامراض
كتاب أبات الاسنان
كتاب العدارى
كتاب تدبير النساء
كتاب مل يبول الدم
كتاب علل النسا
كتاب النساء اللواتي لا يحبلن
كتاب الساء اللواتي لا يحبلن
كتاب الباء

قال علي : وليس هي مرتبة ويمكن ان ترتب ترتيبين : احديهما يليق باصحاب التجارب(١٣) وهي ان ببدأ بقراءة قاطيطرون ، وتمسيره حانوت الطيب ، ثم نثي بعده كتاب الكسر والرض ، ثم كتاب الحبر ، ثم كتاب الحراجات ، ثم ساثر الكتب العلمية على ترتيب ما ينبغي ان يقرأه شيئا بعد شيء .

هادا فرعت الكتب العملية ، يبدأ بعدها بكتاب طبيعة الانسال و ترتيب القراءة فيها على ما ينبغي .

والثرتيب الاخر يليق نرأى اصحاب القياس : وهو ان يبدأ نفراءة كتاب طبيعة الانسان ثم يوالي الفراءة على ما دكرت ويحفظ طاهر كتاب الفصول ، وكتاب تقدمة المعرفة فاذا فرغت كتب علم هذه الصاعة يدى، نقراءة كتاب قاطيطرون وما يعده على حسب ما يوجبه العمل .

Empiriques - ۱۲ . والمعلوم أنه كان ثمة ثلاث معارس طبية بوسانيه اصحاب الفياس Magmatists - الذين يعتمدون على الملاحظة والمعلق

وأصحاب الحيل Méthodistes الدين يعتمدون على مقارعه المرصى باية طريقة كان الشعائه والعمهم طالبيس Thesalus إلى وأصحاب التحاريب الذين كاموا العتبدوال على نتائج السجرية العلمية العلاجية

۲۵.

الباب الثاني

في تعريب ف ابستقراط (١٣)

ويقال ان معنى هذا الاسم : ماسك الفرس ,

قالوا · انه اتفق لرجل كان شديد القوة انه ضرف بيد الواحدة الى رأس او عنق فرس هايح ، وضرب بيد الاخرى الى اصلى دفه ، فمسكه قائمًا لا يقدر يتحرك . فتعجب الناس من شدته وسموه بقراطيس اي ماسك الفرس واشتهر هذا الاسم في اليونانيين ، عضرب به المثل لكل من كان من الناس شديد القوة ، الى ان صار اليونانيين يسمود ابنائهم كما نحن تسمى ابنائها اسد وصاعد نحو دلك الى يومنا هذا .

والمشهور هذا الاسم من علمها البونانيين خمسة رجال . احدهم ذكره السطوطاليس (١٤) في المقالة الاولى من السماع الطبيعي، وفي غيرها اعاد دكره على اله وجل مهندس ظل اله وحد مربع الدائرة . فإن هذه المسألة مختلف فيها الى يومنا هذا بين المهندسين. والاربعة الباقون اطباء ذكرهم جالينوس في تفاسير كتب ابقراط فقال في مقالته في المولود لسبعة اشهر : لقد اختلف المفسرون لكتب الفاضل ابقراط . منهم من قال اللهوات وضعها انقراط واحد ، ومنهم من قال : انها ليست لواحد . وذلك ان القوم الذين كانوا يسمتون بهذا الاسم ، اعني ابقراط ، اربعة نفر يتلو بعضهم عضا واولهم : بقراط ابن اغوسيديقس والثاني : نقراط بن ايراقليدس ، والثالث : نقراط بن بساكوس (١٠) ، والرابع : نقراط ابو دراقن ولجميعهم كتب .

وقال في تفسيره المقالة الثانية من كتاب طبيعة الانسان . نقراط الكبير له ولدان احدهما تاسالس(١٦٠) ، والاخر دراقن . ولكل منهما ولد سماه بقراط .

قال على : وعرف جالينوس دلك في مواضع أخر من كتبه . وقال : ان ثاستالس بن بقراط كان من المتقدمين في صناعة الطب . لكنه لم يحلف اباه بقراط في التعليم بمدينته .

١٣ - ويسمى ايضا بقراط ويلقب بالكبير والحكيم والعاضل والالحي وابي الطب توبي حوالي عام ٣٥٧ ق. م
 ١٤ - ويكتب ايضا أوسطو فيلسوف يوناني شهير (٣٨٤ - ٣٢٧ ق. م) .

١٥ - فعلها - تامالوس - تامتالوس

كن صحيب ارسالاوس الملك والدي خلف بقراط في التعليم تلميذه فولوبس ، ودلك ان يقراط ن ايراقلبلس كان له جماعة من التلاميذ وولداه تسايس(١٧) ودراقن ، ولم يخلفه في التعليم سوى تلميذ فولوبس ، وذكر ان المقالة الثالثة من كتاب طبيعة الانسان (١١) التي هي حفظ الصحة لفولوبس(١٨) ، وان المقالة الثانية من كتاب ابيذيميا لتاسالس(١١) وان قوما نسوا كتاب المولودين لثمانية اشهر الى فولوبس . وبالحملة فليس ما وضعه هاؤلاي الرجال السبعة الاربعة المسمون بقراط ، والثلاثة ثاسالس(٢٠) ودراقن الى بقراط بن اراقليدس لان هو الذي خرج له الاسم وكان اعصل القوم ، وافضل جميع بقراط بن اراقليدس لان هو الذي خرج له الاسم وكان اعصل القوم ، وافضل جميع من كان في عصره ، ومن تقدمه ومن تأخر الى يومنا هدا من الإطباء .

الابدين ، ما دام الناس موجودين . ولقد بلغ من امره في حياته ، وبعد وهاته الى ابد الابدين ، ما دام الناس موجودين . ولقد بلغ من امره في حياته ان ملك الفرس المسما بملك الملوك ارطحششت (٣١) بدل (٣٢) له مائة قنطار ذهب ، والحبات العظيمة (٣٧) بملك الملوك ارطحشش والمياب اليه ويتحدمه بالمطب عما عمل ولا اجابه . وبذل له اهل ابديرا (٢٤) عشر قناطير ذهب على علاج حكيمهم دمقراط (٣٥) لما طنوا انه يغير عقله ، فرد المال ومن عليهم وسار اليه معهم ، فلما شاهد دمقراط علم انه صحيح ، وابه لما اشتغل بالعلم عن تدبير مدينتهم طنوا انه قد تغير عقله ، فاعلمهم بقراط انه صحيح وابه آثر الانفراد والحلوة بالسطر والفلسفة والسكون عن تدبير المدينة . وابصرف عبهم الى مدينته قو . ولا قراط اختار كثيرة ، وعجاب جدا ، تدل على فصيلة عظيمة ، وشرف عطيم . وانا اثبت وضع بقراط في المعمورة ، ووصع مدن الحكما المشهورين بالحكمة الصحيحة ، وانا اثبت وضع بقراط في المعمورة ، ووصع مدن الحكما المشهورين بالحكمة الصحيحة ، فان بطلميوس ٢٠٧) صححح وضع هذه المدائن في كنابه في صورة المعمورة من الارض فمنها قو مدينة ابقراط : فطولها مد درجة ، وعرضها كسر درجة . واما فرغاس مدينة فمنها قو مدينة ابقراط : فطولها مد درجة ، وعرضها كسر درجة . واما فرغاس مدينة فمنها قو مدينة ابقراط : فعلولها مد درجة ، وعرضها كسر درجة . واما فرغاس مدينة فمنها قو مدينة ابقراط : فعلولها مد درجة ، وعرضها كسر درجة . واما فرغاس مدينة

١٧ - في الاصل - تاستالس
 ١٩ - في الاصل - تاسالس
 ١٩ - في الاصل - تاسالس

٢١ - في الاصل - اد طحمت والاغلب الله اردشير و الانصل اردشير وحده في اللهود ان القراطكان في عهد " بهن بن اردشير " ٢٢ - في الاصل - اليقل عهد " بهن بن اردشير " ٢٢ - في الاصل - اليقل .

٣٤ -- جريرة يونانية صعيرة الشهر اهلها عُقْفَة النقل .

۲۵ اوديمقر اطيس وهو فيلسوف تلميذ ارسطو وعاش في حدود عام ۲۵۹ ق . م .
 ۲۲ - ويسمى ايضا بطلساوس وبطليموس وابطليموس وسلميوس (۲۸۵ - ۲۵۲ ق . م)

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حاليوس عطولها دله وعرصها مآر واما اثينا مدينة الحكماء ، وهي مدينة سقراط (٢٧) وافلاطو (٢٧) : فطولها يب م وعرضها لذك . فجميع هاؤلاي في الاقليم الرابع وفي السهف العربي من المعمور قريب من منتهاه الى جهة المشرق المحاور لاشياء وذلك ان الحكمة نقلها من مصر بالس الملطي (٢٧) . وفيثاغورس (٢٠) الى اليونانيين ، لاهما سافرا الى مصر وتعلما من حكما أم وسارا الى اليونانيين فاطهرا ما تعلماه من اهل مصر ، لان مصر كانت في القديم دار الحكمة والعلم ، وهذه الحكاية يشهد بصحتها كتاب التوراة ، وقد كتبها فلاطن وارسطوطاليس في كتبهما ، ودونها فرفوريوس وغيره ممن عبي بكتب تواريح الحكماء من الفلاسفة والاطباء ، وذكر جاليوس في كتبه ان الطب اقتصر عليه اسقليوس (٢٧) ، واسقليوس مختلف فيه فطائفة رعمت انه ملك بعثه الله عز وجل فعلم ، هل هذا المحث صناعة الطب قسمي على عادة القدماء في تسمية المعلم اباً للمتعلم ، واليه وطائفة زعمت انه رجل اوجي اليه الطب واستخرج هو ايضا من تلقاء نفسه ، واليه تكسب الاطباء في سالم الدهر ، ودلك ان الطب كان اولا بجزيرة قنيدس (٢٧) ، ثم انتقل الى جزيرة قورة ٢٠) ،

اما حزيرة رودس فطولها عر وعرضها لسو ، واما جزيرة قبيدس فطولها لويه وعرضها لو ، واما حزيرة قو فطولها ع مر وعرضها فيما سلف

وكان الطب في هذا البيت يتعلمه الولد من اليه وجده فقط ، ولا يمكن عريب تعليمه الى ان دشأ القراط بن البر قليدس المشهور بالفضيلة ، فحات على الطب ال يبيد ويصد ، فشرط شروطا انت نقف عليها من كتاب الناموس والوصية والعهد على المعلم

٧٧ ــ انقراطيس فيلموف يوناني حكم عليه الموت بالسم .

٣٨ - ي الاصل - فلاطون. وهو القياسوف اليوناني المثالي (٢٤٧ - ٣١٧ ق. م) .

٩٩ – بولس الامتيطي أو القرابل – أحد أطباء مدرسة الاسكندرية

۳۰ Pythagore حكيم يوناني , زار مصر وبابل برائنام , ويعرى ليه تقوم الحسب المعروف مجلول مشفورس في المعرب ثوفي في حريرة سعوس (حوالي عام ۲۰۰ ق . م)

٣١ - يسم ايضا المقيليوس والمقليبياريس

Cos - 71 Cnides - 77 Rodes - 77

والمتعلم . فمن الزم نفسه تلك الشروط وكانت فيه ، اباحة التعليم ، كان من بسله او من غير نسله . وكان تلميذه فولوبس افضل تلاميذه ولم يرل الطب ينتقل من واحد الى واحد الى ان انتهائه الى جالينوس ، وليس هو من نسل اسقليبوس ، فزيف جالينوس (٣٥) الاقاويل الفاسدة وبهرج الاراء الكادبة الردية وهذب صاعة الطب فيما وضعه من التفاسير لكتب ابقراط ، ومن كتبه وعرف في تفاسير وكتب ابقراط الاقاويل المدلسه عليه التي دلستها الماس السوء على أنها يسيرة جدا بالقياس الى ما في هذه الاراء الصحيحة التي اخصي فيها ذلك التدليس، فاداكان كدلك لا فائدة محددة في كتب غير بقراط وجالينوس سوى الكتب التي نص عليها مثل كتاب ديسقوريدس (٣٦) في الادوية المفردة ، ومسا سوى لا ينتفع به وضار لا محالة بالمتعلمين . اذ كان لا يمكن علاح مرض حتى يعرف اوقاته الكلية والجزئية فيعطي في كل واحد منها ما يبغي ، وهذا لا يمكن الا ان يفهم كتاب الفصول ، وكتاب تقدمة المورفة ، وكتاب البحران ، وحيلة البرء .

واذ قد دكرنا مدائن الحكماء ، وانا نريد في تعريف بقراط بمعرفة تاريحه وتاريح كل واحد من الحكماء المشهورين بالفصيلة فاقول : ان حالينوس يقول في غير موضع من كتبه انه كان على عهد ادريانوس الملك وانه تحصص بخدمة انطونيس وهو الذي علك بعد وفاة ادريانوس. وقد بلغني في داك حكاية حكاها في كتابه المعروف بالادوية (المقابلة) (۱۲۳ للأدواء نحو ثلني المقالة الاولى بأن جاليوس اتى لما انخذت الريق لانطوبيس الملك رأيت اواني عده مملوه دار صيني (۱۲۸ بعضها حزن على عهد طراباويوس وبعضها على عهد ادريابوس ، ورأيت جميع اصناف الدار صيني التي جذبتها واحد يفصل كل منها على صاحبه في القرة والضعف والطعم والرائحة بحسب تقادمه في الزمان الاول من

٣٥ ما يستفرب مثل هذه الصقات ان يتسبها على بن رضواد الى جاليموس . لان على مثل الراري والكثيرين من الاطباء المرب يتعدثون عن بقراط ولكبم لا يقرأون ويستشهدون الا بكتب جاليموس . ونقد فسر وشرح ابن رصوان مئة كتب خاليموس وخلال كل ما قرأناه من كتب انن رضوان محده تلميدا متحمما جداً له .

٣٦ ~ ريسمى أيضا دياسةوربدوس ريلتب يصاحب النفس الزكة والسائح و لحكيم الحشائشي والعبي رد في هاش في القرن الاول والثاقي بعد الميلاد . وله كتاب الحشائش الشهير .

۳۷ – عير معهومة Cinnamamum Zeylanieum – ۳۸ بره و ببات يشه القرفة (انظر احياه التذكرة رمري معتاح) – القاهرة ۱۹۵۳ – ص . ۳۹۳ – وكتاب المعردات لا بن البيطار (- بولا ق – ص ۸۷).

مثناث ثناية علية

اصناف الدار صيني فاتخذت منه معجونا لمرقس الملك المسمى انطونيس فوجدت ذلك المعجود اهضل من سائر المعجودات ، حتى ال الملك لما داقه لم يدعه مدة من الزمان ، كما يفعل سائر المعاجين الى ال يستحكم (٣٦) . لكنه استعمله على المكال (١٠) من غير ال تزله شهرين . هلما ورث الملك بعد فورمودس الذي لم يعن لا بالترياق ولا بالدار صيني ، صاع ما كان معي من قلك الشجرة ، وكلما جلب من الدار صيبي بعد اندرانوس حتى ان ملك سورس امر ال يتخد له الترياق على ما كان يتخذ لانطونيس، فاضطررت ان اختار لعمله من الدار صيني . فينت من ذلك الترياق بيانا واضحا انه اضعف على انه ، لم يكن مضى على الدار صيني ثلثون سنة كاملة .

قال على . وبطلميوس في كتاب المجلطي (٤١) انه رصد ثلاث كسوقات قمرية باسكندرية في عقر ادريانوس الملك ويقول في المقالة الثالثة : ورصدنا نحن ٣ و الاستواء الحريمي بعاية الاحتياط والتحرز من الخطأ في السنة الثائثة لانطوبيس وهي سنة اربع ماية وثلثة وستين من وفاة الاسكندر .

٤٠ أي – فور .
 ٢٥ أي ألاصل – ثلامية .

۲۹ - اي حق يشج Almagest - 11 واحدى وعشرون سنة الى ان توفي الاسكندر سنة ست عشر سنة ، فيحمع دلك ماية وسبعه وثلثول سنة ، فيحمع دلك ماية وسبعه وثلثول سنة ، وادا السكندر كال ما بين يقراط وجالينوس من السين خمس ماية وسبعة وثلثول سنة . وادا قابلنا ما استخرجنا من هذا الحساب ما دكره يحبي اللحوي في تاريخه وتفسيره كال للادوية المقابلة للادواء ، وجدفا يحبي النحوي المقول . مسى رمن وفاة بقراط الى ظهور جاليوس ستماية وخمس وستون سنة وان بقراط عاش خمسة وسبعين سنة ، وجالينوس عاش سبعة وثمائون سنة منها صبيا ومتعلما سبع عشر سنة ، وعالما ومعلما سبعون سنة .

قال على : فالحلف اذى بين التاريخين سبعة وسبعون سنة فان كان القراط توفي عصر ارطخست اربعة وعشرون سنة ولدلك ان كان ما ذكره يحيى هو الذي علمناه جالينوس صح قوله وال لم يكن كذلك فقد عرض له سهو في التاريح اصح واوفق ، لانا اخذناه من قبل نظلميوس وبجلول تاريخ الملوك وليسى في ذلك شبهة ولا شك وهو ان بين جاليوس ، وبين بقراط ستماية سة فقط ، واذا حسنا ما بينا وبين كل واحد منهما وجدنا تاريخ الاسكندر الى وقتنا هذا ، وهو سنة ست وثلثين واربع للهجرة ، الف وثلثماية واثنين وستين سنة تامة زدنا عليها ماية وسبعة وعشرين سنة بين وفاة ارطخست الله وثنين وستين سنة تامة زدنا عليها ماية والعملية والرسماية وتسعة وثمانون سنة ، واذا نقتصنا من تاريخ الاسكندر الارسماية والثلاث والسين سنة ، كان بيننا وبين حالينوس واذا نقتصنا من تاريخ الاسكندر الارسماية والثلاث والسين سنة ، كان بيننا وبين حالينوس تسم ماية سنة بعشرات سنين واحاد لان جاليوس يقول في كتابه في فهرست كتبه ان انطليوس اشخصه معه من بلده اليه وقد جاوز سبعة وثلثون سنة بمقدار قليل قد يمكن تصحيحه فقد تبيل عا ذكرت ال منه هاؤلاي الحكماء .

فلنعرد الآن الى غرضا في هده المقالة وهو أن نبين كيفية التطرق بالطب الى السعادة .

Jean le Grammairien - 27 - احد علماء مدرسه الاسكندرية ، عاصر الفتح العربي ، وهو احد الذين شاركوا في التقاء ورضع الكتب السنة عشر لجالينوس .

طان قايه

الباب الثالث في التطرق بالطب الى السعادة

قال على : قد بيد فيما سلب ان صناعة الطب يمكن ان تتعلم في ثلاث سنين . وانه لا حدحة بالتعليب الى عير كتب بقراط وجالينوس وكتاب دياسقوريدس ولذلك اقول ان التشاغر بغير هذه الكتب كما قال بعض الناس دار حمى للاشقياء المحرومين المكدودين الذين لهم الى الحير المحتمل سبيل فيعلوه وقد تبن ان الطبيب يمكنه ان يفعل الحير ويصطم المعروف الى الدس في حفظ صحة الدالهم وشفاء امر صهم حتى يقوموا الى اشغالهم .

وقد قال جاليبوس في آخر المقالة الاولى من حيلة المره: ويبغي لما ان ننافس وندهي الملائكة في فعل الحير فانه لا شيء اقبح ولا اشبع من ان يقدر على فعل الحير فيتوانا عنه ويطرحه وحكا عن اوديسوس في مقالتة في تعرف لانسان عيوب نفسه بي لك من مر ما اقبحه وازدراه ان ثعرت الحير ولا تعمل به ، وقال ارسطوطليس ليس التواي عن العبابة بالحير شر و كان الاسكندر يقول المما احدثه عن معلمي ارسطوطاليس أي لا اعد ملكي يوما لم افعل فيه خيراً ولم احسن فيه الى انسان ، وظاهر ان الطبيب الماهر ادا قصد الاحسان الى الناس فلا بد ان يحصل له منهم ما يكفيه في الضرورة وزيادة عليه .

قال لقراط: اله ليس في الدنيا شيء يعي باحرة الطيب اذا كانت الصحة لا عبش الا بها ، ولا يتم شيء من الاعمال الا بها . والحلاص من المرص اتما هو الخلاص من الموت ، فلدلك لا يغي شيء وال كثر ناجرة الطيب ، لكن اجره على الله عز وحل ، وما حصل له فيسفي ان يكون على وجه الهدية والصلة ، فاما غير ذلك وادا كان يمكنك فمن الدين ان الطيب يتوصل الى الكماية في الضرورى ، والى الاحسال الى الناس وفعل الحير ولما اجتمع نقراط مع دمقراط في ابديرا المدينة ضحك دمقراط ضحكا افرط فيه فسأله نقراط عن السب المضحك له فقال دمقراط بهذا اللفظ ، اخرجني يا بقراط الى الصحك طول لتعجب مما ارى عليه امور الناس واحوالهم التي انا اشرحها لك لاتهم

يفتون اعمارهم فيما لا يعود عليهم بمفعة زمانهم بما يجب ان يهترأ به ويضحت مه فمهم من يجول اقطار الارص ويتعب نفسه ويشقيها وبذلها حرصاً على اقتاء الذهب والفضة فادا حصلا له مات وتركهما ، ولم ينتفع منهما نشيء . وممهم من يشتري الحيل والدواب والضياع والارضين الواسعة ويعمرها ويغرس فيها الاشجار ويجعلها ملكا خاصا له وهو الضياع والارضين الواسعة ويعمرها ويغرس فيها الاشجار ويجعلها ملكا خاصا له وهو لا يقدر يملك نفسه ، ما هذا الحرص الفارع الذي لا فرق بينه وبين الكينون ، اذا افادوا المال راد واشترى الارصين واذا اشتروها ناعوا علاتها وتمارها وجمعوا مالها . فكم في السرة يتقلبون ، اذا لم يكن لهم ثروة تأسفوا واغتدوا، واذا اثروا ستروا مالهم وعطوه ، وتعلوا وقوع الحيلة عليهم فيه . ، قد شقيت نجوتهم ، وتخطوا نواميس الحق لمحبتهم لا يعادي نعضا ، وفيهم من يقاتل احواته واولاد بيته ، وبي مدينته بسب اغراض الدنيا التي اذا مات نزلها ولم يكن مالكا لها . فلم اعزل يا بقراط على صحكي اغراض الدنيا التي اذا مات نزلها ولم يكن مالكا لها . فلم اعزل يا بقراط على صحكي وليس بهم من المرص اكثر مما وصفاه ، فالرؤساء يقولون الحيط والسعادة لعامة ، والعامة تشمهي الرياسة والمدر للمدينة ان الصناع بايديهم اسعد واحمد عاقمة ، والصناع يعبطون المدينة .

قال ابقراط · قلت الحق يا دمقراط واقسم نالله أنك لسعيد لما ربحث من هذا السلوان (٤٤) .

قال على : وقد بين ارسطوطاليس ان السعادة هي الحياة بالعقل وان العمر الطيب (منه) الملذيذ هو العمر مع العقل ، اد ليس احد يختار الحياة وعقله عقل صبي . ومن عقول الصبيان التماس الشهوات البهيمية وبين ايضا فيما بعد الطبيعة ان التمتع بالمشهوات وللوع الامائي منها انما هي ادراكات ملدة . ومن كان حظه من هـذه الادراكات ي والملدة اكثر ، كان مغوطا بما له اكثر ولذلك يكون ان من كان اكثر ادراكا للامور العظيمة ، فهو اوفر سعادة واكثر حطا ولذلك صار الحيوان افضل من النبات ودلك انه اكثر ادراكا من قبل انه حيوان حكيم له يدان يبطش بهما وعقل يفكر فيه ويتروى ويتعلم ، ويستعمل الكلام ، والمخاطبات ، ويجد اصناف الاطعمة اللديدة ، والنبات

وع حق الأصل م الطبيب .

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الرفيعة والنعم الحسنة ، والآلوان المنوعة ٤٦٪ ويلتد بما يشاهد من رؤية السماء بالكواكب ورؤية الارص بالمياه والآنهار ، ومطبوع على حب الرياسة وتتوق نفسه الى معرفة اساب ما يشاهد من الاشياء ومكمل بما ادرك من ذلك . ويتوق غيره محسب ما يفصل عليه في الادراك ويصير افضل منه ، وهو تمن عرف عتايته الى الريادة في الفهم والمعرفة . وان كان افصل ممن لم يتزايد بظن ان حطه من امور الدبيا اقل من حظ غيره من على (. . .) (٤٧) بهـــا ودلك لثلاثة اوجه احدها ان فضائل الا بادخار (٤٨) جياد للابناء والثاني البحث الحادث عـــ عطايا النحوم في المواليد ، والثالث ال يعرض لمــن النصرف الى النظر في اللذة تنا يدركه من كبر النفس ، ما يشعله عن الاكتساب. والخضوع الى من هو دونه في الفهم . وحل هذا الشك سهل لانه لا يفوته وحود الصرورى والحظوط مراد للادراكات اللديدة. ولا شيء من الادراكات اللذيدة ولا اجلّ ولا افضل من ادراكات النظر الفلسمي ، وكلما كان ادراك الانسان افضل واسعد على الحقيقة , وافضل الادراكات واوفقها بقينا وصحة هي الادراكات الفلسفية اعبي النظر في الحكمة واستعمال العدل والسحاء والعمة في نفقات المال , فاذن : السعادة الانسانية على اليقين والصحة هي التفلسف عدما وعملا ولقد رأينا من على دلك الطبيب ادا انصرف بعض يومه في رياصة بدله في اعمال الطب وصرت ما في يومه في العمل الصالح والفكر في ملكوت السماوات والارض ، وعبد الله واطاع العقل ودلك ما اردنا بيانه .

تمت مقالة على بن رصوال في التطرق بالطب الى السعادة . والحمد لله وصلى الله على سيدنا محمد واله اجمعين . نقلت ذلك جميعه من نسخة دقيقة الخط الى عاية ما يكون ما يعرف منه اول الحرف من اخر الا يفتح من الله سلحانه وتعالى ، بعبارات غريبة بعيدة عن القصد واتحير في اختصارها او اصلاحها ، ولطف الله جل وعلا بحسب ما المكن من القلوة . وترجو من كرم الله تصحيحها ان شاء الله تعالى وهو حسبنا وتعم الوكيل . نقل عبيد الله سلمان ابن الاسعد المتطبب عفا الله عنهما . في شهور سنة نور عشر وتمان ماية (على عادس الله عاقبتها .

٢٤ - في الاصل الموقعة ٤٧ - كلمة غير مقرؤة ٨٤ - في الاصل - بدحاير
 ٤٩ - ٧٠٤١ م

١.

ملفصت للهان کالمیسور در ا فی لاهمیشیم لاه مبن

مسألة هندمية وحسابية تشرف الدين الطومي

رشدي راشد

لقد بينًا في دراسات سابقة أهمية أعمال شرف الدين الطوسي الرياضية . وهذه الأعمال هي :

 ١ - كتابه ، في المعادلات ، الذي يمثل حطوة أساسية في تاريخ الجبر ونجد فيه بدور ما سيسمئ من بعد بالهندسة التحليلية .

 ٣ – رسالته و في الحطير اللذين يقربان ولا يلتقيان » ، وهذه الرسالة هي أحد أشكال الكتاب انسابق ومن ثم لا يمكن اعتبارها كعمل منفصل .

٣ - جواب على سؤال سأله أمير المدرسة النظامية ببعداد : وهذه الرسالة هي موضوع مقالنا هذا وهي آخر عمل رياضي نعرفه لشرف الدين الطوسي وموضوعها : قسمة مربع معلوم إلى مستطيل وثلاثة ممحرفات على نسة معلومة .

فمن البين إذاً أن هذه الرسالة تهدف إلى بناء شكل هندمي يحقق علاقات عددية معينة بالمسطرة والبرجل ، واتبع الطوسي فيها طريق التركيب محافة التطويل ، ولكن هذا الطريق وحده لا يفسر لنا اختيار الطوسي للقيم العددية المتعددة ولا للأسية التي يقوم الما لتسلسل عرض تلك الأبتية . فإدا رجعنا إلى مفاهيم الطوسي ووسائله كما بعرفها من

كتابه ، في المعدلات ، لادراك وتحديد التحليل المستر وراء التركيب ينزما افتراض ترجمتين : الأولى ترحمة جبرية المسألة الهندسية تنتهي الى معادلة حبرية ، الثانية ترجمة هندسية المسألة اخترية ، الثانية البرجمتان المسألة اخترية هدفها الرد على السؤال المعروص بالبناء الهندسي . وهاتان الترجمتان تعبر ال عن علاقات جديدة بين الحبر والهلسة وعن تصور مختلف المشكلة التقليدية أعبى مشكلة التحليل والتركيب مند كتاب عمر الحيام في الحبر والمقابلة ورسالته في قسمة ربع دائرة على شروط مفروضة . ومن الحدير بالملاحظة أن الحبريي لا يهملون الوصول الى نتائج حسانية محددة ، كما يشهد بذلك رسالة الحيام ورسالة الطوسي التي يصددها ،

وأهمية مسألة نطوسي تعود إلى طريقة الحل وعما تعبر عنه من تصور للعلاقات التي دكرناها ولا ترجع الى صعوبة المسألة ولا إلى ندرة هذا النوع من المسائل ، همن المعروف أن هذا النوع تم يكن ادرأ قبل الحيام والطوسي من بعده على قلد توصل الرياضيون إلى حلول مسائل أكثر صعوبة أي تلك التي لا يمكن عملها بالمسطرة والبرجل كتقم الراوية إلى ثلاثة أقسام متساوية وغيرها من المسائل الهندسية التي تستازم قطوع المخروطات ،

ملاحظات حول كتاب المفروضات أأقاطن

دولد ـ سامبلونيوس

لقد عالحت المؤلفة رسالة المعروضات الأقاطن بالتفصيل في أطروحتها للدكتوراه أستردام ــ ١٩٧٧). وهي موحودة في فسختين تعودان للقرل الثالث عشر . احداهما والتي تحمل عنوال كتاب المعروصات لأقاطن موحودة في مخطوطة أيا صوفيا رقم ٢٠٣٠هـ في استنبول (٨٩ ط ٢٠٠٠ ط) . وتألف من ٤٣ فرضية في الهندسة المستوية وهماك ١٩ فرصية من النصف الأول تشكل رسالة منفصلة تحت عنوان كتاب أرشميدس في الأصول الهندسية . وهي موجودة في مخطوطة بانكيبور رقم ٢٤٦٨,٢٩ (١٩٤١ و ١٤٤٠ ط) . وقد نشر مكتب المشورات الشرقية العثمانية (حيدر أباد ٤٠ دكن ١٩٤٧) نخفة عربية هده المخطوطة مع مخطوطة بانكيبور رقم ٢٤٦٨,٢٨ (١٩٤٤ ف ١٤٤٠ و

كتاب أوشميدس في الدوائر المتماسة) وقد تم دكر أسباب قبول عنوان كتاب المفروصات وأقاطن مؤلفاً له في الفصل الثاني من الأطروحة .

وقد أضيف لعنوان مخطوطة بانكببور ما يلي - يو ترجم ثابت بن قرة الرسالة من اللغة اليونانية يلى العغة العربية بم. وسنعتمه على الحدس والتوقع في معرفة العنوان اليونانية الأصلي للرسالة والأسم الذي كان ينطلق على أقاطن في اليونانية إن فعل مرص رعا يفائل في اليونانية إن فعل مرص رعا يفائل في اليونانية قعل ($\pi \sigma_{1} (\sigma_{1} \sigma_{2} \sigma_{1} \sigma_{3} \sigma_{3})$) أو ممعى خساص يمكن أن يقابسل ($\pi \sigma_{1} (\sigma_{2} \sigma_{3} \sigma_{3} \sigma_{3})$) أو ممعى خساص يمكن أن يقابسل ($\pi \sigma_{1} (\sigma_{3} \sigma_{3} \sigma_{3} \sigma_{3})$) أو ممعى خساص يحكن أن يقابسل ($\pi \sigma_{1} (\sigma_{3} \sigma_{3} \sigma_{3} \sigma_{3})$) وليس للمؤلف علم بوجود أبسة إشارة أو كما في الحالة السابقة والأبي والسم العربي . وبهذا يمكنا الوصول إلى الأسم اليوناني الأكثر شيوعاً ($\pi \sigma_{1} (\sigma_{3} \sigma_{3} \sigma_{3})$) ولكنه لم يتم دكر أي رياصي بهذا الاسم .

وتتصمن الرسلة (الأطروحة – الفصل النائث) فرصيات جديرة بالاهتمام ، لكن دون وجود نظريات ذات شأن كبير وتعالج بعضى الفرضيات الحواص الأساسية للمثلثات وبعضها يدخل في نطاق علم المثلثات والأخرى تتصل بعثم البصريات . ومن خلال دراسة العلاقة بين رسالتنا ومجموعات ببوس فإنه رعا كان أقاطى أحد معاصري ببوس . ويمكن ملاحظة تأثيرات غتلفة على الرسالة (الاطروحة – الفصل الرابع) . والمكان الوحيد الذي له علاقة ماشرة بالرصيات العربية هو في رسالة ابن الهيم وفي خواص المئلث من حهة العمود » . وفيها يبرهن ابن الهيم على تقابل العرصيات ٨ – ١٠ و إن الميثم على تقابل العرصيات ٨ – ١٠ و إن يساوي ارتفاع المثلث متساوي الأصلاع الثلاثة بساوي ارتفاع المثلث متساوي الأصلاع الثلاثة بساوي ارتفاع المثلث متساوي الأصلاع . وعلى أية حال إن هذا التعميم ليس صحيحاً ولا في حالة مثلث متساوي الأصلاع . وعلى أية حال إن هذا التعميم ليس صحيحاً ولا القرن المئت رسالة أقاطن تحتفظ بقيمتها وأهميتها بالنسة لعلماء الرياضيات العرب في القرن الغرب في القرن الغرب في القرن الغرب في القرن المناه عشر كما هو واضع من الملاحظات الهامشية العديدة .

كناش في الطب العربي من القرون الوسطى : كتاب المئة لأبي سهل المسيحي

غادة الكرمي

أَلْفَت في اللمة المربية كتب طبية شاملة وعديدة بعد عام ٢٠٠ للهجرة . وكانت هده الكتب تعرف ناسم * كُناشات * . ويشير هذا الاسم إلى نوع معين من الكتب الطبية التي كانت تتصمن جميع المعلومات الاساسية بشكل محتصر حول الممارسات والنطريات الطبية في ذلك الوقت . وكلمة * كُناش * ليست عربية بل هي مشتقة من الكلمة السريانية * كُناش * على مر الزمن أكثر الكلمة السريانية * كُناش * على مر الزمن أكثر الكنت انتشاراً التي كاد يستخدمها الطبيب وطالب الطب على حدسواء

ال « كتاب المئة ه لأي سهل المسيحي كناش نموذحي يعود للقرن الرابع . والمسيحي طبيب عاش في بلاد الفرس وقد قبل إنه أحد معلمي ان سينا . توفي أبو سهل حوالي 101 . وقد ألف كتباً عديدة في الطب والمنطق وانفلسفة . ولكن أشهر كتبه هو و كتاب المئة ه . ولا يزال هذا الكتاب موحوداً فيما لا يقل على ٢٩ مخطوطة تم نسخها في مترة امتدت منذ القرن الخامس حتى أواخر القرن الماضي . وكان كُنّاش المسيحي يتمتم بقيمة عظيمة أيام طهوره وفيما نعد . ولكنه لم يترجم أنداً إلى اللغة اللاتينية في المصور الوسطى كما حدث لمؤلفات طبة عربية كثيرة .

يقدم هذا البحث نبذة عن حياة أبي سهل المسيحي ووصفاً لمحتويات كأناشه وتورد المؤلفة مقتطفات من النص العربي مع ترجمة انكليرية لها . ولم يتم تحقيق هذا الكتاب حتى الآن ومادة الدحث مستفاة من مخطوطات لهذا الكتاب . وتتعرض المؤلفة لمكانة وأهمية هذا الكناش وتبحث في الاسباب التي أدت الى عدم ترجمة هذا الكتاب الى اللغة اللاتينية خلال القرون الوسطى .

تقرير عن مخطوطة هامة للجزري

دو نالد هيل

يصف هذا النحث مخطوطة رائعة من كتاب الجزري في الآلات. وقد بشر المؤلف ترجمة انكليزية لهذا الكتاب وستصدر قريباً نسخة عربية قام بتحقيقها الدكتور أحمد يوسف الحسن (معهد الراث العلمي العربي — حلب). وكان يُعتقد سابقاً أن هذه المخطوطة قد تشتت كلها ، بالرغم من أنه قد تم الإشارة إلى وجود عدد من الأشكال في مجموعات عامة وخاصة . على أن ٧٠ ٪ من المخطوطة الكاملة قد عرض المبيع من قبل شركة سوثبيز في لندن في الرابع من يسان ١٩٧٨ واشترتها شركة سبينك في لندن أيضاً لقاء أكثر من ١٩٠٠ جنيه استرليلي ويعبر المؤلف عن امتنانه هاتين الشركتين لتعاونهما معه ولتزويده بصور فوتوغرافية ولسماحهما نشر هذا البحث .

لقد كتبت المخطوطة على ورق مصقول سميك ، قياس كل صفحة ٢١٩ × ٣١٤ مم بخط نسخي جميل جداً . وتحوي كل صفحة ٢٩ سطراً . ويشير حرد المنز (الكولوفون) الموجود في الصفحة الأخيرة إلى اسم الباسخ (فرح بن عبد اللطيف) وإلى تاريخ هذه النسخة (٧١٥ه / ١٣١٥ م) . ويعتقد أنه قد ثم اعداد هذه النسخة إما في سورية أو في مصر . وتأتي هذه النسحة (١١١٥ م من أنها ناقصة .

ويقدم البحث على شكل جداول تحليلاً كاملاً للمحتويات المتبقية من المخطوطة بمقارنتها مع المحتويات الكاملة المعروفة سابقاً من مخطوطات أخرى . ومن الأبواب الخمسين الأصلية هناك ١٤ ماناً كاملاً مع الأشكال . ويوجد الآن ١٠٦٠ أشكال صغيرة ورسوماً توضيحية من أصل ١٧٣ . ويوجد منها ١٩١ شكلاً رئيسياً . وقد تم نشر سبعة أشكال ملونة من المخطوطة في البحث المنشور في قسم الأبحاث الأجنبة من هذا العدد . وهي تتضمن فوارتين ورأس موارة وآلة موسيقية آلية وثلاثة أشكال لمضحة المكبسية (ذات الاسطوادين المتقابلتين) والمعروفة جداً الماحثين .

علم الفلك الاسلامي في اللغة السنسكريتية

دافيد بنجسري

يقوم هذا النحث بدراسة انتشار علم الفلك الاسلامي في الهند عبر قرون عديدة ويدرس أيصاً ردود الأفعال المحتلفة للعلماء الهود تجاه الطرق والنتائج التي مارسها زملاؤهم المسلمين . ويركز البحث اشكل خاص على قصية عشل هذا النقل في احداث تعيير هام في علم الفلك الهدي . ويرى المؤلف أن حلاً حزثياً لتلك القضية يكمن في عدم تفهم الهود لمتهجية علم الفلك عند المسلمين .

الساعة الشمسية الني وجدت في جامع ابن طولون في القاهرة

دافيد كينج وأويس جنان

إن آثار الساعة الشمسية الرائعة التي كانت قبل كسرها تزين جامع ابن طولون في القاهرة منذ سنة ٣٩٦ هجرية وتعيد زوار الحامع بالموقت الماضي من شروق الشمس والباقي إلى غروب كما وكانت تبين لهم وقت ابتداء صلاة الطهر والعصر قد اختفت أثناء البحوث التي احريت عليها على أبدي المستشرقين الفرنسيين المنتمين إلى بعثة نابليون في أوائل القرن التاسع عشر ولحسن الحظ لم تحتف الساعة إلا بعد أن رسمها أحد أعضاء المعثقة رسماً دقيقاً , وقد بحث المؤلمان في هذا الرسم من حديد لكي يحللا الخطوط المحتفة التي توجد على وجه الساعة كما بحثا في الجداول التي استخدمها الفلكيون في العصر المموكي ليخططوا ساعات من هذا النوع .



ثلاث ساعات شمسية من الاندلس

دافيد كينج

توجد في متاحف اسانيا ثلاث ساعات شمسية يرجع عهدها الى العصر الاسلامي في الاندلس . وقد بحث المؤلف في رسومها المختلفة التي ترتبط بالساعات الزماية من المهار وبوقتي صلاة الظهر والعصر . ومع أن إحدى هده الساعات من صناعة أحد الفلكيين المشهورين من الاندلس في أواخر القرل الرابع الهجري الا أنه يوجد في تحطيطها بعص الأخطاء . اما الساعتان الأحريان قصناعتهما تقريبية وقد حاول المؤلف أن يكتشف طريقة رسمهما ويظهر من الدحث أن صناعة الساعات الشمسية في الاندلس لم تكن على مستوى صاعتها في الشرق الاسلامي كما امكننا تصوره من الرسائل المؤلفة في موضوع تحطيط الساعات في العصر العباسي .

المشاركون في العدد

عادل أنبويا : يبحث في تاريح الحبر والهندسة - درّس تاريح العلوم عند العرب والرياضيات في الجامعة اللبنانية وفي الكلية الفرنسية للعلوم الاقتصادية في ديروت . تضم منشوراته دراسات عن الكرجي والشجاع بر أسلم والسموءل وآخرين من علماء الرياضيات العرب .

دافيد بنجري : أستاذ في قسم تاريح الرياضيات يحامعة براون . يتقن استحدام المصادر السنسكرينية والعربية واللاتبية والبونانية . وله اهتمام حاص في تاريح علم التنجيم .

جهاري في · محاصر في حامعة أوكلاند ، بيورلندا ، قسم الرياضيات . يعمل بشكل أسسي في التحليل العددي والحساب بالإضافة إلى تاريخ العلوم

لويس جنان : دكتور في الحقوق . تقاعد من عمله في سوك عدد من الدول العربية . وهدا ما حمله يهم نثاريخ العلوم عند العرب و شكل حاص في نظرية الساعات الشمسية في العصرين الوسيط والحديث

سامي حمارته : ياحث في المتحف القومي للتاريخ والتكنولوحيا ، معهد سميشنوليان ، وانسطن . مؤرخ في الطب والصيدلة عند العرب . له كتب ومقالات عديدة في هذا المجال منها ١٠٠ أصل الصيدلة والعلاج في الشرق الأدبى ، و و ابن الفف الطبيب والمعالخ والحرّاح ، .

ايفون دولد ــ ساميلونيوس · تدرّس حالياً تاريح الرياضيات عند العرب في جامعة هيدلمرع ها مشورات في تاريخ الهندسة عند العرب ـ وتعمل الآن في كتاب المفروسات لثابت بن فره .

وشدي واشد : أستاد بتاريخ العموم في المركز القومي الفرنسي للنحوث الفرنسية للعلوم ويمعها، تاريخ العلوم مجامعة باريس (. تتصمى منشوراته دراسات في تاريخ الجبر والهمدية

صلمان قطايه : أستاذ أمراص الأذن والأنف والحسجرة في كلية الطب يجامعة حلب . له مؤلمات وأبحاث عدة في تاريخ الطب .

هادة الكرمي , طبيبة ومؤرحة في الطب العربي , تقوم الآن عدراسات وأبحاث في تأريخ الطب عند العرب في معهد التراث العلمي العربي بجامعة حلب , الدوارد من. كتدي . استاد سايق في الحامعة الامريكية في نيروت واستاد باحث حاليًا في معهد العرب والمسلمين. التراث العلمي العرفي محلب. له امحاث وكتب عديدة في ثاريخ الطلى والمسلمين.

دافيد كينج · بعى بشكل أساسي في علم الفلك والرياضيات عند المستمين في العصر الوسيط . يعمل الآن في موكز المحوث الأمريكي بالقاهرة . له مشورات عديدة في علم الميقات .

هونالله هيل ٪ يزاول عمله كمهمدس . ويبحث في تاريخ التكنولوجيا العربية . ترجم كتاب اخرري الى الانكليزية ويقوم حالياً ناكال تحقين محلوطات بي مومى

ملاحظات لمن يرغب الكتابة في المجلة

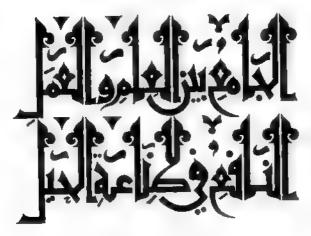
- ١ تقديم بسختين من كل بحث أو مقال الى معهد التراث العلمي العربي. طمع النص على الآلة الكاتبة مع ترك فراع مردوج بين الاسطر وهوامش كبرة لأنه يمكن أن تجرى بعص التصحيحات على النص ، ومن أجل توجيه تعليمات الى عمال المطبعة . والرحاء ارسال ملخص يتراوح بسين ٣٠٠ ٧٠٠ كدمة باللعبة الانكليرية إدا كان دلك ممكناً وإلا باللغة العربية .
- حرم الحواشي المتعلقة بتصنيف المؤلفات بشكل معصل وتبعا للارقام المشار البها أي النص مع ترك فراع مزدوح أيضا . وكتابة الحاشية بالتفصيل ودون أدني الحتصار .
- أ ــ بالنسبة لمكتب يجب أن تحتوي الحاشية على اسم المؤلفوالعنوان الكامل للكتاب والناشر والمكان والتاريح ورقم الحرء وأرقام الصفحات التي ثم الاقتباس منها ـ
- ب أما بالنسة للمجلات فيجب ذكر اسم المؤلف وعنوال المقالة بين أقواس صغيرة
 واسم المجلة ورقم المجلد والسنة والصفحات المقتبس منها.
- ج أما إذا أشير الى الكتابأو المحلة مرة ثانية بعد الاقتباس الأول فيجب ذكر اسم
 المؤلف واختصار لعنوان الكتاب أو عبوان المقالة بالاضافة الى أرقام الصفحات.

أمثلسية :

- أ ... المطهر بن طاهر المقدسي ، كتاب المده والتاريخ ، نشر كلمان هواي . باريس ۱۹۰۳ ، ج ۳ ، ص ۱۹ .
- ب عادل انبوبا ، و قضية هندسية ومهندسون في الفرن الرابع الهجري ، تسبيع
 الدائرة ، علمة تاريخ العلوم العربية. مجلد ١، العدد الثاني: ١٩٧٧ ص ٧٣.
 - ج ـــ المقدسي ، كتاب البدء والتاريخ ، ص ١١١ . انبـــوبا ، و فضية هندسية ١١ ، ص ٧٤ .

🏎 🎇 منشورات معهد النراث العلمي العربي 🛞 –

صسسار حديثها النص العربي السكامل لسكتاب الجسزري



تحقيق الدكتور أحمد يوسف الحسن

هذا الكتاب مرجع لا غنى عنه الورخي التكنولوجيا والعلوم • إنه النص المربي الكامل الذي يتحاور • ٥٠ صعحه والذي تم تحقيعه بالرجوع الى افصل مغطوطات الكتاب المعروفة في الوقت الحاصر • وقد تم اعداد ورسم ١٧٥ رسما يحدد دراسة دقيعة و بشكل مطابق المرسوم الاصلية • ويبحث السكتاب في محدل الواع الآلات الميكانيكية والهيدووليكية العربية التي تدين الابداع العربي في محال الهندسة الميكانيكية في القرن الناني عشر/النالت عشر الميلادي ويحتوي الكتاب على فهرس شامل للحصطلحات الصية مع معجم للمصطلحات بالانكليرية والعربية ، مما يصعي على الكتاب فيمة كبيره ا

تعت رعاية السيدرئيس الجمهورية الندهة العالمية الثانية التأريخ العلوم عند العرب

٥ ــ ١٢ نيسان ١٩٧٩

التسجيل طرال ٤ نيسان

حلقات البحث :

١ ـ تاريخ الجير العربي

٢ _ مكانة الثقافة العلمية في الحضارة الإسلامية

٣ _ انتقال العلم العربي الى الغرب اللاتيسي

الجلسات العلمية :

الطب

الزراعة والحبوان

فنسفة الملزم وانتفالها

العلوم المقيقة (رياضيات ما فلك ما تنجيم ما فيرياء)

الكرن _ الكيمياء _ المفتاطيسية _ علوم الارص

التكىولوجيا

أبحاث عامة في تاريخ الملوم العربية

* * *

نوجه المراسلات الى :

الأنسة أمل رفاعي _ مكتب الرئيس _ جامعة حلب

خلب سالجمهورية المربية السورية

مطبورعات معهد التراث العلمب العربي بجامعة حلب

آ ۔ الکتب : ا .. احمد يوسف العسن وتقى الدين والهندسة الميكانيكية المربية معكتاب الطرق السنية في الآلات الروحانية من القرن السادس مثير ١٩٧٦٠ ٨ دولارات : رياضيات بهاء الدين العاملي ٩٥٢ ــ ١٠٤١/هـ ١٥٤٧ ــ ٧ - جيلال شيوقي A دولارات - 1471 - 1377 * معطوطات الطب والصيدلة في المسكتبات العامة يحلب ١٩٧٦ · ء - سلمان قطسناية ٠١ دولارات إ - ادوارد كندي وعماد غائم : ابن الشامل فلكي عربي من القرب الثامن لهجري/الرابع البلادي ــ ١٩٧٦ -٦ دولارات أفراد المثال في أسر الطلال للسروسي • ء ـ ادوارد س • كثلى جزء (١) : الترجمة الانكليزية -جزء (۲) · التعليق والشرح (بالانسكليرية) · Lotte Yo ب معهد الثراث العلمي العربي : أبحاث المدوة العالمية الاولى لتاريخ العلوم عند العرب (المنعقدة بجامعة حلب من ٥ ــ ١٢ تيسان ١٩٧٦) ۳۵ دولارا الجزء الاول الإبحاث باللعة العربية ٠ الجرء الثاني الايحاث باللفات الاجنبية أبعاث المؤتمر الثاني (١٩٧٧) والثالث (١٩٧٨) للجمعية السورية لتاريخ العلوم . (تحت الطبع)

ب ـ الدوريات :

1 معلة تاريخ العلوم العربية: دورية عالمية متحصصة تصدر مرتبين كل عام ، المجلد الاول (١٩٧٧) ، المجلد الثاني (١٩٧٨) الاشتراك السنوي ٦ دولارات ، ٢ ماديات حلي: حولية تبحث في تاريخ الحضارة والآثار والمعلوم : المحدد الاول (١٩٧٥) العدد الواحد - ١ دولارات للعدد الواحد - ١ دولارات للعدد الواحد - ١ دولارات للعدد الواحد - ١٠٠٠)

٣ ـــ رسالة معهد التراث العلمي العربي: نشرة دورية تعددر أربع سرات كل عام ١٠ الاشتراك السنوي ٤ دولارات بالبريد العادي ، ٥ دولارات بالبريد العادي .



لأبي بكر عمد بن زكريا الرازي (١٥٠ / ١٥٠)

قام الدكتور سدمان قطاية بتحقيق هذا الكتاب عن ثلاث ضطوطات وهي الوحيدة المعروفة . والكتاب وثبقة متميزة لأنه يعالج قصية تشحيص الأمراضي على شكل سؤال وجواب .

ويحتوي الكناب على مقدمة وفهارس وحدول المحتويات وتنصمن العهارس معجماً بالمصطلحات الفية القديمة والحديثة . يقع الكتاب في ١٣٥٠ صمحة وفيه ٧ رسوم .



فهرس المجلد الثاني

المدر الأول ، ص 1-230 المدر الثاني ، ص 231 - 450 - 15 YA -

> [ابن البيطار] ، السفرجل ، ملحوظة هامشية على كتاب الخامم للفردات الادوية والاغتية لابن البيطار (بالانكبرية) ، 143 .

> > [ابن رضوان] ، انظر تطاية .

[ابن المقار] ، انظر كينج

[ابن مدي] ، مقالة في تيون الفصل بين صناحة المنطق الفسقى والتحو العراب ، (بالعربية) ، . 156 ء ملحمي بالانكلازية ۽ 156

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[ابن مراق] ، ادخال مفهوم الثلث القطبي من قبل آن نصر بن مراک ۽ (بالفرنسية) ۽ 126 ملحمن بالبرية (169 .

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3. In the transliteration of words written in the Arabic alphabet the following system is recommended:

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For long vowels the following discritical marks are drawn over the letters $\hat{a},~i,~i.$

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NOTES ON CONTRIBUTORS

Adel Anhouse, works on the history of algebra and geometry. He has taught the history of Arabio science and mathematics at the Lebanose Luiversity and at the French Faculty of Economics in Bearut His publications include studies on al-Karaji, Shujā' b. Aslam, al-Samaw'al, and other Islamic mathematicions.

Yvonne Dold-Samplenius, presently teaches the history of Arabic mathematics at the University of Heidelberg. She has published studies on the history of Arabic geometry and is currently working on Thabit b. Quira's Kuib al-mafrādā.

Sams K. Hamarneb, of the Smithonian Institution's National Museum of History and Technology, is a historian of Arabic medicine and pharmacy. He is the author of several hooks and articles on these subjects, including Origins of Pharmacy and Therapy in the Near East, and The Physician. Therapist, and Surgeon, Ibn al-Quff

Donald Hill, is a practicing engineer whose avocation is the history of Arabic technology. He has published an English translation of the treatise of al-Jazari, and is currently completing an edition of manuscripts of the Band Müsä.

The editors have just learned with esdaess of the sudden death of Louis Janin, doctour an drust. He had retired some time ago from a hanking career which included residence in various Arabic-speaking countries. This led to his interest to Arabic strence, in particular medicinal and modern gramonics.

Ghada Kurmi, is a physician and bistories of Arabic medicine. She is engaged in research at the Institute for the History of Arabic Science.

Salman Kataye, is Professor of Otoshynolaryngology at the Faculty of Medicine, University of Aleppo, He has published several works on the bistory of medicine

E.S. Kennedy, sometime professor of mathematics at the American University of Beirut, is currently a research professor at the Institute for the History of Arabic Science. He has published several atudies in the bistory of Arabic-Islamic science.

David A. King, whose professional interest as in the astronomy and mathematics of medieval Islam, is resident in Egypt. In particular, he has numerous publications in the field of astronomical timekeeping

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Garry J. Tee, is a sensor becarer in the mathematics department of the University of Auckland. He works chiefly in the fields of numerical analysis and computing, but also in the history of science.

Summary of the Arabic Article in This Issue

A propos du discours "Fi'l-tatarruq fi'l-fibb ilà al-sa'āda" (Vers le bonheur par l'intermédiaire de la médicine de "Ali b. Ridicân)

SALMAN KATAYE

Nous présentons pour la première fois, le texte complet du manuscrit Maqāla fi'l-tajarruq fi'l-tibb ilā al-sa'āda de 'Alī ibn Ridwan. Ce texte, unique, est conservé jusqu'à présent dans la bibliothèque de Ḥakim Uglū Bacha.

Ce discours revêt une certaine importance.

Il nous permet de déterminer la date de naissance de 'Alī ibn Ridwān et de calculer son âge avec précision.

Nous pouvous relever dans ce même traité certaines évocations portant sur la conception qu'avait Ibn Ridwan de l'enseignement médical. Il prétend qu'on peut étudier la médecine sans professeur. Ce qui lui a attiré beaucoup de critiques.

Dans al. Tatarriq, il expose de nouveaux arguments rendant son point de vue plus acceptable.

La trossième partie de son discours est consacrée au développement du titre de ce dernier, il explique alors l'aspect philosophique de la pratique médicale. C'est une conception religieuse qui s'appuie sur l'idée que la médecine est un acte de charité et un moyen de satisfaire Dieu et ménter le paradis.

Enfin, dans ce même discours, Ibn Ridwân aborde l'histoire de la médecine pré-islamique. Nous remarquons qu'Hippocrate et Gaben sont, d'après lui, les senls dignes d'être estimés et respectés, surtout Galien, dont les ouvrages sont, à son avis, d'une valeur incontestable, il s'en prend même durcment à ceux qui l'ont critiqué, tel Rhazes. science to mediaeval Europe. Although the two Dutch publishers are to be commended for publishing these two volumes, it might have been more appropriate for the entire text to have been published in the scholarly journal where it began to appear.

GARRY J. TEE

Computational Mathematics Unit, Department of Mathematics, University of Auckland, Auckland, New Zealand

- H. L. L. Busard, The Translation of the Elements of Euclid from the Arabic into Latin by Hermann of Carinthia (?), Books I-VI, Leiden, E. J. Brill, 1968, 142 pages.

 (Books I-VI) 24 f.
- H. L. L. Busard, The Translation of the Elements of Euclid from the Arabic into Latin by Hermann of Carinthia (?), Books VII-XII. Amsterdam, Mathematisch Centrum. 1 977. 198 pages Mathematical Centre Tracts 84

In 1271, Gerard d'Abbeville bequeathed to the Sorbonne a Latin manuscript. (Bibl. Nat. Latin 16646) of Euclid's Elements, Books 1 to 12, and that text has now been printed by Busard. Books 1 to 6 are contained in the 1968 volume (which is reprinted from Janus, 54, 1-2, (1967)), and Books 7 to 12 are contained in the 1977 volume - Books 7 to 9 had first been printed in Janus (59, (1972), 125-187). The manuscript does not contain Euclid's Book 13, on the regular polyhedra.

The Latin text is obviously translated from Arabic, and there is some tenuous evidence suggesting that the translator might have been Hermann of Carinthia (fl. 1143). Hermann is known mainly as the translator from Arabic into Latin of Ptolemy's Planisphere (which has survived solely through his translation), and as co-translator with Robertus Ketenensis of the Koran.

This Latin translation of Euclid appears to be intermediate in time between the 3 versions ascribed to Adelard of Bath (fl. 1110-1142), and the version ascribed to Campanus of Novaro (c 1205-1296), which was used for the first printed edition of Euclid.

It is approximately contemporary with Gerard (c1114-1187) of Cremona's translation, which includes the pseudo-Euclidean Books 14 and 15. Campanus made use of the versions by Adelard, but Bussid considers that this version by Hermann (?) was not used by Campanus.

Busard analyses and compares the several known Arabic and Latin texts of Euclid, in order to determine which Arabic version was used as the source of this text. In the 1968 volume, after an analysis of Books 1 to 6 he considers that it was translated from Thabit ibn Qurra's revision of the translation by Ishāq ibn Hunayn. However, in the 1977 volume, after analysing the full text, he considers it more likely to have been translated from the very first Arabic version of Euclid, the translation made by al-Ḥajjāj ibn Yūsuf ibn Maṭar under the patronage of Hārūn al-Rashīd.

This Latin text cannot have had much influence on the development of geometry, since no other manuscript of it is known, but it is of some interest for the evidence which it presents concerning the transmission of Arabic from a manuscript (in Uppsala) in which the work is attributed to al-Fārābī (who died in 339/950). In fact, in a later book (A.K. Kubesov, Matematicheskoys naslediye al-Fārābī, "The Mathematical Heritage of al-Fārābī", in Russian, Izd. "NAUKA"Kaz. SSR, Alma-Ata, 1974), Kubesov explains pp. 52-53) that the manuscripts of the work On Geometrical Constructions incorporate almost the entire book On Geometrical Figures (written by al-Fārābī, according to the Uppsala manuscript), together with some additional material, presumably supphed by Abū'i-Wafā'. On p. 29, Toomer mentions citations of al-Fārābī's commentary on Ptolemy's Almagest. "Which does not appear to be extant". However, Kubesov (1974) devotes chapters 4 and 5 to analysing that commentary (from a manuscript in the British Museum), and the publication of a Russian translation of al-Fārābī's commentary on Ptolemy's Almagest was announced by B. A. Rozenfel'd on p. 109 of the first issue of this Journal.

Toomer's edition of Diocles is a valuable contribution to the history of Greek and Arabic science.

Note on the Text

Dr. N. Kanawati has examined the reproduced manuscript, and he informs me that Toomer has made a very accurate translation of the difficult non-mathematical introduction (sentences 1 to 37); except that in the opening invocation the phrase "grant long life" is much more likely to be "grant help", i. e. a'in instead of a'mir. The word hattā (= till, to, even), repeated in sentences 3 and 4 in the Arabic transcription, should certainly be rendered matā (= when). Compare these two instances with the way hattā is written in sentences 22, 24, 36 and 37. Curiously however, Toomer's translation in both cases is the correct one — "when". The emendation of the important corrupt name (in sentences 3 and 4) to "Zenodorus" is probable, but hardly "certain", as Toomer asserts.

G. J. TEE

Computational Mathematics, Unit, Dept. of Mathematics, University of Auckland. 10-16 deal with the doubling of the cube. (Propositions 6 and 9 are trivialties, which Toomer considers plausibly to be spurious additions to Diocles' text.) Propositions 1, 4 and 10 contain the carliest known treatment of the focus and directrix of the parabola—the Conics of Apollonius treats the foci of ellipses and hyperbolae, but it is remarkable that none of his surviving writings mention the focus of the parabola.

The theory of come sections was invented by Menaechmus (mid-4th century), who named the 3 types as the "section of an acute-angled cone", "section of a right-angled cone" and "section of an obtuse-angled cone"; whereas we use Apollomus names of "ellipse", "parabola" and "hyperbola" respectively. Archimedes (killed in 212) used Menaechmus' "cone" names, even though he effectively defined the curves by their equations in Cartesian coordinates, rectangular and even oblique Diocles consistently calls the parabola a "section of a right-angled conr". Ellipses and hyperbolae occur only in his proposition 8, and there he uses their modern names, supposedly invented by his exact contemporary Apollonius. Could the Conics have been 'published' while Diocles was writing his book, inducing him to change his concept of the conic sections? Toomer suggests alternatively a modification of the accepted history of conic sections, according to which the names "ellipse" and "hyperbola" were invented together with the "coordinate" definition of the curves, and Apollopius standardized those names instead of inventing them.

Eutocius quoted Diocles' proposition 7, but he re-wrote propositions 8,10,11,12 and 13 to accord with the geometric style (Apollonian) regarded as orthodox in his day. In particular, as had been suspected by some previous investigators, the references to the Comes in Eutocius' version did not occur in Diocles' text. It is noteworthy that Diocles refers 4 times to a flexible strip of horn, used exactly like a modern draughtsman's spline for drawing a smooth curve through a set of points.

The 16 diagrams omitted from the manuscript have been restored most effectively by Toomer. Geometrical texts can permit such complete reconstructions of missing diagrams, an interesting contrast with, say, a biological text, where such a reconstruction would usually be impossible.

On p.23 Toomer refers to an elegant construction of a parabolic mirror with a given focal distance, which he ascribes to Abu'l-Wafa (mid 10th century), and which has been printed in French and in 2 Russian versions. Toomer notes that Krasnova's translation was made from a manuscript (in Istanbul) of Abu'l-Wafa's book On Geometrical Constructions, but that the translation by A. Kubesov (al-Fărābi, Matematicheskive traktaty, "Mathematical Treatises", in Russian, Alma-Ata, 1972, pp.104-106), was made

book had been translated into Arabic, since Eutocius' extracts say nothing about burning mirrors (except in the title).

A few years ago Dr. Fuat Sezgin directed G. J. Toomer's attention to an Arabic manuscript of mathematical writings in the Shrine Library at Meshhed in Iran, including an Arabic version of Diocles treatise On Burning Mirrors. That manuscript (dated A H. 867 1462 3) is a carelessly written version of an anonymous well-written translation of Diocles' work, and it is the only known manuscript of that work (apart from an inferior transcript of that Moshhed manuscript, now in Dublin). Blank spaces are left in the manuscript where the diagrams should have been inserted.

Toomer's admirable edition consists of Preface and Contents, then an Introduction (pp.1-33), the edited Arabic text with facing English translation (pp. 34-113), photographs of the entire Arabic manuscript of Dioclea' treatise (pp.114-137), Commentary (pp.138-175), Appendix A with text and translation of Eutocius' excerpts (pp 177-201), Appendix B with other ancient and mediaeval proofs of the focal property of the parabola (pp.202-204), Appendix C (by Otto Neugebouer) on Archimedes' problem and Diocles' solution (pp.205-212) Appendix D (also by Neugebauer) on a non-standard parabolic mirror (pp.213-216), Bibliography (pp. 217-223), Index of Technical Terms in Arabic (pp.224-238) and a General Index (pp.239-249). The elegant printing of the Arabic text was generated by a computer; but it is amusing to observe that the 12 pages of Eutocius' Greek excerpts (with claborate textual apparatus) are reproduced from bandwriting, although Greek words and phrases are printed neatly in the Introduction. There can have been few mathematical books of recent times in which some footnotes have been written so casually in Greek.

One of the most important features of the Arabic text is that it enables Toomer to determine the date of Diocles. The 4th and 5th sentences associate Diocles (in Arcadia) with a person whose name is rendered corruptly, first as 'Byūdām-s and then as 'Ynūdām-s: in view of the careless writing of the Meshhed manuscript these corruptions are emended by Toomer to Zīnūdūrus, which corresponds to Zenodorus. Now, Zenodorus was a mathematician of the early -2nd century, best known from the fragments of his pioneering work on isoperimetric problems. Thus, Diocles appears to have been a close contemporary of Apollonius, the Great Geometer himself. This dating raises interesting questions about the chronology of the theory of conic sections.

Diocles' text contains 16 diverse propositions. Propositions 1, 4 and 5 deal with parabolic mirrors (including parabolicids of revolution), propositions 2 and 3 treat spherical mirrors, propositions 7 and 8 deal with a problem posed by Archimedes (expressible as a cubic equation), and propositions

as "social parasites", thrown out of society to meet their own fate. They inevitably sought ascetic hving. And in their ascetic conditions and meditations they dreamed of rebuth for a happier rejuvenation. They tended to practice spiritual exercises and to utilize the herbo-metallic drugs of the Rasayana (p.117) to attain that end. But interestingly, the author comes out triumphantly and pointedly when he concludes by emphasizing his praiseworthy statement that "Indian medicine is unique in recognizing rejuvenation, and Indian philosophy is unique in aiming at immortality". (p. 118).

I must conclude by saying that here is an excellent literary contribution, a book deserving the attention of historians of science, cultural history, and the occult. It shows a buk in the history of alchemy between countries and cultures in the East and in the West - a connection worth extoring and ducidating. It fills a gap in this new and dynamic topic by exploring the origins and development of alchemy, and the philosophy of this ancient "art".

SAMI K. HAMARNEH

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G. J. Toomer. Diocles, On Burning Mirrors, The Arabic Translation of the Lost Greek Original. Edited with English translation and commentary. Berlin-New York, Springer-Verlag, 1976, 249 p. Sources in the History of Mathematics and Physical Sciences. \$27.90.

In the 6th century Eutocius (a friend of Anthemius) produced a valuable series of commentaries on ancient Greek mathematics, written perhaps at Alexandria. In his commentary on Archimedes' Sphere and Cylinder II he quoted passages from several earlier authors on the problem of doubling the cube, and in particular he quoted (or rather, he paraphrased) several pages from a treatise On Burning Mirrors by a certain Diocles, employing conic sections and also a special cubic curve for solving cubic equations. That commentary by Eutocius was translated together with the text of Archimedes into Arabic and then into Latin (first by William Moerbeke in 1269, translating from the Greek text), and later into many modern languages. They have been printed together in every major edition of Archimedes since the editio princeps, in 1544.

Much controversy has raged over the dating of Diocles, with various investigators suggesting dates from the 3rd century B.C. to the lst. The full Greek text of Diocles is lost, but in 1905 Eilhard Wiedemann drew attention to a 14th-century Arabic encyclopaedist's reference to Diocles having proved that burning mirrors should be paraboloidal; which suggested that Diocles'

Herbs were plentiful, easy to secure, and most convenient to gather and utilize. Soon the herbometallic drugs developed. Finding and compounding such "mirscle drugs and panaceas" led to the belief in rejuvenation, and eventually to immortality—the final goal of Rasayana. Here enters, likewise, the philosophic-religious thinking and exercises—yogs.

This reviewer disagrees with the author in identifying such a process with the elixir (Arabic iksir) of the Muslim alchemists. Basically, the iksir (or the philosopher's stone) is considered to be that special element or compound that, once prepared and "isolated", when treated with lesser metals transforms them into silver and gold. This Islamic notion of alchemy based on Greek writings embodies the rational concept that elements are transformable from one condition to another, hence from one metal into a more honorable one under the right amount of pressure, temperature, and other natural forces and conditions. To the alchemist, this meant the application of fire and other techniques and "potent" ingredients including the elaxir to speed up the work of nature. His chemicals, fire, drugs, and equipment achieve in a very short interval what might take nature a long time to attain.

Indian alchemists introduced instead, imaginary and possibly pagan religious and philosophical practices, exercises, and theories quite foreign to their Muslim counterparts. The Indian alchemist believed in resurrection of the body as explained in Christian teachings as well as in heathen mythology. Here it is believed that the perishable part of the human put on the imperishable nature, and the mortal that is capable of dying put on immortality, acquiring freedom from death. These constituted the true precepts of Indian alchemy as explained by the author.

In reviewing and examining several original Arabic alchemical treatises even those abounding with symbolism, this reviewer found that Muslim alchemists were primarily seekers of material riches. Religious and spiritual values and rewards were found there no more than in contemporary writings in the arts and sciences. More "picty" entered into later compilations as a cover-up for failure, or as a hypocritical cloak put on for protection, or as a ray of hope amid continuous disappointments in achieving what had been sought in vain. Much "spirituality" was perhaps to deceive or for self-deception. In the Arabic alchemical literature, kimiyā is essentially an art, an bonorable one (sinā'āh sharifāh) by which material ends are attained and riches gained with high prestige. It was not primarily intended to promote imaginary spiritual values or ascetic dreams and religious aspirations.

In fact, one finds it difficult to appreciate the logic followed by the author in assuming the original theory for ascetic rejuvenation and immortality as the origin of alchemy. He states that senior citizens were looked upon

Book Reviews

S. Mahdihassan. Indian Alchemy or Rasayana in the Light of Asceticism and Gertatrics, New Delhi (India), Institute of History of Medicine and Medical Research, 1977. x + 139 pages, \$5.00.

Here at last is a book on alchemy in India that departs from the traditional historical studies carried out in the West for the last two centuries. It makes for some of the finest reading on the subject. Although this reviewer disagrees with the author on many essential interpretations, this in no way minimizes the importance of a presseworthy contribution to the history of alchemy.

For clarity and organization. Dr. Mahdihassan divides this brief text into over sixty chapters—a case of oversimphtication. But the reader will greatly benefit from its objective, straightforward approach and thoroughness.

Following a foreword by Prof. S. H. Nasr, the author presents a very useful introduction summarizing his analysis of the topic and the discussions that follow. He also gives a select bibhography and seven previously published illustrations. In the discussions, he asseverates the antiquity of alchemy in India, associating its origin with yoga. He refers to this "art" as a living "cultural fossil", the product of alchemists who led a life of asceticism and sought gernatric treatment. He explains how human concepts and the appliestion of asceticism changed man's belief from animism to dualism in a developed society realizing the creation process. Here the interpretation of how the two opposite sub-souls of male and female (the Yang and Ym of China and the Brahman and Atman of India) in their union led to immortality dream and goal of Rasayana. This, in the author's opinion, is the source of Indian alchemy defined by Patanjali as the Rasayana. It denotes health restoration, and with its specially prepared medications causes rejuvenation and makes one immortal. At this point, the author introduces the Indian deity, Shiva, who modified Rasayana and founded alchemy, which in turn modified him. The connection, however, seems the result of legendary traditions and folklore rather than a historical development. The insistence of the author upon defining the exact origin of alchemy, and upon naming its founders seems to be a well-nigh unattainable pursuit.

To interpret the appearance of Rasayana, the author skilfully describes the impact of two disciplines: medicine and philosophy, or rather, Indian philosophic-religious thinking. Since healthy living, virility, and longevity were the alchemist's primary objectives, medicine then entered the picture. rabbinical text is placed between the two treatises written by Ibn Mu'adh, namely Kutāb majhūla (fols. 49-74) and the Matrah al-shu'ā'āt (fols. 76-81), it clearly refers to the Kutāb al-asrār (fols. 1-48) because it is the only one in which mechanical devices, corresponding to Ishāq b. Sīd's allusions, are mentioned.

All this, of course, agrees with the fact that all the dates mentioned in the manuscript (until fol. 105) correspond to the reign of Alfonso X. We have, therefore, the only specimen remaining of a manuscript copied in his Toledan court. The link suggested by Hill, between the use of inercury as a source of power in one of the clocks described in the Kitāb al-asrār and in another one contained in the Libros del saber de Astronomía, becomes very probable.⁴

4. Furthermore the Libra de las Armellas quates Ibn 'du'adh's system for saguim al-buyút in a way samilar to Ibn Mu'adh's in his Matrah al-shu'á'ái which, as we have seen, is found in the manuscript.

Note

The "World Directory of Historians of Mathematica", first published in 1972, has just appeared in a second, revised and much enlarged edition. Listed are about 1200 scholars who are devoting at least part of their time to teaching and/or research in the history of mathematics. Besides the current address, the main fields of interest of each person is given. Indexes by fields and by countries follow the alphabetical list.

Prepared by K.O. May (1915-1977) and Laura Rocbuck, the new edition (iv + 92 pp.) may be ordered from the International Commission on the History of Mathematics, 11 Evergreen Gardens, Toronto, Ont. M4G 1C4, Canada. Price: \$7.00 if payment is included with order; \$1.00 extra for postage on billing with shipment.

C. J. SCRIBA

NOTES AND CORRESPONDENCE

A Further Note on a Mechanical Treatise Contained in Codex Medicea Laurenziana Or. 152

MARIA VICTORIA VILLUENDAS*

The importance of the Codex Medices Laurenziana Or. 152 has recently been emphasized by Drs. D. R. Hull and A. I. Sabra. I also have been acquainted with this manuscript since 1973, although at that time, I was mainly interested in another of the works contained in it; the Kitāb majhulāt qisi al-kura by Ibu Mu'adh al-Jayyānī which was the main subject of my Ph. D. thesis. Therefore I have a certain knowledge of the Ibn Mu'adh style which allows me to confirm Sabra's hypothesis; I do not think Ibn Mu'adh can be considered the author of the Kitāb al-asrār (it natā'ij al-afkār and agree with Sabra concerning the name of the author (Ah)mad or (Muham)mad b Khalaf al-Murādī. The nisba al-Murādī appears frequently in Ibn Hayyān's Muqiabis and in other Andalusian texts of the 10th and 11th centuries. He might, of course, be the Abu'l-Hasan 'Abd al-Ralimān b. Khalaf b. 'Asākir mentioned by Sā'cīd of Toledo, as proposed by Sabra.

In the preliminary survey of the Kitāb al-asrār certain data contained in fol. 75 should be taken into consideration. In it there is a text written in Andalusian dialect, but in rabbinical Hebrew script. I have been able to read it thanks to the very valuable help of Professors Fernando Diaz. David Romano and Juan Vernet of Barcelona University. The text states that Ishāq b. Sid, the famous Jewish translator and scientific collaborator of the Castillian King Alfonso X, was the copyist of the manuscript. He knew only one manuscript of the work, the one he used, which increased his difficulties in understanding the Kitāb al-asrār. But his efforts led him to an almost complete teconstruction of the majority of the models described in the work, and he fuled to understand only a few of them due to the incomplete state of the original manuscript or to difficulties impossible to overcome. Though this

[&]quot; University of Barcelona.

Donaid R Hill, "A Treatise on Machines by Ibn Mucadh Abu Abdullah al-Jayyani" JHAS, 1 (1977), 36-46.

A. f. Sabra, "A Note on Codex Biblioteca Medicea-Laurenziana Or. 152" JHAS, 2 (1977), 276-283.

^{3.} Read at the University of Barcelona on the 2nd October 1975, now in press.

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Thus his contributions to our field, while revailing in significance those of many professionals, were made by an amateur. They were carried through in time snatched from the requirements of a demanding profession. All the more remarkable was it that, for example, any book review written by Hermelink was the fruit of deep and meticulous examination of everything the volume contained. This quality of his was the source of shamed admiration on the part of those of us who resent every minute spent in reviewing the books of others as being time lost to one's own work.

His own publications in the history of science were wide ranging, and included: recreational mathematics, number theory, magic squares, analemma methods, trigonometry, and Archimedean treatises which have survived in Arabic only. To these topics he brought all the virtues traditionally associated with German scholarship. His untimely death is a grievous loss to the many colleagues who counted him a personal friend, and a setback to the history of Arabic science.

Éloge

HEINRICH HERMELINK



11 DECEMBER, 1920 - 31 AUGUST, 1978

By E. S. Kennedy*

As an infant, Heinrich Hermelink was a victim of poliomyelitis, and survived only as a severe cripple. Hence for him mere day-to-day living, let alone professional accomplishments, represented a continuing triumph over dire adversity. The physical disability made any public appearance inevitably conspicuous, and his wheelchair, his gracious wife, and he made up a porgnant group familiar to historians of science attending scientific meetings.

In 1947 Hermelink graduated in physics from the Munich Technischehochschule. Following this he studied oriental languages and the history of mathematics at the University of Munich, taking the doctorate in 1952.

From a remark dropped by him in a conversation, one gathers that an academic career would have been most congenial (his father was a professor of church history at the University of Varburg), but continuing medical treatment demanded a more lucrative vocation. He entered a patent agency in 1952, and in 1957 commenced independent practice as a patent lawyer.

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٦- باب في معرفة القبلة من الرسالة في العمل بالاسطولاب لابسن النسطاح

المصدر : مخطوطة لندن المكتبة البريطانية اضافية ٩٦٠٢ ، ق ١٨ ط ـــ ١٩ و

باب في معرفة القبلة اذا اردت معرفة القبلة بهاذا بحذ ارتفاع الشمس وضعها على مثل ارتفاعها واعرف سمتها واستخرج منه الحيهات الاربع على ما ينيت في الباب قبل هذا فاذا عرفته فاثرك الاسطرلاب على حاله ولا تحركه على ما هو عليه ثم در العصادة دون تحريك الاسطرلات على ثلاثين درجة في ربع الارتفاع فما قابلت الشطية من الجهات فتلك هي القبلة بقرطة على خمس واربعين درجة وقبلت في معلقات عن ابي القاسم الصنيرى تضع العصادة على ثلاث وعشرين وحبدت في معلقات عن ابي القاسم الصنيرى تضع العصادة على ثلاث وعشرين المرجة ادا كان عرض البلد لح ل هذا الدي دكرته هو مدهب اهل صناعة التعديل واما المفها فيرون الربع كله قبلة والمسجد الجامع بقرطبه على ستين واكثر مساجد قرطبة على مذهب المبايل فاستخرح على ما شقت من الجهات الاربع على ما تقدم ثم در العصادة الى ربع اجزا الارتفاع على ما شقت من المحلاد التي ذكرت ال القبلة عليها بقرطبة فافهم .

التحقيق : ؛ – في الاصل : يقسم ﴿ – في الاصل : ثلاثا .

القبلة ال شا الله [وال] اردت ال تعرف دلك بوجه اخر نستوحمى(؟) وقت مغربها في البوم السادس [عشار السالع عشر او التامن عشر من يونيه فانها في هذه الثانة ايام يكود مغربها واحد فتقيم عودا قايما مستويا او تقف انت قياما مستويا فحيث انتهى طلك او ظل العود فهو سمت القبلة بمشية الله تعلى وتوفيقه والعمل يودياك [1] الى شي واحد وبالله التوفيق .

۴ قطعة من كلام مؤسى بن ميمون في عمل البلاطة

المصلو · كابانبلاس ص ٤٠٤ (ويلاحظ ان الاصل مكتوب الحروف العبرية) رحامة تسى في الارص وترسم فيها خطوط مستقيمة مكتوب عليها اسماء الساعات وهي دائرة وفي مركز تلك الدائره مسمار قائم على روايا قائمة كلما سامت ظل ذلك المسمار لحط من تلك الخطوط علم كم ساعة مضات من النهار واسم هذه الآلة المشهور عند المنجمين البلاطة .

٤_ قطعة من كتاب في الأنواء للحسن بن علي الأموي الفرطبي

المصدر : مخطوطة اسكوريال ٩٤١ ، ق ٢٦ ظ

القول في رسم القبلة ثعلم القبلسة بالاندلس بان تصع القطب على كتفك الايسر ثم تستقبل اجنوب فما لقى بصرك فهو القبلة والقطب .

هـ قطعة من الرسالة في العمل بالاسطرلاب لابسن الصفسار

المصدورة مياس، النص العربي، ص ١٥٠

. والثلاثوِن درجة من الربع الشرقي الحنوي التي هي سمت للقبلة بقرطبة

وما قرب منها . . .

رافيد كينج 388

لوحا او ححوا مستوى السطح فتدير فيه دايرة دورها قنو الشبر وتقيم في مركزها قامة قلم نصف القطر على اعتدال ثم ترصد طله في صدر النهار فاذا بلع طرف الدايرة علم عليه بنقطة قبل أن تميل فادا رالت الشمس ترصده ايصا فاذا بلع الحائب الاخر من الدائرة علم عليه بنقطة ثم تمنط من يتن التقطير على حرف الدائرة بنصفير وتعلم على وسط . ° بنقطة ثم تمنط حطا من ارض القامة الى بقطة الوسط فيكون هو خط [الروال] فادا وقع ظل القامة على الحط فهو قصف النهار بالاعتدال ثم تاخذ البلاطة حين يقع طل القامة على انحط يشتها في مكان مشرف على اعلى حر معجول اثبات وتستقبل بوجوه الساعات جهة الجنوب حتى يقع طل المرودين على الحطين اللذين هما احر السادسة واول الساعة ثم تنقن لصوق البلاطة بالجدم اتفانا حسنا لبلا تزييه الرياح ثم نتعاهد والله اليه اي وقت اردنا ان نعلم ما مصى من ساعات النهار وما يقى فانه لا يحفى عليك ذلك وهذا امر واضح فاعمل في دلك كله من البلدان ان شا الله تعلى وهو المستعان وبه التوفيق وهذه صووته ٥٠٠٠

(1-2) - 3 الأصل - لوح أو حجو -2 م - كلمة غير بينة في الأصل -3 كلمة عير بينة في الأصل -3 الأصل -3 الأصل يالحس -3 الأصل يالحس -3 الأصل الأصل الأصل الأصل الأصل الأحل الأصل الأحل الأصل الأحل الأصل الأحل ا

٣- بابان في معرفة ارتفاع الشمس نصف النهار بقرطبة وسمت القبلة بها من كتاب الأسرار في نتائج الأفكار

المصادر . مكتبة فلورتر لورينتزيانا ١٥٢ ، ق ٤٨ ط

ارتفاع الشمس عند حلولها بروس البروج بقرطة ارتفاعها عند حلولها براس الجدي كو ارتفاعها عند حلولها براس الجدي كو ارتفاعها عند حلولها براس الدلو لج . . . الحوت م . . . الحبوزا عب . . . السرطان عه . . . الاسدع . . . السنبلة صح . . الميزان نا آل . . . الحوزا م . . . القوس آج الحمل نطيره الميزان الميزان الميزان نظيره الحمل الثور نظيره العقرب العقرب نظيره الثور السنبلة نطيرها الحوت الحوت نظيره السنبلة

راب في معرفة سمت القبلة [في مد]ينة قرطبة استوحى طلوع الشمس يوم خمسة عشر او يوم ستة عشر [او يسـو]م سعة عشر من دحنبر فانها في هده الثلثة ايام يكول مطلعها واحد [في] اقصى مطلعه في الجنوب ومن حيت طلعت هو سمت Thus there were several accepted qibla values in Cordova, and even astronomers such as Ibu al-Naṭṭāḥ preferred to invite his readers to choose their favorite one rather than take the trouble to compute one consistent with the mathematical and geographical knowledge of his time.

Appendix B

Arabic Texts

In this appendix I present the Arabic texts of (1) the chapter on the "sundial" by Ibu al-Saffār taken from the K. Natā'ij al-afkār of al-Murādī; (2) the anonymous chapters on the meridian altitude and qibla at Cordova from the same work; (3) the passage on the same "sundial" by Maimonides; (4) an extract from the chapter on the qibla in the treatise on folk astronomy by al-Hasan b. "Alī al-Umawī; (5) the passage on the qibla at Cordova in the treatise on the astrolabe by Ibn al-Saffār; and (6) the chapter on the qibla in the treatise on the astrolabe by Ibn al-Naṭṭāḥ.

١- باب في عمل البلاطة لابن الصفار كما ورد في كتاب الأسرار في نتائج الأفكار لابن محلف المرادي

المصلىر : مخطوطة مكتبة قلوريز لورينتزيانا ١٥٢ ، ق ٤٧ و – ٤٧ ط

باب في عمل بلاطة تعرف بها ساعات النهار على الحقيقة لابن الصفار تاخد حجر كتان او رخامة وتنقش فيه على ما ياتى ذكره في شكله المصوو ويكول الوسط اللدي بين الساعات ثابتا خارجا عن وجه الساعات فيكون الوجه الواحد شرقيا يدل على ساعات انتو لا النهار والثانى عربيا يدل على ساعات اخر لا النهار ثم تقيم لكل واحد مرودا مشتا في شتمع الساعات على اعتدال واستوا يكون طول كل واحد قد عد عد شرويا وتجعل هيمه قياد عقد عقد عقد عن الرض مستويا وتجعل هيمه

التحقيق . ١ – في الاصل : يعرف ٢ – في الاصل - اول (٣-٣) – عير واصح في الاصل

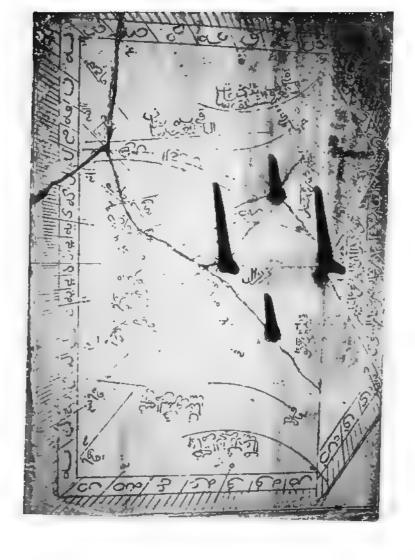


Plate 6: The sundial of the Mosque of Sids Okha in Qayrawan.

(Courtesy René Rohr)

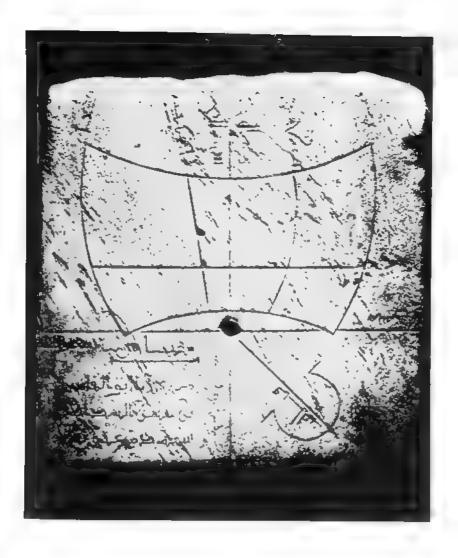


Plate 5 A fourteenth-century Tunisian sundial displaying the times of prayer.

(photo Alain Brieux, courtesty Francis Maddison)

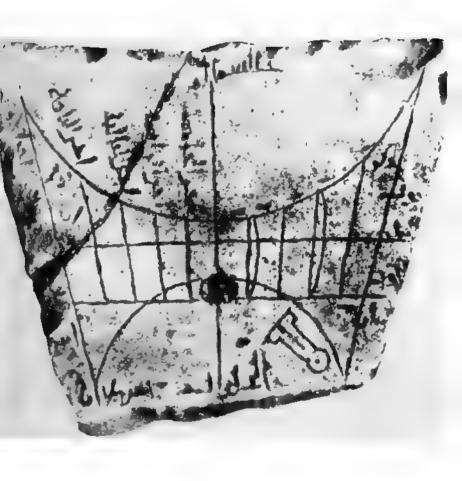


Plate 4: The Granada sundial.

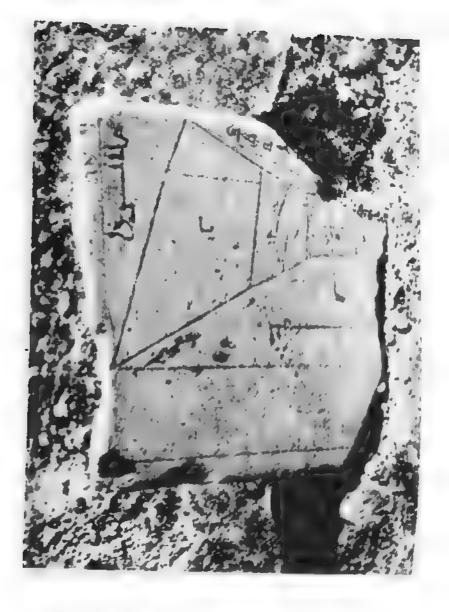


Plate 3: The Almeria sundial.



Plate 2: The sundial of Ahmad b. al-Şaffar
(Courtesy Museo Arqueologico Provincial de Cordoba)

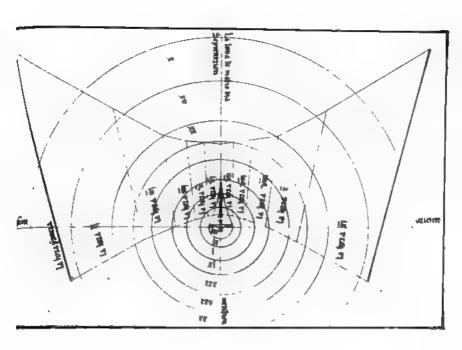


Plate 1 The horizontal sendial illustrated in the Librar del Saber.
(Courtesy Harvard University Library)

In his geographical tables15 al-Battani gives the following coordinates

	L	φ
Cordova	27;00	38;38°(?)
Mecca	71: 0	21;40

With his geometrical construction we derive from these coordinates that the qiblo at Cordova is about 23° S. of E., which is precisely the value attributed to "the astronomers" by Ibn al-Naṭṭāḥ.¹⁴ I have no information on Abu'l-Qāsim al-Snyry who is quoted by Ibn al-Naṭṭāḥ in the same context. The "correct" qibla for these coordinates, derived using the accurate mathematical formula, is 11° S. of E., and this is only 1° off the modern qibla for Cordova, which is 10° S. of E.

Ibn al-Naṭṭāh's remark that the Jāmic mosque in Cordova is at 60° (S. of E.) is incomprehensible to me because, as noted above, the Great Mosque of Cordova has its qibia wall due south. Ibn al-Naṭṭāh's other statement that most of the mosques in Cordova are laid out according to the opinion of al-Battāni, that is, at 23° S. of E., or at 30° S. of E., that is, the direction of the rising sun at the winter solstice, will be, or should be, of interest to historians of Andalusian architecture.

From the Granada sundial we know that south-east was also used as the qibla in Andalusia. The direction 45° S. of E. would have been bandy for the qibla in Andalusia since, as Ibn al-Naṭṭāh says, the legal scholars thought that the whole (south-eastern) quadrant was the qibla. The qibla indicator on the Tunisian sundial also points due south-east, and although this qibla is grossly maccurate for Tunis, it is a happy compromise between due east and due south, both of which directions are attested for qiblas of medieval Maghribi mosques.¹⁷

15. Nollino, 11f, pp. 234-242. The reading of the mirrates in the latitude of Cordova appears to be in error.

16. Other medievel coordinates yield similar but not identical results. For example, al-Marrakushi, in astronomer of Morvecan origin who worked in Carro co. 1280, recorded the following geographical coordinates (Stdillot-pårs, 1, pp. 202-204 and 315-317)

	L	φ
Cordova	27,00	38,300
Mecca	77.0	21:0

Using al Battaui's method I derive a gibts of 21° S of E. Agam, in the Toledan Tables, a hodgepodge of tables called mainly from the Zijes of al-Battion and al-Khwarizmi, and compiled in Toledo in the thirteenth century we find the following coordinates (Toomer, pp. 134-139, nos. 3 and 16):

	J.	φ
Cordoya.	9;200	38:300
Месси	67:0	21:0

These coordinates are derived from those of Prolemy, and were used by al-Khwarismi. I compute that they yield a gible of 20° S. of E. using al-Battani's method.

17, Cf. King 2, p. 190-191

The treatise on the use of the astrolabe by Ihn al-Saffār, published by J. Millas Vallicrosa, contains a remark (Appendix B. extract 5) that the gibla at Cordova is 30° south of east. The treatise on mechanical devices entitled Kitab al-Asrār fi nutā'ij al-afkār by Ibn Khalaf al-Murādī° concludes with a chapter on the qibla at Cordova (Appendix B. extract 2), in which the author states what is equivalent to an assertion that the qibla there is in the direction of the rising sun at the winter solstice. The two directions given in these two sources are in fact the same, and al-Murādī's definition explains the value of Ibn al-Saffār.

The local direction of the rising sun at the winter solstice was also taken as the qibla in early Muslim Egypt. The justification for such qibla determinations appears to result from an early Islamic tradition of using al-Jady, the Pole Star, to find the qibla. As we have seen in the treatise of al-Hasan b. Ali al-Umswi, what was intended was that if one stood with one's back to the Pole Star one would be facing the qibla. Since one would be in fact facing due south, this injunction is valid only for points due north of Mecca. However, when Muslim domination extended eastwards and westwards, another interpretation was given to the injunction, and al-Jady was taken to refer to the sign of Capricorn. At the winter solstice the sun is at the first point of Capricorn; its rising point was used for the qibla in Egypt and Andalusia.

A fourth discussion of the qibla at Cordova occurs in a treatise on the use of the astrolabe by an individual named Ibn al-Na(tāh, 10 extant in the unique copy MS London B.L. 9602,1 (fols. 1v-24v, copied ca. 600H). Ibn al-Na(tāh's treatise was apparently well esteemed in its genre: a note in MS Caro Dār al-Kutub hay'a 10, fol. 39v, copied after 1163H by a Maghribi astronomer, states that the best treatises on the astrolabe are these of Ibn al-Na(tāh and of Ibn al-Samh. 11 Ibn al-Na(tāh's remarks are found on fols.

- 4. Un Ibn al-Saffår see note 9 above.
- 3. Millia, p. 65 of the Arabic text
- 6. See note 22 above.
- 7. For $\phi=38^\circ$ (the latitude of Cordova is actually 37,53°) and $\epsilon=23.35^\circ$, the samuth of the hilogogna at midwaver is 30,31° S. of F. For $\phi=38.30^\circ$, a value popular with Andalusian astronomers, the szimuth would be about 30,45° S. of £.
 - 8. See the article Kible in Elg.
 - 9. See, for example, the treatme on folk astronomy by 1bn Qutayba (fl. 850), p. 122.
- 10. Ibn al-Najtāh and the London manuscript of his treatise on the astrolabe are listed in Suior. No. 499 He is not mentioned in Millös (1), and I have no other information on him.
- 11 On the al-Samb see Seague, V. p. 356 (the treatise on arithmetic contained in manuscripts in the Esconal and to Berlin is not by Ibn al-Samb) and V1, to appear. His treatise on the astrolabe sextant in the unique copy MS Loadon B L. 9602.2 (fols. 25v-55v, copied ca. 600H, defective at end). This treatise of course contains a chapter on the determination of the qubia, but no values are given for anywhere in Andalusia.

comprises four main sets of markings (1) graduations around the edge of the sundial from which the hour-angle can be read using the shadow of a thread attached at the centre of the graduations and oriented in the direction of the celestial pole; (2) markings displaying the seasonal hours since sunrise and before sunset: (3) markings for the zuhr28 and 6asr, the latter being duplicated; and (4) markings displaying time relative to daybreak and nightfall. The first part of the sundial is called al-musitara in late medieval Arabic,28 and the development of this kind of hour-angle dial in medieval Islam remains to be studied. On the second part of the sundial there are no shadow-traces for the equinoxes and solstices, and this feature, not attested on any of the Egyptian. Syriam, or Turkish sundials currently known to me, may be the result of a Maghribi innovation in gnomonics: since it is so difficult to draw acceptable hyperbolae, leave out the shadow-traces altogether.

Appendix A

Some Medieval Values of the Qibla at Cordova

Very few astronomical works compiled by Andalusian astronomers have survived in the manuscript sources, so that there is not much hope of recovering written material on the qibla in Andalusia. Treatises which deal with the determination of the qibla without giving specific examples do not concern us here, and I have found references to the specific values of the qibla in Andalusia in only four Andalusian treatises. Details follow.

The treatise on folk astronomy written by the late twelfth century Cordova scholar Abū 'Alī al-Hasan b. 'Alī b. Khalaf al-Umawī, which is extaut in the unique MS Escorial ar. 941 (38 fols., co. 800H), contains a statement (fol. 26v, see Appendix B. extract 4) that to find the gibla in Andalusia one should stand with the celestial pole behind one's left shoulder and face south. It was probably on this kind of authority that the Great Mosque in Cordova, which dates from ca. 785, was built with its qibla wall facing due south.

^{28.} In Janua, p. 210, the shadow increase at the beginning of the gular is given incorrectly as in rather than 1/2n.

²⁹ Cf. Janin-King, pp. 199-200 and 214.

¹ For a brief introduction to the determination of the qible in medieval Islam see the article Rible in EI₂ by A. J. Weissinck (religious aspects) and myself (mathematical aspects).

^{2.} On al-Umawi see Sarer, no. 323.

^{3.} Creswell 1, 11, pp. 145-146 (repeated in Cressell 2. p. 216) stated ""(The Mosque) is set, as nearly as can be measured, exactly north and south, although the direction of Mekka from Cardava is 10914".

S. of E" A remark such as this reflects the misundecstanding of orientations of medicial Islamio buildings common amongst biotosians of Islamic architecture. Such orientations are usually to be explained in terms of medicial gibbs values, if they can be explained at all.

- 888H. This treatise, arranged in 44 fasts with numerous diagrams but without tables, treats of the construction of horizontal sundials with markings for the hours and the prayer-times. This work merits detailed investigation.
- (3) An anonymous treatise on the construction of a horizontal sundial displaying the seasonal hours for the latitude of Fez. 33;40°, is contained in MS Cairo Taymūr riyāda 141.6, pp. 146-156, copied ca. 1100H. The treatise contains tables displaying the shadow lengths and azimuths at each hour for both solstices, with values to two sexagesimal digits.
- (4) An anonymous Maghribi treatise on the construction of a sundial displaying the times of the suhr, and the beginning and end of the suhr (corresponding to shadow increases of $\frac{1}{2}n$, n, and 2n) is contained in MS Cairo Halim might 19,3+4, fols. 45v-58r, copied 1144H. The author states triplets of both azimuth values and shadow lengths for each of the three times at the solstices and equinoxes. Values are given to the nearest degree or unit, and are stated to be for the latitude of Fez (value not stated). The azimuth values given for the beginning and the end of the suhr are the same.
- (5) An isolated table of coordinates for constructing a horizontal sundial displaying the seasonal hours for the latitude of Marrakesh, 31;30°, is contained in MS Cairo Taymūr riyāda 131,2, p. 1, copied ca. 1200H in Maghribi script.
- (6) A treatise entitled Rawdat al-nāzir fi kayliyat wade khujūt fadl al-dá'ir by Muhammad al-Idrisi is preserved in MS Cairo Där al-Kutub migåt 1169,2, fols. 11v-25v, copied 1223H. This treatise, arranged in 4 habs, deals with the construction of a horizontal sundial with markings for the seasonal and equinoctial hours and the prayer-times, and it contains several tables computed for the latitude of Tunis. 36,510. The author quotes other Maghribi writers named Ibn al-Najiär and Abū 'Abd Allāh Muḥammad Kwynkh (?), author of a treatise on sundial theory entitled lhya' al-mawat fi'l-basa'it wa-lmunharifit, as well as the two well-known Egyptian astronomers Ibn al-Majdi and Sibt al-Märidini.20 The kind of sundial discussed in this treatise apparently became known in the Maghrib from the Muslim East, and its introduction there seems to have occurred rather late, that is, co. 1600. One kind of late Maghribi sundial is illustrated in Plate 6, which shows the sundial of the Mosque of Sidi Okba in Qayrawan in Tunisia, constructed in 1258H (= 1842 A.D.) and recently discussed by L. Janin.27 This kind of sundial is late, and not related to the Andalusian tradition. As Janin has shown, it

^{26.} Suter, nos. 432 and 445.

²⁷ See Janin, especially pp. 208-211

preserved in the unique MS Florence Medicea-Laurenziana Or. 152, fols. 1v-48v, copied 664H (= 1266) in Maghribi script, and the passage occurs on fols. 47r-47v (see Appendix B, extract 1). The same type of sundial is described by another scholar of Cordova, namely, Maimonides. In his commentary on the Mishna Maimonides gave a much more succinct account of the sundial than Ibu al-Şaffar. The text (see Appendix B, extract 3) translates as follows:

A piece of marble (rukhāma) is fixed on the ground and straight lines are drawn (as radii) with the names of the hours written on them (to form) a circle. In the centre of that circle there is a nail standing perpendicular (to the plane of the circle), and whenever the shadow of that nail is in the same direction as one of those lines, it is known how many hours of daylight have passed. The name of this instrument, which is used by the astronomers, is the ballāta.

Ibn al-Şaffăr's text confirms that what is intended is to form a semicircle with the diameter oriented east-west and the circular part towards the north. The twelve hour-lines are the radii at 15° intervals from west to east. There is no suggestion that the dial be oriented in the plane of the celestial equator, when it could indeed be used to display equinoctial hours before or after midday. Rather, the dial is horizontal, and it is assumed that the sun rises due east and sets due west, and that its change in azimuth is proportional to the passage of the seasonal hours.

A far more interesting instrument for timekeeping is described and illustrated by al-Murādī as the last of the thirty-one devices presented in his book (fols. 45r-46v). This is a horizontal dial of the kind known in other medicial Arabic souces as shāmila or musātara, although in al-Murādī's text it is simply labelled "a kind of bullā'a". This dial was as far as we know invented by al-Khujandī in the tenth century, although the one described by al-Murādī may be an Andalusian invention. In any case the Islamic tradition of horizontal dials in general awaits study.**

(2) A treatise by the early fourteenth century Tunisian (?) astronomer Ibn al-Raqqam³⁵ is extant in MS Escorial ar. 918,11, fols. 68v-82v, copied

^{23.} This passage is quoted without comment in Cobanelas, pp 404-495 The original text was in Judaeo-Arabic written in Hebrew characters

^{24.} See Janus-King, p. 199, and the references there cited Al-Khujandi's treatise is currently being studied by Dr. R. Loreb.

²⁵ On Ibn al-Raqqim (was he Tunisian or Andalusian's) see Suter, nos 386 and 417, Renaud, no 388, and King 2, pp. 191 and 192. All of his works ment detailed investigation.

and hence to date the sundial! For the Tunssan sundial I computed $\varphi\approx 37^\circ$, which corresponds quite well to Tunis. For the Cordova sundial I have derived $\varphi\approx 39\,b_2^\circ$, which serves Cordova. But I doubt that one should attempt to compute the latitude underlying sundials as crude as the Almeria or Granada sundials.

Conclusions

Rather than assert on the hasis of our investigations of the only three sundials known from Islamic Spain that the Andalusian astronomers were not competent in gnomomics, we can only conclude that these three surviving specimens are not particularly impressive when viewed in the light of the sundial theory of Abbasid Baghdad. Are there any other sundials from Islamic Spain? A single dial could greatly add to our knowledge of Andalusian sundial construction.

Another source for our knowledge of Andalusian gnomonics would be treatises on the construction and use of sundials, but there are very few known treatises on this subject of Andalusian or even Maghribi provenance. Besides the treatise in the Libros del Saber, I know of only the following:

- (1) A short passage attributed to Ibn al-Şaffār in a twelfth-century Andalusian treatise on mechanical devices by Ibu Khalaf al-Murādī²² describes at length a "sundial" for measuring the hours "correctly". The treatise is
- 21. In de Orún the Almeria anndual is dated to the end of the tenth century or the beginning of the eleventh by the following method. Measuring the eccentricity, s, of the "hyperbola" for the winter solution as 2.00, and taking $\Phi = 36^{\circ}50'$ for the latitude of Almeria, the obliquity of the ecliptic. C, hiderentanced using the relation cos $\Phi = s$ sin C, and found to be 23°34. Newcomb's formula for the secular variation of C is then used to derive an approximate date for the sandant.
- 22. On this treatise see King 3, p. 289. Hill, and Sabro. The chapter by Ibn al-Şuffar (Sabra, p. 280) is followed by a chapter on the determination of the meridian, correctly attributed to al-Bettání (fils. 47v-48c; Sobra, p. 280, states that this is appropriately, and by two anonymous chapters (both as fol. 48v) dealing with the meridian shitudes of the sum in the signs at Cordova and on the qible at Cordova. These two chapters may be due to Ibn al-Şuffar (as suggested in Sabra, pp. 280-281). The solar meridian shitudes are based on latitude 38.30° and obliquity co. 23.30° values are given to the nearest half degree for each godinant sign. On the value stated for the qibla at Cordova see Appendix A.

As Sabra has pointed out (Sabra, p. 278), the author of this treatise is named as . . . (?) Iba Khalaf al-Murădi rather than the eleventh century scholar Iba Murădia as was assumed in Hill However, Sabra read the last and only visible letter of the name preceding the word has a nün (= n), when it is actually a dal (=-d). From Toledo in the mid-eleventh century there were two scientists asmed "Ali b Khalaf and "Abd Aliāh b. Khalaf (Blachère, pp. 138-139) who cannot be the authors. Ahmad b. Khalaf and Muhammad b. Khalaf, both celebrated astrolabists of ninth-century Iraq (Iba al-Nadim, pp. 284-285), are also not candidates. Neither, most probably, are Muhammad b. Khalaf al (uzrubi (d. 557/1162) author of a legal work histed in Brockelmann, I. p. 185, or al-Hasan b. "Ali b. Khalaf al-Umawa al-Qurtubi (d. 602/1205-06), author of a work on folk astronomy listed in Sabra no. 323.

XY measures the length of the gnomon, because it is about the same length as OW.

We now observe that the hour-lines divide equally the two east-west lines; this reveals the method by which they were constructed. But how did the maker construct the first and eleventh hour-lines, AB and CD? Notice that AOD and BOC are more or less straight lines and that they are inclined at approximately 45° to the mendian. Notice also that OA and OC are roughly twice OB and OD. The reason why the maker might have used the approximation $OA \approx 2$ OB is clear from Ibn al-Şaffār's sundial. Notice also that OA and OC are roughly twice the length x, but OA and OC should be about four times the length of the gnomon, so that x cannot represent the length of the gnomon. The directions that the maker chose for AOD and BOC are nice and symmetrical but not so reasonable.

Notice that the winter-solution shadow at the 'ayr, is in excess of the midday shadow OW by the length x. From this one might conclude that the length x was a measure of the length of the guomon, but the relationship is fortuitous. Both the zuhr and 'ayr curves have been drawn as arcs subtended by the seventh and ninth hour lines. If we superimpose the Cordova and Granada sundials we see that the error in the time of the 'ayr displayed by the Granada sundial is about one hour.

In a recent publication I have discussed in some detail the Tunisian sundial mentioned above, ¹⁰ but at the time of writing that paper I was not aware of the existence of the Granada sundial. The Tunisian sundial displays four times of day with religious significance, including the zuhr and the 'air prayers and a morning prayer at the same time before midday as the 'air after midday. Each of the curves for these three times is drawn as an arc of a circle, as are the shadow-traces for the solstices. I have already proposed a method of constructing such a sundial, but I think that I may have placed too much emphasis on the possible use of calculation, or even tables of the kind well attested in the astronomical traditions of Egypt, Syria, and the Yemen, rather than geometrical construction, in the marking of this Tunisian sundial. I also now question the validity of trying to derive the local latitude for which such an approximate sundial was drawn, although it is certainly more valid than attempting to derive the value of the obliquity underlying the markings

^{20.} King 2. In this paper the dimensions of the sundial are given (p. 187) as 24 × 34 cm.; read 24 × 24 cm. Also, the time of the invite shown on the sundial (see p. 190) does indeed relate to the Friday prayers in the unonymous Moroccan treatise of sundials preserved in MS Cairo Hallim might 19 the author mentions the first and second ta akhab on Friday (fol. 47v). Unfortunately be gives no further information.

drawn using a geometric construction of the kind known as analemma,13 or by using tables of coordinates of the intersections of the hour lines with the three shadow traces taken from tables prepared in advance. The only known tables for constructing sundials which predate the time of Ibn al-Saffär are those of al-Khwarizmi, compiled in early ninth century Baghdad, it and displaying the coordinates of the intersections of the hour-lines with the two solstical traces. Al-Khwarizmi gave values of the shadow length, measured from the foot of the gnomon, and the azimuth, measured from the east-west line, for each hour at both solstices and for a series of terrestrial latitudes, including 38° and 40°. In view of the fact that some of the hour-lines on Ibu al-Saffar's sundial consist of two segments drawn between each of the shadowtraces for the solstices . d that for the equinoxes, it follows that if he used tables, then they must have displayed coordinates for the equinoxes, although these are superfluous since the hour-lines are taken as straight lines. To construct the lines using an anolomma one likewise needs only two sets of points. But Ibn al-Saffar used three. Furthermore, the fact that the segments between the shadow traces at the equipoxes and the summer solstice for the third, fourth, fifth, seventh, and eighth hours are more or less parallel to the meridian indicates the seriousness of his error. The curve for the zuhr was probably constructed by joining the three points on the shadow traces which are such that their distance from the gnomon is the meridian shadow increased by the standard one quarter of the length of the gnomon. However, one might think from looking at Ibu al-Şaffār's sundral that the zuhr was at about 143 seasonal hours after midday at the summer solstice and at about 214 seasonal hours after midday at the winter solstice. In fact, the curve for the zuhr should not dross the eighth hour line.14

The remains of Ibn al-Şaffar's sundial do him little credit. One might have expected something better from one of the leading astronomers of Andalusia, when that province of the Islamic world was close to its cultural zenith. Nevertheless Ibn al-Şaffar's sundial is a better specimen than the two that we shall investigate next.

(b) The Almeria Sundial

The second sundial is preserved in the Museo Arqueológico de Almeria, and is displayed in Plate 3. It has been described by Juan J. de Orús (1956) and Dario Cabanelas (1958). A substantial part of the western half of the sundial is missing, and the maximum dimensions of the remaining portion of the marble slab are 28 × 29 cm.

^{13.} On the analemms see Neugobauer, pp. 214-218 and the references there cited

^{14.} See note 5 above.

IS. Cf. King 2, p. 191.

^{16.} Cf de Orus, and Cabanelas, pp 392-394. See also note 18 below.

meridian.11 This hole has been violated by the gnomon to such an extent that its centre is no longer on the mendian. A segment perpendicular to the right edge of the sundial when extended passes through this hole and represents the east-west direction. The three lines which are drawn across the meridian are: closest to the hole, the hyperbola representing the shadow trace at the summer solstice (when shadows are shortest), next, a straight line representing the shadow trace at the equinoxes, and, furthest from the hole, the shadow trace at the winter solstice (when shadows are longest). The lines drawn across these three lines indicate the seasonal hours of day, starting at the first on the right, then the second, third, fourth, and fifth, then the sixth, which is precisely midday because we are dealing with seasonal hours that are one-twelfth divisions of daylight, and then the seventh and eighth. The hour-lines are marked akhir al-ūlā, "end of the first (hour)", akhir althaniya, "end of the second (hour)", etc. The curve close to the left hand edge of the sundial indicates the time for the guhr prayer. We may presume that the sundial originally hore a curve for the beginning of the fast prayer se well.

We now investigate the markings more closely, firstly to establish the underlying latitude, and secondly to ascertain the accuracy of the markings. All of the measurements are based on the photograph illustrated in Plate 2. The length of the gnomon is $n=9\frac{1}{2}$ mm., and the midday shadow at the winter solstice OW is $18\frac{1}{2}$ mm. Thus

$$9\frac{1}{2} \cot (\bar{\varphi} - *) = 18\frac{1}{2}$$

so that

cot
$$(\bar{\phi} - \epsilon) = 1;57$$
, $\bar{\phi} - \epsilon \approx 27^{\circ}$ and $\bar{\phi} + \epsilon \approx 63^{\circ}$

But * = 23:30°, so that

$$\varphi = 39;30^{\circ},$$

which is close to the standard medieval Islamic value for the latitude of Cordova 38;30°. ¹¹ The accurate value for Cordova is 37;53°.

A glance at the sundial reveals several defects. Firstly, the equinoctial shadow trace is not a straight line, as it should be. Secondly, the lines for the third and fourth and eighth hours are not straight, as, in a sundial of this size, they should be. These defects are so obvious to anyone with the most modest knowledge of guomonics, that we may well wonder why Ibn al-Saffar put his name to the sundial. We cannot be sure whether the markings were

II Cf. Cabanelus, p. 396, where it is suggested that the circle serves no purpose other than decoration.

This is easily confirmed by consultation of the computer print-out of medieval Islamic geographical coordinates described in Kennedy-Haddad.

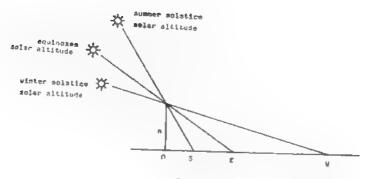


Fig. 1

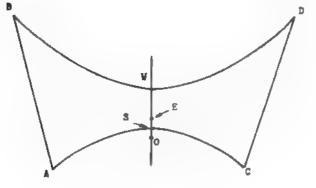


Fig. 2

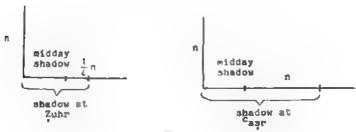


Fig. 3

in Andalusian practice are that the gnomen shadow shall have increased beyond its midday minimum by 1/4 n and n, respectively (see Fig. 3).7

(a) The Cordova Sundial

In the Museo Arqueológico Provincial in Cordova there is a fragment of a horizontal sundial, illustrated in Plate 2, which was found in the Camino Viejo de Almodovar in Cordova. It has been published by Samuel de los Santos Jener (1955) and Danio Cabanelas (1958). The instrument bears the name of Ahmad ibn al-Saffār, an astronomer of some renown who worked in Cordova about the year 1000 A.D., and is thus the oldest surviving Islamic sundial, although it has not been previously identified as such.

The remains of the Cordova sundial consist of a little more than half of the original instrument. The dimensions of the original sundial were 48 cm. (approx.) × 34.5 cm. × 4.5 cm. The inscriptions are in elegant floriated Kufic, and the maker's name appears in the upper right corner. The cardinal directions are marked on the sundial, which is broken just to the left of the meridian or north-south line. The hole on this line once carried a vertical gnomon, the length of which is indicated by the radius of the circle to the right of the

- 7. On the times of prayer in Islam see Wiedemann-Frank, A. J. Wenninck's article 'tik' in El' 1, and King 4. For an explanation of the definitions in terms of the increase of the shadow see King 2, Appendix B. A more detailed study on the origin of the definitions of the times of prayer in Islam is in preparation.
 - 8. Cf. de los Santes and Cabanelas, pp. 394-396. See also notes 10 and 11 below
- 9 On the al-Saffar see Blackers, p. 131, and the orticle by B. R. Goldstein in El₂, 111, p. 924, and the references there cited, to which add now Seagin, V, pp. 356-357, and V1, to appear. Ahmad the al-Saffar had a brother Muhammad who was a maker of astrolabes (cf. Maser, p. 75, for details of an instrument made by him in the year 1029).

Ibn al-Saffar was a student of the Andalussan astronomer and mathematician Maslama al-Majriff, author of a recession for Andalussa of the a.j (astronomical handbook consisting of text and tables) of the unith contary Baghdad astronomer al-Khwāriami (oo whom see G. Toomer's article in DSB). Ibn al-Saffar also compiled a zij based on the methods of the Indian Zij ni-Sindhind (Kennedy, no. 17). Only the introduction to Ibn al-Saffar's zij survives, namely, in an Arabic manuscript written in Hebrew characters preserved in the Bibliothèque Nationale in Paris (the tables in this manuscript are not related to Ibn al-Saffar). His only other known work is a treatise on the use of the introlabe, which was popular amongst later Mushim astronomers and is extant in several copies (the Arabic text of this treatise was published by J. Millas Vallicrosa in 1955), and was also translated into Latin and Hebrew. In his later years Ibn al-Saffar moved from Cordova to Denia, where he died in the year 1935.

10. In do los Santos the name is read Ahmad b. al-Tulb, and in Cabanelas. p. 396 as Ahmad b. al-Sawwär I agree that the reading sourcer is easier to justify than suffer (the dot over the middle radical is a scratch), but firstly "sawwär" is not attested as a name meaning " diseñador, delineante, pinter", and secondly Ahmad b. al-Saffar was a well-known astronomer of Cordova

The three sundials are preserved now in three different museums in Spain, and I shall henceforth designate each of the sundials by its present location, namely, Cordova, Almeria, and Granada. All of the sundials are of the horizontal kind designed for a specific latitude and displaying the seasonal hours of day. Such sundials were used already in antiquity, and are described in the earliest Arabic treatises on sundials. They are also described in the thirteenth century Andalusian Libras del Saber (see Plate 1).

Two of the Andalusian sundials are broken, but each of them displays all or parts of three main sets of markings. These are (a) the north-south line and shadow-traces for the solstices and equinoxes; (b) the hour lines for each seasonal hour of daylight from the end of the first hour to the end of the eleventh hour; and (c) the curves for the midday (zuhr) and afternoon (*asr) prayers. Each sundial was originally fitted with a gnomon creeted vertically in a hole in the sundial; in all cases, these gnomons are now missing.

I shall use the following notation freely. The points at which the shadow-traces for the summer solstice, equinoxes, and winter solstice, intersect the north-south line (see Fig. 1) are labelled S. E., and W. The base of the gnomon is O, and its length is n. The most commonly used length of the gnomon in Islamic sundial theory was 12 units. Clearly, for a locality with latitude φ (see Fig. 2):

 $OS = n \cot (\tilde{\varphi} + \epsilon)$; $OE = n \cot \tilde{\varphi}$; and $OW - n \cot (\hat{\varphi} - \epsilon)$, where ϵ is the obliquity of the ecliptic and $\tilde{\varphi} = 90^{\circ} - \varphi$. For Andalusia $\varphi = 38^{\circ}$ and approximately $OW.OS = 7\frac{1}{2}$:1. Also, E is roughly at the point of trisection of SW closer to S, so that approximately SE EW = 1:2. The lines for the first and eleventh hours between the summer shadow-trace and the winter shadow-trace are labelled AB and CD.

The standard definitions of the times for the guhr and carr prayers

^{4.} See Gibbs, pp. 39-42 and 323-338

^{5.} See Seagin, VI, pussim. An important aspect of these treatises is the tables of coordinates for marking sundials which some of them contain. I am currently preparing an edition of al-Khwārizmī's madial tables, and a survey of all later Islamic sandial tables. For a brief introduction see King I, pp. 51-53 and 56.

^{6.} Libros del Saber, IV, pp. 1-23. No author is associated with this treatise, which was written especially for Alfouso X because no book on the subject could be found which was "complete in itself" (Proter, p. 18). It is in two parts arranged in 14 and 4 chapters, and deals with the construction and use of a horizontal sundal marked for the sessonal hours (see also Cabanelas, pp. 400-403). The treatise contains tables of the solar declination, and the sine and cottangent functions, but no tables or geometrical procedures for constructing the kind of rundial described in the text. The latter is distinguished from the three Andalusian sundials described in this paper by the inclusion of circles drawn about the gnomou corresponding to the shadows of each 5° of solar skithude, and by the fact that there are no curves for the prayer-times, since these would no longer be of concern to a Christian reader.

Three Sundials from Islamic Andalusia

DAVID A. KING*

In memory of my friend Louis Janin.

In this paper I propose to discuss three sundials from medieval Andalusia. Each of these sundials has been published previously, in the sense that photographs and a list of the Arabic inscriptions have been published, but in the present study I shall attempt to investigate the markings on the sundials beyond a mere description thereof. These markings cannot be fully explained in terms of our present knowledge of Islamic gnomonics, but I anticipate that the publication of the repertory of Islamic astronomical instruments currently being prepared by A. Brieux and F. Maddison, which will include all known Islamic sundials, will serve to revive some interest in a subject which has hardly progressed for several decades. Hence it seems worthwhile to present these sundials answ and to point out the various problems associated with each one.

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The Cordova sundial was brought to my attention by my friend Dr. Lies Golombek of the Royal Ontario Museum and the University of Toronto. A photograph of the sundial, together with information on its size and provesance, was hoodly provided by Srs. And Maria Vicent Zaragosa, Director of the Museo Arqueológwo Provincial in Cordova. The fact that the sundial had been published and the existence of the Almeria and Granada sundish came to my attention during an abusal vinit to the Sterling Library at Yale University in the spring of 1978. A photograph of the Tinisian sandial from the archives of Mr. Francis Maddison, Curator of the Museum of History of Science, Oxford, was kindly provided by M. Alain Bricux of Paris. A photograph of the Quyrawan sundial was kindly provided by Capt. René Rohr of Strasbourg. Prof. Owen Grigerich of Harvard University kindly obtained for me a microfilm of the Librar del Saber from Harvard University Library. Finally, it is a pleasure to record my gratitude to those libraries which have supplied me with microfilms of managingta in their collections, including the Egyptian National Library in Cairo, the Biblioteca de El Escorial, the Biblioteca Medices-Laurennians in Florence, and the British Library in London

- 2. Each of the publications (de los Santes on the Cordova dial. de Oris on the Almena dial; and Cobanelas on all three Andalusian duals) contains errors of interpretation, and none of them points out any of the defects of the deals. However, Cabanelas provided useful physical descriptions of each of the dials and put them in the context of earlier Greek sundials and the treatise on sandials in the Libros del Saber.
 - 3 Until now the only general repertory of Islamic sandlals has been Mayer.

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K. Schoy, Gnomonik der Araber, in Die Geschichte der Zeitmessung und der Uhrm. E. von Basiermann Jordan, ed., Baud IF. (Berlin-Leipzig, Vereitrigung Wissen-

Sédillot-file: L. A Sédillot, "Mémoire sur les Instruments Astronomiques des Arabes", Mémoires de l'Academie Royale des Inscriptions et Bolles-lettres de l'Institut de France, 1 (1844), 1-229.

Table 3
Coordonnées des positions respectives sur le cadran Ibn Țülün (Ombre en mms., azinuts au degré le plus proche)

	4.4	nut	Z	Z	Z	Z	Z,	Z	2 2
	Côté droit	Azimut	2.2 2.2 0	40	48	29	73	90	45 ½ N 44 ½ N
'hiver	Côt	0mbre	272	130	\$6	73	62	57	102
Solstice d'hiver	Côté gauche	Azimut	33° N		N 64	N 09	74 N	N 06	°aبr (original) °aبr (corrigé)
t	Côté	Ombre	275		93	73	62	28	2 0
J===:		nut .	- ·	UD.	S/S	7	-	7	
	Côté droit	Agimut	39°S	11.5	4	2 N	N 61	N 06	\$
Solstice d'été	3	Ombre	187	83	20	128	13	10	50%
Solstion	Côté gauche	Azinat	18° S	30 8	\$5 \$4	Z .		N 06	
	Côté	Ombre	185	60	20	738		ιn	
	Heures	1	-	64	m)	4	vs.	9	^c asr

Equinoxes: Ombre de midi 26, ombre de l''an 71 $^{1}{}_{2},$ azimut de l''an 21 $^{1}{}_{2}$

Table 2

Tables d'al-Magsi pour un cadran horizontal à la lantude 30º (MS Istanbul Nurosmannye 2943, fol. 13v)

Equinoxes: Ombre de mid 6;56[0], ombre de 11-a;r 18;56[0], azimut de 11-ca;r 21;28º [0]

Le MS Vanosmaniye porte 55 mais le MS Le Caire Dar al-Kutub miçát 955, fol. 9v, porte 15. Narosmaniye: 18, Le Caire: 15, exact: 57.

Tables d'al-Marrakushi ponr un cadran horizontal à la latitude 30º

(MS Paris B. N. ar. 2507, fols. 123v and 137r)

	ore.	. 7	9	[0]	[+1]		. 5	<u> </u>	
	Ombre	72,53 [-4]	37;10	25,21	19;48	17,5	16;16	28;16	
d'hiver	Azımut	[0] 34;14°[-2 N]	[-1] 42;14 [+1 N]	51;40 [-1 N]	[+1] 62;55 [0 N]	[+1] 75;53 [-1N]	2 2	[0 N]	_
Solstice	Az	34:14	42;14	51;40	62,55	75;53	90;0	48;20	
	teur	<u> </u>	[-]	[0]	[+ 1]	[+ 1]	9	[0]	-
	Hauteur	9:210	17;53	25;20	[0]; 31;15	12	[0] - 36;25	23,0	
1	Ombre	(-1] 9.21°	[+1], 17,53	` _ _	[0]	[+1] ; 35;5	[0]	[0]	
	0 1	48:40	[0] S, 22;15	[0] S 12;45	7;24	3;38	1;21	13;21	
d'été	Azimut	[0] 19;28° [-1] S. 48;40	S[0]	S [0]	3;16 [+3] N	18;12 [5] N	[0] N	[0] 8	
Solstice d'eté	Azi	19,280	12;19	5;13		18;12	0:06	5;52	
	Hauteur		28;21 [-1] 12;19	43;15 [- 1]	58;22 [+ 1]	73; 8 [4]	9	41;58 [+ 1]	
	Hau	13;510	28:21	43;15	585	73; 8	83,35	41;58	
1	Heures	-	F1	ra	4	l/3	9	asr	

Equinoxes: Ombre de midi 6,56 [0], ombre de l'ajr 18,17 [devrait être 18,56i],

azimat de l'agr 21;14º [- 14] S

un dessin (voir Pl. 5). Ce cadran comporte un demi-cadran à droite qui montre le temps écoulé depuis le lever du soleil (et du même coup le temps qui reste à courir jusqu'à midi et à la prière qui y est associée, le zuhr). Les courbes des heures sont dessinées pour chaque dix degrés équinoxiaux et les valeurs sont indiquées sur la courbe du Cancer comme suit: 20°, 30°, . . ., 100° (le maximum pour la latitude 30° est environ 104½°). Le demi-cadran à gauche montre les degrés qui restent jusqu'à l'éast comme suit: 50°, 40°, 30°, 20°, 10°, puis la courbe de l'éast même, puis les degrés qui restent jusqu'au coucher du soleil (et à la prière du maghrib) comme suit: 50°, 40°, 30°, 20°. Voici donc un cadran hien utile pour la mosquée, qui sert à montrer le temps qui reste à courir jusqu'aux temps des trois prières: zuhr. °ast, et maghrib.

APPENDICE

Additions et Corrections à Janin & King

- 1. Nous avans amis de souligner le fait, d'aillours évident, que lorsqu'ibn al-Shâţir explique qu'il regarde l'extréinité de la boussole par le trou dans le couvercle de la boite, il ignore la déclinaison magnétique. Un aircle plus tard, aiust que pous l'avons remarqué, al-Wafá'l suggessit une correction de 7º pour en tenir compte.
- 2. Nous préparions notre description et usage du cadran polaire universel dans l'instrument d'Ibn al-Shâțir, forsque nous avons eu connaissance d'une illustration et d'une description dans Michel et Ren Eli, d'un cadran polaire pour une latitude déterminée construit à Acce en 1786-87. Nous reproduisons l'illustration dans la Pl. 6. Notez qu'il n'y _ pas de courbe pour l'agr, on surait pu en dessiner une pour la latitude locale, mais elle n'aurait pas pu servir pour d'autres latitudes. Il n'est pas exact de dire, avec Michel, que le cadran d'Acre etait surtout destiné à régulaisser les beures de prières. Nous ne connaissons pas d'autre cadran polisire dans le monde de l'Islam.
- 3. L'autre instrument décrit par al-Wafà'i, appelé al-muquamer et mentionne p 217 note 11, est en fait que armille équatorisle comme le dâ'irat al-mu'addul mais les différentes parties se replient et peuvent ette conservées dans le boite ronde avec convercle qui forme le base de l'instrument. Il résulte du trinté d'al-Wafà'i sur cet instrument que c'était une production antérieure à celle du dâ'irat al-mu'addul il ne vientionne pas par exemple, la déclinaison magnétique, se contentant de dire que l'aiguille de la boussole a sa direction "près du méridieu". Dans un article précédent nous avons comparé le Sandüg al-yawāgit d'Ibn al-Shāṭur avec le dâ'irat al-mu'addul d'al-Wafà'i a'-muqawwar d'al-Wafà'i constitue un échelon intermédiaire de développement et confirme notre impression qu'al-Wafà'i a'-était mapuré du Sandüg al-yawāqit d'Ibn al-Shāṭur
 - 4. A la p. 213 linex samkarahu un lieu de mubkiruhu.

que Marcel avait à sa disposition. les renseignements qui découlent de ces mesures sont assez surprenants.

En général les dessins du cadran que nous avons examinés semblent être assez exactement disposés, mais deux exceptions sont la courbe de l'east et le tracé du solstice d'hiver. La branche gauche inférieure de la courbe de l'east a été visiblement ajoutée plus tard pour essayer de rectifier la courbe originale de l'east. De plus, l'erreur de la courbe originale de l'east près du tracé du solstice d'hiver apparaît bien provenir d'une erreur dans la position de l'intersection du dit tracé avec le méridien. Si nous ajoutons la longueur du gnomon à la distance sur le méridien entre le pied du gnomou et le tracé du solstice d'hiver, nous obtenons la distance entre le pied du gnomon et l'intersection de la courbe originale de l'east avec le tracé. Celui qui a dessiné la courbe corrigée de l'éast s'est arrangé pour que l'ombre de l'éast au solstice d'hiver ait une longueur correcte, mais l'erreur dans le tracé du solstice d'hiver sur le cadran entre la neuvième heure et la onzième, resultant probablement d'une erreur dans la position de la marque de la dixième heure au solstice, rendait impossible d'obtenir en même temps l'azimut correct pour l'east. Etant donné que la fonction la plus importante d'un cadran de mosquée est l'indication du temps des prières, on ne peut pas dire que le constructeur de ce cadran ait remporté un plein succès! Peut-être, d'ailleurs, avous nous mis le doigt sur la raison de la destruction de ce cadran, brisé en plusieurs morceaux.

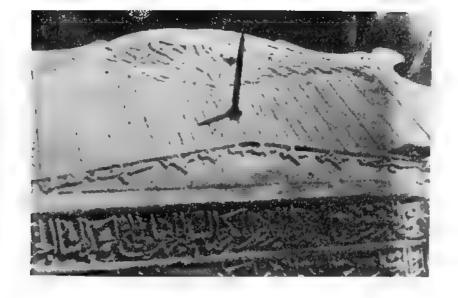
Enfin, nous remarquons que le seul autre exemple d'un cadran fait de deux demi-cadrans superposés que nous connaissions se trouve dans un traité sur la gnomonique par le muicaggit égyptien Ibn al-Muballabi, écrit au Caire en 829 H. = 1425—26 J. C.º Ce traité existe dans un beau manuscrit unique conservé à la Bibliothèque de Chester Beatty à Dublin, numeroté 3641 et copié à Alexandrie en 858 H = 1455 J. C. Ibn al-Muballabi commence son traité par un éloge d'al-Maysi, en ajoutant que le lecteur qui vent en savoir plus que ce qu'il va exposer dans son traité doit se tourner vers le compendium d'al-Marrakushi. Puis Ibn al-Muballabi presente de nouvelles tables (voir Pl. 4) et de nouveaux dessins pour construire les cadrans horizontaux, verticaux, et inclinés, tous calculés pour la latitude du Caire, 30º. Parmi tes textes on trouve des tables pour tracer un cadran à deux moitiés avec

6. Si a est la distance requise en mms, nons avons, du fait que la distance méridienne entre les traces des deux solstices est 52 mms, et que les ombres solsticiales sont 1;21 et 16:16 unites, que

$$\frac{n+52}{n} = \frac{16;16}{1;21} \approx 12 \quad ,$$

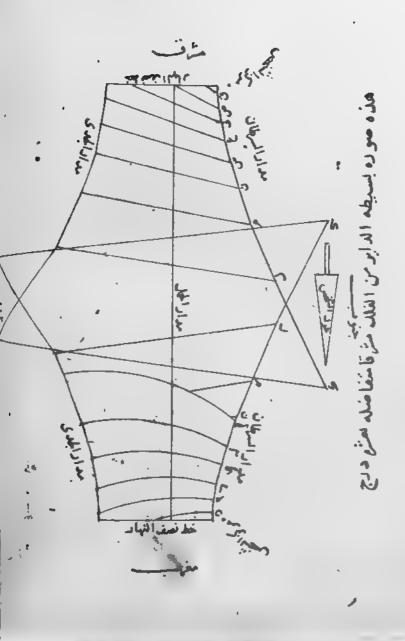
d'oà

7. Ibn al-Muhallabī n'est mentionné dans aucun travail moderne sur la science islamique et on se loi opposit queun aptre ouvrage secentifique.



Pl. 6: Le cadran polaire d'Acre.

(photo Abumux)



Pl. 5 Extrait du manuscrit Chester Beatty no. 3641 (fol. 11v), qui montre le cadran à deux moitirs d'Ibn al-Muhallabi, qui sert à indiquer le temps qui reste jusqu'aux trois prières du ¿uhr, cast, et maghrib.

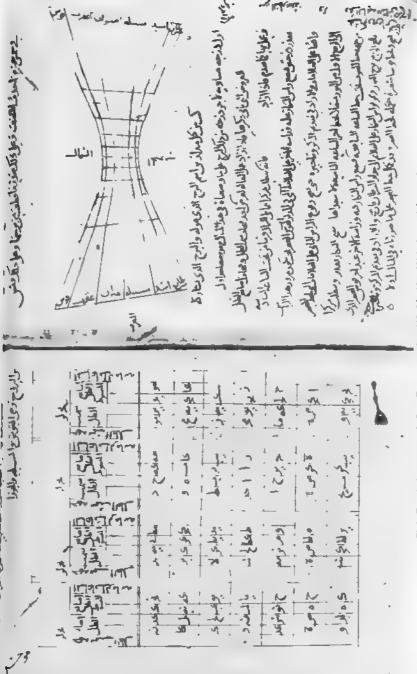
41142			17 17 19	100 mm (100 mm) (100		2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	
					F. C. 3		1.,	
4. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	2 4 1 V 0 Fr	4 5 4	1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	16 16 16 16 16 16 16 16 16 16 16 16 16 1	1 4 3 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	علائد و دانسداند درناسدا در مراز دراسد و در مراسدا در دراز در دراز المداعد	
ا الحراد ا العالم	1 3 3 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1 2 3	4 4	75 T Page 1 7 5 5 1 1 2 5 1 1 1 2 5 1 1 1 1 1 1 1 1 1	44 CL 0 68 63 CC	200	1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	

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بطه الداير من المندورة

Pl 4 Extrait du manuscrit Dubhn Chester Beatty no. 2641 (fols. 10. et 111), qui montre les tables avec lesquelles on pourrant dessuaer le cadran illustré en Pl. 5. A droste on vost les tables qui dannent la hauteur du soleil, son azimuth, et la longueur de l'ombre d'un style de 12 unites, le tout calculé pour chaque 5º de temps ecoulé jusqu'an milieu du jour pour les deux solstices. A ganche on voit les trois mêmes quantités calculees pour chaque 5º avant l''ajr pour les deux solstices et les equinoxes.



meuite al-Asbraf, qui montre le dessin d'un cadran aux heures tempiraires pour la latitude de Taix Pl 3 Extrait du manuscrit le Caire Taymûr riyâdiyêt 195 (fols 137v-138s), du traité du roi yé-(13.37°), et les tables qui servent a le tracer. On remarque que le pied du gnomon se trouve entre la

counts do collected distants determined to an one is counts of $1^{16}av$ montre on discontinuity

زاديودحه بنصفير واخرع اكط الفاحمها حي ملع خط زكي غيث لفيد فهوسوكذ النخد الأطول المطلوب وبافرالول على انقلم الاان مداد الحمل بريمهنا ماز بوخفال عالدوموفي عذا لمتال وتوكا لركان السطره وموضع احوالمرفيه فيعركز التخدرويع إطرفه للاعم فحطاهر مايلالمال لإزالع ضللفروض المعلامه تم يخرج سنعاده العلامه خطابوارى مد 0 1 6 me to en e fine できゅうとりし 一二世 وينتى حات الجهنز المعاخر العائلاوله والمحداول الباد إلةائيه عشروا بدالمؤنق B 81 NAT 7246 Amabe 2567 tol,137

Pl. 2: Extrait du manuscrit Paris B.N. ar. 2507 (fol. 137r) du traité de Abū 'Ali sl-Marrākushı, qui montre le dessin d'un cadran aux heures temporaires pour la latitude du Caire, et les tables qui sotvent à le tracer.



INSCRIPTION ET CAORAN ROLFIQI ES DE LA MOSQUÉE DE TULLOUS

Pl. 1. Le cadran solaire de la Mosquée d'Ibn Tülûn, reproduit par M. Marcel, et meré comme illustration dans la Description de l'Egypte.

référer à Ibn al-Shatir ni à aucun autre astronome syrien.

Examiuons maintenant les tables d'al-Marrākushī (Pl. 2) et d'al-Maqsi pour un cadran borizontal donnant les heures temporaires pour la latitude du Caire, retenue pour 30;0° avec une obliquité de 23;35°. Ces deux tables sont reproduites dans les Tableaux 1 et 2¹ et il apparaît probable qu'elles ont été calculées indépendamment. Les valeurs ont été recalculées avec le calculateur électromique de l'Université Américaine du Caire,² et pour chaque valeur des tables d'origine l'erreur dans le deuxième chiffre sexagésimal, c'est-à-dire dans les minutes, est donnée entre crochets, calculée selon la convention:

Les deux tables sont assez exactement calculées, bien que chacune comporte quelques erreurs qui auraient dû surprendre leurs calculateurs. Néaumoins les erreurs dans les coordonnées de l'éast chez al-Marrakush pour les équino-xes sont bien moins graves que celles qui ont produit la branche inférieure droite de la courbe de l'éast aur notre cadran.

Le Tableau 3 montre les coordonnées correspondant aux positions solsticiales et équinoxiales du cadran d'Ibn Tülün, basées sur les mesures prises sur la planche de la Description de l'Egypte. Pour obtenir ces coordonnées on a d'abord calculé que les pieds des deux gnomons étaient à une distance d'environ 5 mms. au nord de l'intersection des meridiens et du tracé du solstice d'été. Si l'on tient compte du caractère fragmentaire du cadran

4. La table d'al-Marrakushi se trouve déjà dans Sédillos-père, II, pp. 456 and 491.

S. Le processus trigonométrique pour le calcul de ces tables est le suivant. Nons posons le latitude locale φ. l'obliquité ε, le longitude du soleil λ. Nous calculous la déclination δ solsire par la formule

et l'équation du jour d par la formule

Enruite la longueur d'une heure de jour temporaire s se dédujt de la demi-longueur du jour D par la formule

$$t = \frac{D}{6} = \frac{90^\circ + d}{6}$$

La hauteur du soleil à correspondant à une angle horaire égal à un multiple a de cette heure temporoire est alors fourtie par la formule

et la longueur de l'ombre correspondante a pour un guomon de longueur 12 tet alors

Pour trouver l'azimut a nous utilisons la formule

$$am a = \frac{\sin h \sin \phi - \sin h}{\cos h \cos \phi}$$

Les procèdés mediévaux étaient mathématiquement equivalents aux procédés ci-desus. Ils étaient déjà connus des astronomes musulmans au début du neuvième siècle, venant de sources indiannes où ils etment déduit des projections orthogonales de la aphère celeste. Etant donné que ces déductions n'exigent aucune connaissance de trigonométrie sphérique, il est regrettable que bien des auteurs indicense persent que les anciens autronomes musulmans qui ont utilisé ces formules devaient nécessairement connoître la formule du cosinus de la trigonométrie aphétique (voir, par exemple, tont récemment, Sazyin, V, pp. 35 et 261).

Moyen Age aussi comme la latitude du milieu de 4º chmat.

On ne peut pas encore tracer le dévelopement des tables islamiques depuis l'époque Abhasside jusqu'à l'époque d'al-Marrăkushī, d'al-Magsī et du cadran Ibn Tūlūn, mais les matériaux ne manquent pas pour les recherches futures. Il existe enfin des douzaines de manuscrits arabes et turcs dont la plupart sont de provenance égyptienne, syrienne et turque, qui traitent de la gnomonique et présentent des tables, mais qui n'ont encore jamais été etudiés. (Curieusement on ne trouve presque rien en langue persane.) Toutes les tables qu'on trouve dans ces traités sur la gnomonique représentent une tradition islamique consistant à préparer des tables presque pour le seul plaisir de préparer des tables! Il est dejà évident dans leurs compilations sur d'autres chapitres de l'astronomic que les astronomes musulmans avaient une véritable passion pour le calcul des tables."

IV. Analyse des dessins du cadran d'Ibn Tülün

Ni les tables d'al-Marrakushi, ni celles d'al-Magsi ne donnent les coordonnées pour chaque signe du zodiaque, telles qu'elles auraient été nécessaires pour construire le cadran d'Ibn Tülün. De plus nous n'avons pas d'autres tables égyptiennes de cadrans solaires remontant au treizième siècle ou aux nècles précédents. En fait les soules tables connues de cadrans solaires islamiques remontant au treizième siècle et qui donnent les coordonnées pour chaque signe, sont celles qui ont été établies pour differentes latitudes dans le Yémen et le Hedjaz par le Sultan du Yémen al-Ashraf, dans son traité sur l'astrolabe, le cadran horizontal et la boussole magnétique, écrit aux environs de 1295.1 Le Sultan al-Asbraf connaissait l'ouvrage d'al-Marrakushi écrit à peine quinzo ans plus tôt. Un extrait de ses tables de cadrans, montrant des tables calculées expressément pour la latitude de Taiz retenue pour 13:37°, est reproduit dans Pl. 3. On ne connaît pas de tables pour cadrans aussi detaillées depuis le quatorzième siècle, hien que le cadran d'Ibn al-Shaur construit pour la Mosquée Umayyade de Damas porte le tracé des ombres pour chaque signe du zodiaque," et qu'Ibn al-Shaiir ait très probablement construit son cadran en utilisant des tables qu'il avait preparées à l'avance. L'astronome syrieu du quinziène siècle al-Tizini a dressé un jeu detaillé de tables de cadrans et presenté son travail comme une extension du traité d'al-Magsi, sans se

^{7.} Voir Nellino, 11, pp. 188 et 295-296.

Une exception est le traité (avec tables) de Sibt al-Măridini (Suter, no 445) qui a été étudie dans Schoy 2.

Voir Kennedy sur les manuels astronomiques appeles zijes et King 3, spécialement op. 51-53 et 56, où l'on traita des tables pour construire les cadrans solaires.

¹ Sur le Sultan al-Ashraf voir Suter, no. 394 Son traité ne trouve dans le MS Le Caire Taymür rivida 105 (149 fols., co. 595H) et il paraît qu'il y en a une autre copie à Téhéran Une table qui donne la hauteur l'anmuth du solieil pour chaque heure lemporaire et chaque signe du solieique, calculée pour la latitude du Caire. se trouve dans la traite sur les cadrane du célebre libs al-Haytham (fl. le Caire, c. 1025 J. C.), dont nous avons examusé le MS Teheran Majhan-Shūra 39341.1 (11 fols., co 1000H). Dans ce manuscrit dus les chiffres manquent dans la table, et nous n'avons pas eu l'occasion de consulter d'autres manuscrits de cette oeuvre.

^{2.} Cf l'illustration dans l'étude citée dans la note 3 de la Section 1

^{3.} Sur al Tizini von Suter, no. 450. Set tables se trouvent dans le MS Vaticau Borg. 105,3 (fols. 20r-38v. en. 900H), texte apparenment unique.

française par J.-J. Sédillot,³ toute la théorie mathématique et en outre des tables pour construire les cadrans horizontaux, verticaux, et inclinés à la fois sur le méridien et sur le premier vertical. Al-Marrakushi donne aussi des tables pour construire ces cadrans à la latitude du Caire, 30°, où il travaillait quelques années avant la construction du cadran Ibn Tūlūn, car il a daté son traité de 1280 J. C.² Voir en Pl. 2 ses tables et son dessin pour un cadran horizontal préparé pour cette latitude.

Il y a un autre tranté égyptien sur les cadrans qui date de la même époque que celui d'al-Marrākushī et qui n'avait jamais été étudié jusqu'à il y a quelques années. Ce nouveau traité qui a été préparé par l'astronome égyptien al-Maqsī en 1277 J. C., soit un peu avant le traité d'al-Marrākushī, contient plus de cent tables pour construire les cadrans à la latitude du Caire, 30°.4 Ce qui rend les tables d'al-Maqsī plus complètes que celles d'al-Marrākushī, c'est qu'il calcule une table pour les cadrans verticaux inclinés sur le méridien pour chaque degré de l'inclinaison. Où est-ce qu'on doit chercher l'origine de ces tables Islamiques pour les cadrans?

Il a été découvert en 1974 un traité sur les cadrans attribué à al-Khwārizmî (fl. Baghdad, ca. 830 J. C.).4 Ce traité existe dans un manuscrit précieux à Istanbul; il consiste en une courte introduction et en plusieurs tables qui donnent pour douze latitudes différentes entre 0° et 40° la hauteur du soleil, son azimut et la longueur de l'ombre d'un style de 12 unités pour chaque heure temporaire. Il ya des tables additionelles pour les latitudes de Samarra et Baghdad, et la valeur de l'obliquité employée est 23:510 (employée par al-Khwarizmi dans ses tables astronomiques). En 1976 quelques unes de ces tables ont été trouvées ajoutées au traité sur les astrolabes extraordinaires d'al-Sijzi (fl. Iran, ca. 950 J. C.), conservé dans un autre manuscrit précieux à Istanbul. D'autres tables de cette sorte existent dans les sources manuscrites. Dans le manuscrit unique du texte arabe du manuel astronomique (zij) de l'astronome Symen al-Battāni (fl. Ragga, environ 910 J. C.). C. A. Nallino, qui a publié ce zíj, a trouvé, parmi quelques tables qui ne doivent pas appartenir au travail original d'al-Battâni, deux petites tables qui donnent la hauteur du soleil et son azimut pour chaque heure temporaire, calculés pour la latitude 36°, employée par al-Battani pour Ragga et acceptée au

Stdillet-père présente une traduction de la première moité du traité dans loquel on trouve une discussion de la gnomonique Sédillot-fils offre un sommaire assez mal présenté de la deuxième moitié du traité.

^{3.} Voir Sédillot-père, pp. 136-137 et 276. J.-J. Sédillot a faussement daté al-Martakushi à 1230 J. C. (voir Sédillot-père, I., pp. 13-14) et n'a mille part mentionné qu'il travaillait au Caire.

^{4.} Sur al-Muqsi voir Sutur, no. 383

⁵ Sar al-Khwārizmī voir l'article de G. J. Toomer dans DSB. Son traité sur les cadrans se trouve dans MS Istanbul Aya Sofia 4830, fols. 231v-235r, copié 626H/1228-29 à Dames.

^{6.} Sur ce traité voir Sezgin, V, p. 334, no. 34.

une deuxième courbe de l'east fut tracée à sa gauche. C'est nettement le cas pour les déclinaisons septentrionales (partie inférieure de la courbe); pour les déclinaisons meridionales, il est impossible de distinguer entre les deux branches. Notre hypothèse se base sur le fait que la branche inférieure droite de la courbe de l'east est effectivement fautive et que la branche inférieure gauche est plus correctement disposée (voir Section IV).

Bien qu'il soit beaucoup plus récent (696 H 1296 J. C.) que la mosquée à laquelle il était destiné (elle tut construite en 259 H = 872 J. C.), ce cadran est le plus ancieu des cadrans solaires musulmans du Caire qu'on connaît aujourd'hui. Son dessin, nous l'avons vu, est original. La gravure est d'une exécution parfaite. Ses inscriptions sont d'une ecriture très rare: elles sont en caractères karmatiques de la forme la plus élégante; les points diacritiques y sont fidèlement indiqués. A tous ces titres et bien que nous ne le connaissions que par une reproduction, heureusement très exacte, le cadran solaire qui ornait jadis la Mosquee d'Ibn Tülün était une pièce splendide, au moins à première vue.

III. Sur les tables employées par les astronomes arabes pour la construction des cadrans

En considérant les nombreux traités sur les cadrans écrits par des savants arabes aux premiers siècles de l'Islam et la pléthore de tels traités (écrits principalement en Egypte, Syrie, et Turquie) dans les six derniers siècles, on voit que le petit nombre des cadrans qui subsistent ne représente point l'intensité de l'activité musulmane dans ce domaine. On connaît l'existence de traités sur les cadrans, dont la plupart sont perdus, préparés par plusieurs astronomes arabes dès l'époque Abbasside (spécialement au neuvième siècle).

Le plus complet parmi les documents les plus anciens qui nous sont connus à l'heure actuelle est une remarquable étude sur les cadrans plans qui émane de Thābit b. Qurra, philosophe, médecin, mathématicien, et traducteur, (fl. Baghdad, ca. 900 J. C.). Ce traité, publié et traduit par K. Garbers et analysé par P. Luckey, expose la théorie géométrique de toutes les sortes de cadrans plats, d'une mamère très rationnelle et très détaillée, précisant les formules diverses utilisées pour le calcul et la construction de ces cadrans, qu'ils soient horizontaux, verticaux, méridionaux, ou déclinants, orientaux ou occidentaux, ou inclinée et déclinants. Mais ce traité ne contient pas de tables. Ou trouve aussi dans le compendium de l'astronome arabe du treizième siècle Abū 'Alī al-Marrākushī et dans la moitié qui a été publiée en traduction

Voir Garbers et Luckey. Une autre très importante étude sur la gnomonique arabe est la thèse de P. Luckey citée dans Sezgin, V. p. 294

n'a rien à faire avec un tel cadran, nous pensons qu'il faut lire: til al-miqyās, c'est-à-dire, "longueur du style", ou bien, til al-miqyāsayn, c'est-à-dire, "longueur des deux styles". Nous croyons de plus qu'à côté de cette inscription on trouvait jadis un trait de la même longueur, qui manque sur le dessin de Marcel à cause des fractures du cadran.

Les 4 points cardinaux sont marqués: Nord A, Sud E, Est C, Ouest D. Les 2 styles identiques et perpendiculaires à la table étaient placés au sud de la petite échelle ouvrant chaque moitié, ils avaient leur pied en des points qui n'ont pu être relevés, car les styles avaient été arrachés en même temps qu'avaient été cassées les parties correspondantes de la daile.

Chaque moitié du cadran comporte les tignes des signes: sur la partie Est sont inscrites la droite des équinoxes (Balance 7) et les hyperholes d'entrées dans les signes (Ecrevisse 4, Lion 5, Vièrge 6, Scorpion 8, Sagittaire 9, Capricorne 10). Sur la partic Ouest sont également inscrites la droite des équinoxes (Bélier 1) et les hyperholes d'entrées (Taureau 2, Gémeaux 3, Ecrevisse 4, Capricorne 10, Verseau 11, Poissons 12).

Les heures marquées sont, selon l'usage ancien, les heures "temporaires", qui représentent la douzième partie de la durée du jour; les "heures" d'été sont ainsi plus longues que les "heures" des équinoxes (heures astronomiques), elles-mêmes plus longues que les "heures" d'hiver. Elles sont indiquées par des droites plus ou moins inclinées et qui sont numérotées, du matin au soir: la première I (il faut comprendre fin de la première heure), la deuxième II..., la sixième VI (midi), la septième VII... la onzième XI. Les heures du lever et du coucher du soleil ne peuvent pas être indiquées, le rayon horizontal du soleil rejetant alors à l'infini l'ombre des styles.

Entre la 9° et la 10° heure, sur la moitié Ouest du cadran l'inscription ques al-cass, c'est a dire, "courbe de l'ass" se refère à l'heure à laquelle, selon la date, doit être récitée la prière de l'ass, une des cinq prières obligatoires de l'Islam. D'après l'opinion dominante, l'heure de l'ass intervient dans l'après-nudi, lorsque l'ombre du style est égale à son ombre méridienne augmentée de la longueur du style.

Afin de prevenir le fidèle que l'heure de l'aşr approche, une plage sans gravure est ménagée sur la partie ouest du cadran, a partir de la droite de la 9º beure. Il est alors plus facile de voir exactement où se trouve la pointe de l'ombre et d'apprécier le temps restant à courir jusqu'a l'aşr. Mais en regardant de près la courbe de l'aşr on constate qu'elle parait avoir été dessinée en double, très nettement dans sa moitié nord, moins nettement dans sa moitié sud; quelle courbe faut il retenir?

La raison de cette double courbe de l'east semble être que la courbe originale de l'east, qui borde l'espace libre, s'est révelée fautive et qu'alors M. Marcel ont été rapportées d'Egypte et le dessin du cadran solaire qu'elles représentent se trouve reproduit dans l'Atlas de la Description de l'Egypte, cet ensemble monumental contenant les rapports de tous les savants chargés de mission et dont on peut dire qu'il a "lancé" l'égyptologie.

Car il s'agit bieu d'un cadran solaire, comme le laissent supposer les inscriptions. A première vue, la complexité (Pl. 1) est grande: deux gerbes de 7 branches, maintenues par des sortes de hens, partent des deux côtés de la dalle et s'élancent l'une vers l'autre en s'entrecroisant; partout des inscriptions qui semblent se mélanger et dont il faut retrouver l'application.

Mais pour qui a l'habitude des cadrans solaires musulmans, il apparaît bientôt que le dessin représente en fait deux moitiés d'un seul cadran, imbriquées l'une dans l'autre. Si l'ou fait glasser par exemple la gerbe de droite vers la gauche jusqu'à ce que coincident les deux échelles les plus petites (ou inversement la gerbe de gauche vers la droite, etc.), on reconstitue le dessin counu d'un cadran solaire horizontal ordinaire (Pls. 2 et 3). Alors que chaque moitié du cadran avait son style particulier, la translation ci-dessus effectuée a fait coincider les deux styles en un seul, qui gouverne l'ensemble du cadran reconstitué.

Pourquoi l'auteur de ce cadran a-t-il adopté la complication des deux demi-cadrans? Il faut d'ahord reconnaître que ce dessin, avec ses courbes, droîtes et inscriptions enchevêtrées, mais disposées selon un plan facile à tetrouver, répond bien à la recherche géométrique et ornementale chère aux dessinateurs musulmans. La conception de ce dessiu semble d'ailleurs être originale, car nous ne connaissons qu'un autre exemple d'une representation analogue (voir ci-dessous). En outre le procédé retenu permet de réduire considérablement l'encombrement du cadran.

L'inscription gravée sur le bord inférieur de la dalle indique:

c'est-à-dire:

... (?) pour faire (?) ces heures dans la mosquée ... (?) connue par (le nom de) Aḥmad ibn Ṭūlūn que Dieu le protège avec Sa grace - dans (?) l'an 696H (· 1296-97 J. C.)

Dans le coin droit supérieur se trouve une autre inscription qui ne se laisse pas très bien lire. Marcel et Sédillot ont cru y lire : ¡al al-Miṣrayn n-h, c'est à dire, "longitude des deux Miṣrs: 55°." Considérant que le longitude

premier autrur commence par un description du cadran (Section II) et le deuxième continue par une discussion des methodes employées par les astronomes musulmans pour construire les cadrans solaires (Section III), et une analyse mathématique des dessins du cadran de la Mosquée d'Ibn Țălūn comparés avec les tables préparées par les astronomes égyptiens à l'époque Mamelouke (Section IV).

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II. Historique et description du cadran

Décidée en 1798 par le gouvernement du Directoire, l'expedition d'Egypte comportait, outre les moyens militaires placés sous le commandement du général Bonaparte, un nombre important de savants et de techniciens appartenant aux disciplines les plus diverses, qui reçevaient la mission de se consacrer à l'étude de l'Egypte et de sa civilisation. Parmi les bénéficiaires de cette initiative se trouvait M. J. J. Marcel, ancien directeur de l'imprimerie royale, grand spécialiste des langues orientales et de leurs écritures.

Dès son arrivée au Caire, M. Marcel se mit à dessiner et à reproduire toutes les inscriptions en langue arabe qu'il put relever sur les monuments, principalement sur les mosquées, écoles et tombeaux.

A la mosquée d'Îbn Tülûn, l'ane des plus anciennes du Caire, il découvrit, dans un pan de mur du minaret attenant à la mosquée, plusieurs fragments brisés d'une dalle de pierre, qui comportaient de nombreuses lignes, courbes et inscriptions gravées. Il rassembla aussitêt ces fragments qui reconstituèrent, à part quelques manquants peu importants, une dalle de 69 cm, sur 53 cm, laquelle faisait apparaître un quadrillage complexe mais harmonieux. M. Marcel s'empressa d'en tirer plusieurs exemplaires par les procédés typographiques, comptant bien emporter plus tard les fragments eux-mêmes; mais... dès le lendemain matin, ils avaient disparu!... enlevés par quelqu'un qui avait peusé trouver là des objets de valeur, à en juger par les soins dont les entouraient des Français... Heureusement, les empreintes relevées par

Le Cadran Solaire de la Mosquée d'Ibn Țulun au Caire

L. JANINT ET D. A. KING*

I. Introduction

Depuis les recherches de Carl Schoy aux environs de 1920 sur la gnomonique arabel les cadrans solaires musulmans ont été presque totalement ignorés par les historiens des sciences. Ce qui manque évidemment pour la documentation foudamentale sur la gnomonique arabe, ce sont des reproductions et des descriptions détaillées des plus importants cudrans solaires arabes.* L'un de nous a publié en 1972 une description d'un cadran magnifique du célèbre astronome Syrien du quatorzième siècle Ibn al-Shatir, cadran qui n'avait jamais été décrit dans la littérature moderne, bien qu'il soit sans doute le plus splendide de tous les cadrans arabes connus.2 L'autre signature a préparé plus récemment une description d'un cadran tunisien du quatorzième siècle qui a une importance spéciale pour notre connaissance des origines des définitions des prières musulmanes. Le cadran que nous présentons ici, qui orgait jades la Mosquée d'Ibn Tülün au Caire, n'existe plus, mais il a été l'objet d'une très fidèle reproduction, parue dans la célèbre Description de l'Egypte préparée par les savants qui accompagnaient Bonaparte en Egypte. De son côté L.A.M. Sédillot en a donné une description dans son "Mémoire sur les instruments astronomiques des Arabes" d'après le traité de l'astronome Abū 'Alī al-Marrākushī, qui travaillait au Caire à la même époque que le constructeur du cadran de la Mosquée d'Ibn Tülön.7 Nous considérons qu'il est interessant de présenter a nouveau ce beau codran à la lumière des plus récentes recherches sur l'histoire de l'astronomie en Egypte médiévale.º Le

1. Voir Schoy 1 et 2, et auen Notes 1 et 2 à Section III

4. King 1.

5. Von Wiet, pls. 2-5 et pp. 100-101.

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^{2.} Plusieurs des cadrans soisures musalmans qui on connaît sont indiques dans Moyer On s'attend aut que la nouvelle édition que préparent M. Alam Breux de Paris et Mr. Francis Maddison d'Oxford contendra assea de nouvelles informations sur les cadrans pour susciter un rénouveau d'interêt sur ce sujet.

^{3.} Janin, reproduit on Kennedy-Chonem, pp. 107-121.

Description de l'Egypte, Etst moderne, planches, tome 11, planche c, et Sédilot-fils, pp. 25-26 et 56-58. Pour la documentation de l'usecription vous RCEA, ac. 5023 à p. 157.

Voir Sédillot-pere, II, Pl. XVI, fig. 86.
 Voir King 2 et les références citées.

We may well doubt that much would ever have come from Hunter's friend. Even more dubious is Tod's famous epitaph of Jayasimha himself: 10 "Three of his wives and several concubines ascended his funeral pyre, on which science expired with him." The "science" he supported never had a chance to develop in Sanskrit because no Indians were ever trained to utilize the observatories or the translations in a constructive manner, and because, whatever the results of Jayasimha's own observations may have been, they were not published in Sanskrit.

We have seen, therefore, that though a few elements of Islamic astronomy were adapted by Indian astronomers before the Moghul period, they were not allowed to affect in any way the structure of the traditional science. Moreover, though efforts were made to introduce various of the works emanating from the School of Samaroand to Sanskrit-reading astronomers in the seventeenth century, the translations met with hostility on the part of some. indifference from most, and, at best, an attempt to Indianize them on the part of a few; but these translations and adaptations contained nothing that would instruct the Indians regarding the reason for the claumed superiority of Islamic astronomy, which was its methodology involving both a reliance on carefully planned and executed observations and a concern with the cinemotics of the planetary models. Finally Javasimha's activities, while they resulted in Sanskrit translations of the Almagest and a few other works that could have taught this methodology to the Indians, were apparently completely ineffective; his original works in Sanskrit were not innovative, the translations themselves were ambiguous, and the majo contribution of his school to astronomy, the Zij-s Muhammad Shāhi was addressed to a Persian tather than to a Sanskrit audience. Nitvānanda, Kamalākara, Javasimha and others may have recognized the superiority of Islamic over Indian astronomy, but they failed to find a way to persuade other Indian scientists of this fact, in part, I believe, because they did not themselves perceive wherein the superiority lay.

For he did, with his Persian experts, construct those five famous observatories. Jagannatha mentions these observatories and some of the results obtained at them, and some obtained by other astronomers at other observatories.46 From this passage and from the Zij-i Muhammad Shahi produced in the name of Jayasimha probably by Khayr Allah Khaner we know that Javasimba intended to follow the traditional method of Islamic astronomy in correcting astronomical parameters by careful observation. and that he hoped to improve the Islamic technique by simultaneously observing the same phenomena from five different localities. Though Jagannatha refers to some minor corrections to parameters like the obliquity of the echptic, it appears unlikely that the tables in the Zij-1 Muhammad Shahi are very different from those in the Zij of Ulugh Beg; but no detailed study of Jayasimha's zij has yet been made, so that we cannot decisively deny real significance to his work. However, the description of them given by Hunter in 179718 makes it clear that the structure of the tables is entirely falamic. We do have for comparison, in Sanskrit, two works attributed to Jayacimha; a Javavinodasarini written in 1735, which contains tables for constructing the traditional Indian calendars, and a Yuntrarajaracana, a conventional Sanskrit treatise on the astrolabe. Neither work shows any trace of a new approach to astronomy. Moreover, other Sanskrit astronomical works written in Rajasthan and elsewhere in northern India in the eighteenth century seem not to have been influenced by Jayasimba. In fact, it seems probable that Khayr Allah Khan was the sole designer of this ambitious project, though Jayasımha supported it enthusiastically and contributed to it financially if not to any great extent intellectually, the Zij-1 Muhammad Shahi was never even translated into Sanskrit as had been the Almagest. And the translation of the Almagest, though extant in some two dozen complete or fragmentary copies, does not seem to have been used at all by those who composed treatises on astronomy in Sauskrit in the late eighteenth and ninetecuth centuries.

Hunter, however, claims to have met at I jiayini the grandson of one of Jayasimha's assistants whom he believed to be capable of carrying on the tradition because, while trained in traditional Indian astronomy, he possessed manuscripts of the Siddhantasamrêt and of a Sanskrit translation of Napier's logarithms, and he acknowledged the superiority of European science. To Hunter's regret, this pandita soon died, "and with him the genius of Jayasimha became extinct"."

^{86.} Siddhāniasamrāļ, vol. 2, pp. 1162-1165.

⁸⁷ Storey, pp. 93-95.

^{88.} W. Hunter, "Some Account of the Astronomical Labours of Jayaninha, Rajah of Ambere, or Jayanagar", AR 5 (1797), 177-211, esp. 205-209.

⁸⁹ Bid., 210.

and then gives Sanskrit equivalents or explanations of them. In doing this the translator demonstrates his knowledge of the traditional Sanskrit terminology in geometry and in astronomy. From time to time either he, or more probably the person who computed the longitude of the solar apogee in 1765, adds Indian material; thus the Sūryasiddhēnta is wrongly mentioned as using 22/7 as a value of τ , on the Indian measurements angula and yava are added to the usual Persian farsang, mil, and gaz. But otherwise this is a straightforward translation of an introductory manual of astronomy through which a Sanskrit reader could learn the elements of late Islamic astronomy, but nothing about its methodology.

The most conscientious effort, however, to make Islamic astronomy and its methodology available in Sanskrit was that of Savai Jayasimha of Jayanura in the early eighteenth century. Unfortunately, I have not yet had access to the unique manuscript, in the Maharaja's Museum at Jayapura (no. 46), of Nayanasukhopādhyāya's translation of Nasīr al-Din's Tadhkira with the commentary of al-Barjandi;" it would indeed be fascinating to examine it and to discover in what form the "improvements" to the Ptolemaic planetary models devised in Maragha were transmitted to eighteenth century India. But Jagannātha's translation of Nasīr al-Din's version of the Almagest, the Siddhantasamrat, has been published, though not critically edited; from this it is apparent that Jagannatha also had access, presumably through the earlier Sanskrit translations used by Munisvara, Kamalakara, and Nityananda, to at least some of the views of Ulugh Beg and of his colleague, Jamshid al-Kashi. 12 For, after the thirteenth and last book of the Almagest, he adds a supplement which includes a vantradhyayo, in which he describes the instruments that Jayasimha had set up in his observatories in imitation of those installed by Ulugh Beg at Samarquad,13 and an explanation of Ulugh Beg's and al-Kashi's derivations of sines." And this is followed by a series of notes on how to deal with traditional aspects of Indian astronomy that are not directly touched on by Ptolemy or that are treated in a different manner by Ptolemy but not, in Jagannatha's opinion, fully enough. He even tacks on at the end a description of the Sūrvasiddhānta's planetary theory, presented in the traditional style." The ambiguity towards scientific method implied by the inclusion of this material in Jagannatha's work is characteristic of Jayasunha's approach to astronomy.

^{79.} Hayatograntha, p. 16,

^{80.} Hayatagrantha. p. 137.

⁸¹ CESS A4.

^{82.} Storey, pp. 72-73.

^{83.} Siddhäntasumrill, vol. 2, pp. 1031-1048

^{84.} Siddhántaramrát, vol. 2, pp. 1048-1085.

^{85.} Siddhäninsamräf, vol. 2, pp. 1165 sqq.

and it computes the longitude of the sun's apogee "at the present time" for A. H. 1178, which began on 1 July 1764. These conclusions are rendered doubtful, however, by the fact that both the references to Kāshī and the computation of A. H. 1178 are omitted by Nīgesa, and are therefore likely to be interpolations in the other two manuscripts. This doubt is strengthened to a certainty by the existence of a manuscript of the Hayatagrantha copied by Tīkrāma Jyotişī in 1730 in the Mahīrāja's Museum in Jayapura (no. 24), and the recording in 1875 of another in Oudh that was copied in 1694.

The Hayatagrantha, therefore, was probably written in the seventeenth century, but on the basis of a Persian work different from that available to Nityananda in 1639. For the Huyatagrantha's parameters for its planetary models, which are completely Islamic, differ from those of Romaka as presented in the Siddhintarajo. The Hayatagrantha refers by name to 'Ala' al-Din 'Ali al-Oushii (allama Lausaji nama ulukavegasya guruputra) for his determination by "our observation" (asmadrasada) of the obliquity of the ecliptic, 28 and for the use of sunset epoch in Arabia (arabadesa), 24 and it mentions "our observation" (asmebbar vedhena rasadah) of the longitude of the solar apogee in Muharram 841 A. H., which is July 1437.75 This suggests that the Persian original of the Heyatograntha is the Risalah dar hay'at or Farst hay'or composed by al-Oushift at Istanbul and dedicated to the Ottoman Sultan Muhammad ibn Murad (1451-1481), the conqueror of Byzautium; the work was known in Mughal India as the commentary by Muslih al-Din Muhammad al-Ansari and was deducated to the Emperor Humayûn (1530-1556) The arrangement of the two texts supports this hypothesis; each contains an introductory section in two parts, two main sections (divided into six and eleven babs respectively in Persian, into four and ten in Sanskrit), and a supplement. I have not been able as yet to examine a copy of the Persian original in order to test this hypothesis. But the fact that the section on thronology in the Hayatagrantha" is a revision of that in Ulugh Beg's Zij" confirms the suggestion that the former represents a product of the school of Samargand.

I do not wish now to go into the details of the Hayatagrantha It should suffice to state that it consistently transliterates the Persian technical terms,

^{72.} Hayatagrantha, p. 69.

^{73.} Hayatagrantha, p. 24.

^{74.} Hayotugrantho, p. 128

^{75.} Hayatagrantha, p. 69.

^{76.} Storey, pp. 75-77.

^{77.} Hayatagrantha, pp. 128-133.

^{78.} L. P. E. A. Sedülot Prolégomènes des tables autranomiques d'Oloug-bre (Paris, 1853), pp. 7-28.

al-Rumi) of computing the sine of 1° and even of 1'."

Unfortunately, the Wellcome Institute's manuscript breaks off in the midst of Nityānanda's descriptions of the Islamic planetary models so that I do not know the extent to which the rest of his work is indebted to Muslim astronomy. But a sufficient portion of the Siddhāntarāja has been investigated to show that his planetary system is completely Islamic, though some of its elements are reworked to fit into a traditional Indian mode of expression. But, despite some assertions (not uncommon in classical Sanskrit texts on astronomy) that the Romaka computations lead to results closer to observed positions than do the Sūryasiddhānta's or Brahmagupta's, Nityānanda shows no understanding of the role of observations in improving the models of celestial motions devised by astronomers or their parameters. He has, in fact, done nothing but to recast a Sanskrit translation of an Islamic astronomical work into a form more congenial, and perhaps more acceptable, to an orthodox jyatiḥtāstrin.

Indeed, we have already seen that such a Sanskrit translation of a work dependent on Ulugh Beg's Zij was available in the seventeenth century, in Benares as well as in Delhi. And a manuscript of a Sanskrit Jica Ulugbegi (Zi)-1 Ulugh Beg) is preserved in the Mahārāja's Museum is Jayapur no. 45; it was acquired from Surata through Nandarama Josi, who is probably the Nandarama Misra who wrote voluminously on astronomy and astrology at Kamyakavana in Rajasthan between 1763 and 1778." We do not yet know whether this translation is identical with that used by Munisyara, Kamalakara, and Nityananda. But that it was expected that translations of astronomical works would be made from Persian into Sanskrit (as they were under the Moghula also from Sanskrit into Persian) is indicated by the existence of a special Persian-Sanskrit dictionary of astronomical terms intended to facilitate the process. This is the as yet unpublished Parasiprakasa composed under the patronage of Shah Jahan in 1643 by Malajit. 89 a scholar from Sristhals in Gujarat who was awarded the title of Vedengurava by the Emperor for his efforts.

One such translation that illustrates again the influence of the Samarquand school on Indian astronomers is the Hayatagrantha. This was edited a decade ago on the basis of three manuscripts in Benares, of which the oldest was copied by Nagesa in 1765. The editor believed that it was composed in Benares in the eighteenth century: for it refers to Kāshi several times.

^{67.} Siddhānjarāja 3, 19-85

^{68.} CESS A3, 128b-130b.

^{69.} CESS A4.

^{70.} Ed. V. Bhatjäcarya as SBG 96. Váránasi 1967

⁷¹ Hayatagrantha, pp. 22, 95, 101-102, and 120-121.

In fact, Nityananda further feels constrained to cast his expression of the mean motion parameters of the planetary theories of his Muslim source in the traditional Indian form, and to give instructions for deriving from mean longitudes computed according to the Romaka those computed according to the Saurapaksa and the Brahmapaksa, presumably to demonstrate that differences already exist within the Indian tradition, and that therefore the unfamiliarity of the Islamic parameters is not to be regarded as in itself vitiating them. Thus the normal Indian divisions of the Kalpa and other auts of time are described;40 the mean motions of the planets, their nodes, and the zudiac (i.e., precession) are given as integer numbers of revolutions m a Kalpa; and the computation of the ahargana follows the traditional pattern, though the epoch is noon at Lanka, which is (mean) sunrise at Romaka.41 The mean longitudes resulting from following these rules are then corrected by bijas, whose purpose seems to be to compensate for the insecuracies involved in expressing the Islamic mean motions as integer rotations in a fixed time; Nityānanda tates that they are necessary to bring the results into conformity with observations.41

The dimensions of the Romaka's planetary models, however, are presented in Ptolemaic terms as eccentricities and radii of epicycles; and the circumferences of the manda and tighta epicycles of the Saura and Brahma paksas are reduced by Nityananda to the same terms. 63 The models themselves are thoroughly Islamic, with equants, protective spheres, and crankmechanisms for the moon and Mercury. 44 The cosmology is almost equally Islamic; 06 the earth is surrounded by spheres of the Indian water, fire, wind, and space rather than the Aristotelian water, air, and fire, but beyond that some the seven planetary apheres in proper order. The eighth sphere, that of the zodiac, rotates at a precessional rate of 10 in 70 years; and the ninth sphere, crystalline and containing the constellations, rotates daily. Here there is no apology offered, nor indeed any justification of the presentation of these alien theories in Sanskrit.

Nityananda's sine table, however, which gives the sine to five sexagesimal places for every degree from 1° to 90° with R equalling 60, is fully justified mathematically; for he gives complete rules for its computation. including Jämshid al-Käshi's method (which was repeated by Qadi Zadah

^{59.} Siddhäntarája 2, 2-21.

^{60.} Siddhântarāja 2, 22-27.

⁶¹ Siddhäntgräig 2, 28-34.

^{62.} Siddhänterdie 2. 35-37.

^{63,} Siddhäntaröja 3, 3-18.

^{64.} Siddhāntarāja 3, 197 sqq

^{65.} Siddhäntaräia 3. 180-196.

^{66,} WHMRL V 36 ff. 18v-19.

"Having examined the Romakasiddh inta [i.e, a zij al-Rūmi], the Saura, and that of Brahmagupta, and knowing the (longitudes of the) planets corrected separately (by each), I have composed an accurate siddhānta".

"It always attains in every way the equality between computation of the planets' (positions) and observation that comes from the Romaka. In this (science, however,) they know that the Sauraiantra is like a Veda, and that even that composed by Brahmagupta possesses suitable methods".

"Then who was (this) Romaka who is numbered among the munis, the gods, and so on? I will tell you the answer to this (question); listen, as it was agreed to previously by Sūrya and Aruna":

"because of (their) fondness for history and stories. Even Bhaskara was known as Romaka because of a curse pronounced by Indra: Yavana lived in Romaka'a city."

"When the curse was removed because of the favor of these two, the sun himself in ancient times composed the best treatise here, which has the form of tradition (stute) though in the guise of being Romaka's".

Nityananda has based this myth, as he himself indicates, on one in the Joanabhaskara or Süryarunasamuada" wherein Sürya claims that he revealed the Romaka(siddhinta) to Romaka when he was born among the Yavand shedgues of a curse of Brahma, and that the Romako was then revised by Romaka in Romakanagara. The author of the Jaanabhaskara was, I believe, thinking of the astrological Romakasıddhönta which claims to be part of a Srisaväyanasamhua,30 whereas Nityananda refers to a work on Islamic astronomy. It is tempting, because of the name, to think of one of the works composed by Oadi Zādah al-Rūmi, " the teacher of and collaborator with Ulugh Beg perhaps his commentary on al-Jaghmini's Mulakhkhas fi al-hay'a. Whatever the case may be, Nityananda feels it necessary to justify Islamic astronomy to his audience not on the basis of a rational discussion of its methodology and an observational testing of its results (though he does state its superiority without adducing any evidence), but on the pretext of its being derived from the revelation of an Indian deity. Such a camouflage is certainly not new, as students of Abū Ma'shar's Kitāb al-ulāf, for instance, well know:18 but it is significant that even the most enlightened Indian astronomer of the seventeenth century did not dare to base his claims on the evidence of the senses.

^{55.} A. Weber, I erzeichnis der Sanskrit-Handschriften (Berlin, 1853), p. 287,

⁵⁶ CESS AS.

^{57.} Storey, p. 67.

^{56.} D Pingren, The Thousands of Ahi Marshor (London, 1968).

Beg's Zj, for that zij seems not to describe the eccentric-epicyclic planetary models with the protective spheres (pale) of Ibn al-Haytham and the later Islamic astronomers though Kamalakara does; ** Kamalakara, however, does not mention the equant,

Moreover, Lamslakara speaks with approval of the computation of planetary distances by the Yavanas on the basis of the internesting of the solid (mūrta) spheres⁵⁰ - a computation that differs from the normal Indian procedure of making the distances of the clanetary spheres inversely proportionate to the numbers of their rotations in a Kalpa.

It is not surprising, then, to find him quietly presenting as perfectly possible the Ptolemaic view of precession that Munisvara had so heatedly attacked. Nor is it uncharacteristic that his fifth adhikāra is a treatise on geometric optics, a subject never before, to my knowledge, discussed in such detail in Sanskrit. I presente that here also he has utilized an Islamic source, though I have not as yet been able to identify it

Kamalakara, then, was quite willing to prefer a Muslim opinion even though it is contrary to that of the rsis. But he neither accepted the methodology of Islamic astronomy, nor abandoned the basic procedures, models, and parameters of Indian astronomy. Two decades before he wrote, however, another Indian astronomer had gone much further in accommodating Islamic science.

Nityānanda⁵² was a Gauda Brāhmana connected with the court of Shāh Jahān at Delhi. In 1628 he completed an enormous Siddiāntasindhu, which he dedicated to Shāh Jahān's minister Āsaf Khān; no manuscripts of this work are available to me. In 1639 he composed a smaller work, entitled Siddhāntarāja, in twelve chapters. Of this I have examined a fragment in the Wellcome Institute Library in London (V. 36). This manuscript of 39 folios (numbered 1-36 and 38-40) contains the first two and a large part of the third chapters of the work.

In the Siddhantaroja Nityananda boasts that he will present absolutely new (that is, Islamic) material, whereas his predecessors have merely repeated each other⁵³ not an unjustified criticism of Indian astronomers. But he feels it necessary to disarm his critics in the following verses,⁵⁴ which I translate thus:

⁴⁹ Suddhänsonaupavineka 2, 253-284

^{50.} Sidáliánsatatsvavireka 2, 497 500.

^{51.} Siddhantotottvaprveka 2, 470.

^{52.} CESS A3, 173s-174s, and A4.

^{53.} Siddhänteröju 1, 9.

^{54.} Suldhäntorája 1, 14-16.

a particular fixed star. Thus he severely criticizes the Părasīkas, their Yavana predecessors, and their Iudian followers, for their arrogance in adhering to a doctrine dependent on their own deductions (svamoti) even though they are contrary to the opinions of the rsis:" at one point he even asserts that ridicule arises against anyone who has confidence in the words of the Yavanas on this matter through misunderstanding the true meaning of precession in Indian astronomy and trusting those observations that the Yavanas call rasada (Arabic rasad) "Munisvara's objections to precession were attacked by Kamalākara's brother, Ranganātha," in his Lohagolakhandana, which in turn was assailed by Munisvara's cousin. Gadādhara, in a work entitled Lohagolasamarthana.

Thus Munisvara's knowledge of the Sanskrit version of an Islamic astronomical work has not been allowed to influence his astronomical theories in any significant way. At best he refers with indifference to some aspect of Islamic science, but more commonly he feels at least obliged to deny validity to what he does find it necessary to mention. And his ultimate weapon against the observational basis of Ptolemaic astronomy is ridicule of what does not conform to the sayings of the ancient sages.

A more tolerant view of Islamic astronomy is manifested by Kamalākara in the Siddhāntatattt oviveka that he completed in 1658, as by his brother Ranganātha in his Bhaingivibhangikarana. Kamalākara agrees with the Yavana opinion that the inhabited parts of the earth rise above the sphere of water so as, however slightly, to alter the local horizon, though he hastens to add that this opinion does not contradict the gods and past Like Munisvara he refers to Khāladātta, which he wrongly locates 22° West of Romaka; but he proceeds to give a set of the terrestrial coordinates – he calls longitude tāla (Arabic tāl) — of twenty cities. The only cities on this list that are located outside of India are Kabul and Samarqand; and in the seven cases where cities are included in Ulugh Beg's geographical lists, the coordinates, with the exception of a few inisreadings of abjad numbers, are identical.

Kamalākara confirms his acquaintance with Ulugh Beg by referring to the computation of a table of sines by "Mirjolukabega". 48 This knowledge probably reached him, however, through a more elaborate treatise than Ulugh

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41 Siddhántasárvabhauma 1, 38-39 1, 123,2, 253-254, and 2, 274-275.
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^{42.} Siddhäntasarrabhauma 2, 279.

^{43.} CESS AS

^{44.} CESS A2, 115a

^{45.} Bhangivibhangikurana, pp. 31-32

^{46.} Siddhantutermurweka 1, 120-126.

^{47.} Siddhantotattvosiveka o. 17º 174; Essay Table VIII 27

^{48.} Seddhäniataiszavereka 2, 89.

section of the Siddhāntasiromant. In this he criticizes the theory of the Yavanas (i.e., the Mushms) that there is an unmoved crystalline (kāca) sphere supporting the sphere of the constellations (mūrtimat) and enabling it to rotate daily from East to West, for, he says, the crystal could not bear such a weight, especially since the sphere of the constellations in its turn bears the weight of the sphere of the codiac. What else he might have derived from a Muslim source I do not know, as I have not had an opportunity to examine manuscripts of his other works.

The same is also true of most of the Siddhantasarrabhauma, which was completed by Munisvaras on 7 September 1646; of its twelve adhyavas, on which Munisvara wrote his own like, only the first two and part of the third have been published with their commentary. In these chapters are found such relatively trivial matters as the recording of the definition of a sidereal month according to the Pārasīkas40 (Munīsvara claims that the concept is useful for astral omens, but not in astronomy): it is stated that the origin of longitudes in the geographical tables of the Parasikas is a city called Khāladātta near Romaka37 (in fact, of course, this place is the Etcrnal Islands - al-jazā'ir al-khālidat - of Arabic geographers); it is claimed that, even though the methods of the Parasikas for correcting the mean longitudes of the planets beginning with the moon are described in the language of the gods (that is, in Sanskrit), yet they must be rejected by the wise because they are without proof;34 and it is mentioned that, whereas for the orthodox the blue sky is a sphere of metal (a lohagola), the Pārasīkas claim that the heavenly spheres are crystalline 30 All of these matters, even the last, seem to trouble Munisvara very little; the reader is warned against some, but never in a very emphatic manner. He was much more incensed by the theory of precession when understood to imply a tropical rather than a sidereal reference system. For the Indians, though they have various theories of precession and treprdation,44 traditionally used them only for the correction of the sun's declination; the juncture of the sun's declination circle with the equator may be permitted to move with respect to the fixed stars, but the traditional Indian method of describing mean motions as integer numbers of sidereal rotations within a Kalpo or a Mahayuga necessitated, in Munitvata's opinion, the unswerving connection of the origin of the zodiac with

^{34.} Maries 1, 2, 1-6.

^{35,} CESS A4

^{36.} Suddhäntasärrabhauma 1, 17

^{37.} Siddhäntasärvahhavmafikä 1, 136

^{38.} Siddhäntasårnabhauma 2, 222.

^{39.} Siddhäntasärvabhauma 2, 228.

^{40.} D. Pingree, "Precession and Trepidation in Indian Astronomy before A. D. 1200", Journal for the History of Astronomy, 3 (1972), 27-35.

are repeated often in Islamic zijes. These Goal-year periods, with the exception that Venus' eight-year period was altered to a 227-year period, were soon used as the basis of an enormous set of planetary tables, the Jagadbhūsana, compiled by Haridatta'' in Mewar in Rājasthān in 1638; Haridatta, however, apparently used an Indian rather than a Persian set of astronomical tables in carrying out the computations of his own tables; the same is true of Trivikrama,25 who composed a similar set of planetary tables based on the Goal-year periods at Nalmapura in 1704 Their knowledge of the Goal-year periods, then, simply provided a convenient framework for a form of perpetual tables, as it had in the West for al-Zarqāli and his source and successors.

In Benares in the eighteenth century the most important astronomers belonged to two Maharasırıan Brahmana families which had migrated to the city in the sixteenth century. The descendents of Cintămani, a member of the Devaratragotra residing at Dadhigrama on the Payosni, include Munisvara Visvatūpa,20 who was born in 1603, the year in which his father, Ranganātha," completed his famous tikā on the Sūryasıddhānta, the Gūdhārthaprakāšīkā. Munīsvara's great rīval was Kamalākara. 11 who was descended through Divakara, a pupil of Caneta, from Rama of the Bharadvajagotra, a resident of Golagrama on the Godavari, not more than a few days' journey from Dadhigrams. These two men and their numerous siblings, cousins, and nephews were all engaged in astronomical activities, but always within the context of the traditional Indian siddhintas, particularly those of the Saura and Brahma paksas. From time to time, however, they display on awareness of Islamic astronomy, which seems to have been available to them in the form of a Sanskrit translation of the Zij completed by Ulugh Begis at Samarquand in about 1437/1438 or some derivative of that zij. The precise source of their knowledge remains obscure, however, we will return to the question of the Sanskrit versions of Ulugh Beg's astronomy later in this paper.

The carliest of these Benares astronomers to demonstrate a knowledge of Islamic astronomy is hamalākara's father, Nisimba, 22 who wrote a commentary on the Süryasiddh.nto in 1611 and one on the Siddhantoirroman; of Bhāskara in 1621. Unfortunately, of these two gigantic works all that has been published is his commentary on the first adhikara of the grahaganits

^{27.} CESS 46.

^{28.} CESS A3, 92b-93b, and A4.

^{29.} CESS 44

^{30.} CESS AS

^{31.} CESS A2, 21a-23a, A3, 18a, and A4.

^{32.} CESS A4. Storey, pp. 67-72

^{33.} CFSS A3. 2040-2060.

of the astrolabe stars - Mahendra is quite willing to substitute Islamic procedures and values for the Indian, without any apparent effort to determine in what sense they might be superior; it was easier to take them over than to recast them in an Indian mold. In the other elements of astronomy he gives no indication that it is at all advisable to abandon or modify existing Indian theories.

The next major infusion of Islamic astronomy into science in Sanskrit seems to have occurred under the Moghuls, who, like Fīrūz Shāh, promoted intellectual exchanges between their Muslim and Hindu subjects. I employ the word "major" because there is one minor case of transmission that cannot be ignored. The Kerala astronomer, Acyuta Piṣāraṭī, is in his Sphutanirnaya and Rāisgolasphutāniti written in the 1590's, proposed a formula for reducing the mean longitude of the moon in its orbit to an ecliptic longitude. Such a reduction had first been suggested, by Yaḥyā ibn Abī Manṣūr in the Zīj al-mumtaḥan, composed under al-Ma'mūn in the 820's. Acyuta probably bears witness to some transmission of at least a part of Islamic lunar theory that took place on the Malabar Coast in the fifteenth or sixteenth century.

A survey of Sanskrit astronomical texts composed in Western and Northern India in the sixteenth century, however, has yielded no reflexions of Islamic astronomy. I have examined, among others, the works, published and unpublished, composed by Jāānarāja²⁰ at Pārthapura on the Godāvarī in 1503; by Ganésa²¹ at Nandigrama in Gujarat between 1520 and 1552; by Dinakara²² at Bārejya in Gujarat between 1578 and 1583; by Ganésa²³ nephew and pupil, Nrsimha,²² at Nandigrama between 1588 and 1603; and by Rāmacandra²⁴ at Benares between 1590 and 1600. Members of the families of several of these sixteenth century astronomers, however, were the leading advocates and critics of Islamic astronomy in Benares in the seventeenth tentury.

But the first author to whom we must refer is Visrāms from Jambūsara in Gujarat, who wrote a description of various astronomical instruments, the Yantrairoman, in 1615. What is of immediate interest to us in his work is the inclusion of the Babylonian Goal-year periods of the planets, which, of course, figure prominently in Book IX of Ptolemy's Almagest, and

^{19.} CESS Al, 36b-38b, and A4. Ratigolaspkujānīti 47; Eisay IX 2

^{20.} CESS A3, 75a-76b.

^{21.} CESS A2, 94a-106b, A3, 27b-28a, and A4.

^{22,} CESS A3, 102b-104b, and A4.

^{23.} CESS A3, 202b-204a.

^{24.} CESS A5.

^{25.} CESS A5.

^{26.} Yantratiromani 92-94.

is probable that he derived this second component also from an Islamic source. It was also known to his contemporary. Bhojar $\tilde{s}_1a_1^{13}$ who wrote the $R\tilde{s}_1a_1$ miganka, with epoch of 21 February 1042, at Dharā in Mālava.

It is highly unlikely, however, that this source should have been the translations of Euclid's *Elements* and of Ptolemy's *Almagest* that al-Birūni claimed, in about 1030, to be engaged in. This claim must be regarded as sheer bravado, since the knowledge of astronomers' Sanskrit displayed by al-Bīrūni and his pauditas was totally inadequate to the task. Another channel of scholarly exchange must be imagined, and of a more limited character; the only elements of Islamic astronomy that appear in Sanskrit texts at this early date relate to the sun and the moon

The next phase in the transmission of Islamic astronomy to India. if we regard Bhāskara's" innovations in trigonometry as entirely his own, was the introduction of the astrolabe into Western India under the Tughlugs. Mahendra Surit composed the first description of this instrument in Sanskrit, the Yantraraja, at Bhrgupura - that is, modern Broach in Gujarat - in about 1370; according to his pupil, Malayendu," who wrote a commentary on the Yantraraja in about 1382. Mahendra undertook to write his treatise at the request of the astronomers of Firuz Shah (1351-1388), during whose reign Sanskrit works were also translated into Persian. The astrolabe itself, of course, was developed in the Roman empire, though our earliest extant examples are Arabic. Mehendra and Malayendu not only introduced the construction and use of the instrument to Indian astronomers, but also an Islamic sine table in which R equals 3600 or 1, 0, 0; a table of declinations with the Islamic value, 23;35°, for the obliquity of the ecliptic; a list of the latitudes of 77 cities, most of which are in India though many are located elsewhere in the Middle East (the Ptolemaic system of representing terrestrial coordinates had not previously been used in Sanskrit texts); a catalogue of 32 astrolabe stars whose coordinates are derived from the Almagest, with the Ptolemaic longitudes corrected for precession (at the rate of 1° in 66 2/3 years) for 1370; and the cotangent tables normal on the backs of Eastern Islamic astrolabes.18 Thus, in those elements necessary for the use of the astrolabe - trigonometry, terrestrial latitudes, and the coordinates

^{13.} CESS A4. Rájampjánko 1, 25; Fissay V 124,

^{14.} D. Pingree, "Al Biruni's Knowledge of Sanskrit Astronomical Texts", in The Scholar and the Saint (New York, 1975), pp. 67-81.

^{15.} CESS A4. Siddhāniasiroman 1, 2, 23; Essay Tuble V 43, and jyotpatti 16. and 21. Essay V 127-128

^{16.} CESS A4.

^{17.} CESS A4.

^{18.} Yantzarājatikā 1, 5-6, Yantzarāja 1, 22-40, and 1-70, Essay Tables XI 1 - XI 3

between the sun and the moon. The result of Ptolemy's model, with its specified dimensions, is that the maximum equation at syzyges is 5;1°, at quadratures 7;40°. In the tenth century a model producing an identical effect first appears in India. The epoch of Muōjāla's' lost Brhamminasa is 9 March 932 at noon (noon-epoch in itself is characteristic of Ptolemaic and Islamic astronomy, but alren to India); his extant Laghumānasa was commented on by Prašastadhara' in Kāsmīra in 958; and both of these treatises were encountered by al-Birūni in the Paūjāb in the 1020's. It is likely, therefore, that, although Muōjāla's Laghumānasa is now found only in South India. he originally composed it in the West or Northwest, and had contact there directly or indirectly, with Muslim astronomers.

Mubjala, however, following the Indian tradition, did not regard planetary models as cinematic or as in any way representing physical reality, but as calculating devices. Thus he felt free to replace Ptolemy's crank mechanism with an elegant formulation of the evection.

$$0 = (\overline{\nu}_m - 11^s) + Cos (\lambda_s - \lambda_s) + Sin (\lambda_m - \lambda_s),$$

where λ denotes celestial longitude, and the subscripts m, s, and a denote moon, sun, and apogee respectively. Because of his choice to express his parameters as integer parts of a radius of 488, his simple lunar model generates a maximum equation of 5;2°; while his formula for evection, since he employs the integer 11° in the first factor, results in a maximum of about 2;29°, so that Muōjāla's maximum lunar equation at quadratures is 7;31° instead of Ptolemy's 7;40°.

A result closer to Ptolemy's was provided by Srīpati, who wrote various works between 1039 and 1056, at Robinikhanda, about 150 miles south of Ujjayini. Srīpati accepts the Brāhmapakṣa's simple lunar model with an epicycle that pulsates in a complex fashion as the body approaches the horizon, but which at its mean, in the meridian, produces a maximum equation of 5:2,7° For the evection Srīpati¹¹ accepts Muñjāla's formulation, but modifies the first term so that the maximum correction is 2:40°—just 1 minute more than Ptolemy's - and the maximum equation at quadratures, when the center of the moon's epicycle is on the meridian, is 7:42.7°.

Srîpati also gives a complete formulation of the equation of time including both that part which is due to the sun's velocity, which had already been known to Brahmagupta, 12 and that dependent on the sun's longitude. It

^{7.} CESS A4.

^{8.} CESS A4

^{9.} Laghumánasa 18-19, Essay IX 1.

^{10.} CESS A6

^{11.} Siddhäntašekhara 11, 2-4; Essay v 123.

^{12.} CESS A4. Brāhmasphuļasiddhānta 2, 29. Eseny V 66

of planetary motion to scientists of the early "Abbasid period," emphasized perphaps over-emphasized the role of observation in refining planetary theories, and because of this emphasis developed both the necessary instruments and theories of optics and of the behavior of light. The most noteworthy Indian reaction to these aspects of Islamic astronomy, though characteristically having no discernible practical effect, was the program for the reform of Indian astronomy instituted by Jayasimba, the Mahērāja of Amber from 1700 till 1743.3 Under his patronage were built the massive observatories at Vārānasi, Ujjaviņi, Mathura, Dilli, and his own Jayapura, while under his patronage the industrious Jagannatha' translated Euclid's Elements and Ptolemy's Almagest into Sauskrit, and the less well-known Navanasukhopādhyāya," at the dictation in Persian of Muhammad Abida (who acted as an intermediary in the way that Spanish-speaking Jews had for some of the Latin translators of Spain in the twelfth and thirteenth centuries) translated Theodosius' Spherics and Nasir al-Din's Tadhkira with al-Barjandi's Sharh thereon. But these achievements, impressive though they might appear, were at the end rather than the beginning of the Islamic influence on Indian astronomy. Let us turn now to the predecessors of that beginning.

Non-Ptolemaic forms of Greek astronomy, sharing many characteristics with what we can reasonably reconstruct of the theories of Hipparchus, were transmitted to India in the third or fourth century A.D., including several alternative planetary models and mathematical descriptions of other colestial phenomena; these were given their characteristic Indian expressions in the fifth, sixth, and seventh centuries, from which developed four of the five schools of astronomy or paksas - in chronological order the Brāhma, the Ārya, the Ārdharātrika, and the Saura. These astronomical schools were generally conservative, but did permit the development of new computational techniques; and it is in the mathematics ancillary to astronomy - trigonometry and indeterminate equations - rather than in astronomy itself that the Indians excelled. There was no tradition of systematic observation in early Indian astronomy.

The Hellenistic lunar model that was transmitted to India allowed for only one inequality in its motion, which was accounted for by an epicycle; Ptolemy's model had a more complex structure, with the center of the moon's deferent traveling on a concentric at double the rate of the mean elongation

D. Pingree, "The Greek Influence on Early Islamic Mathematical Astronomy", Journal of the American Oriental Society, 93 (1973), 32-43.

³ CESS A3, 63n-64b, and A4.

^{4.} CESS A3, \$6a-5Ha, and A4

^{5.} CESS A3, 132n, and A4.

D. Pingree, "The Herovery of Early Greek Astronomy from India". Journal for the History of Astronomy, 7 (1976), 109-123.

Islamic Astronomy in Sanskrit

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The problem that I wish to examine in this paper involves in particular the awareness of and reaction to Islamic astronomy on the part of the traditional Indian astronomers practicing their science in northern India under the Moghuls. But in more general terms I believe that it illustrates the characteristic methods by which Indians throughout their history, until the mneteenth century, have responded to a superior foreign science (the judgment of superiority is here based on experience rather than on theory), though in the last phases of Moghul astronomy in Sanskrit one can perceive the begiamings of a new attitude foreshadowing that which has become the prevalent one among contemporary Indian scientists. Briefly, the shift in attitudes to which I allude is from the classical position that alien scientific systems may be adopted to Indian use, but that they must somehow be made to conform to the older Sanskritic tradition, and the resulting mutation ought to be presented as the revelation of a divinity or of an mi; the attitude of the contemporary Indian scientist is, normally, that there is one scientific method, internationally approved of and validated by experience and by its pragmatic success, and that the views expressed by gods and acers in the past are not guides to scientific truth, though some weaker souls may wish to vindicate them by reinterpreting them to conform to, and thus to anticipate, contemporary scientific hypotheses.

In the seventeenth and eighteenth centuries Indian intellectuals were forced to respond to a forerunner of modern science in the form of Ptolemaic astronomy as practiced by Muslims. Though accepting Aristotelian physics, Muslim astronomers for a variety of reasons, not the least of which was the availability of the conflicting Ptolemaic and Indian models and parameters

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^{1.} For hiographical and hibliographical information on the pothers discussed in these pages I refer the reader to D. Pingree, Census of the Exect Sciences in Sanskeit (henceforth CESS), of which Series A, vols 1-3 have appeared as Memoirs of the American Philosophical Society, vols 21, 86, and 111 (vol. 4 is in press), and to C. A. Storey, Person Literature, vol. 2, part 1 (henceforth Storey), (London, 1958). See also D. Pingree, "Essay on the History of Indian Astronomy" (henceforth Essay, eited according to formulas and tables) in Distributory of Scientific Biography, vol. 15, New York, 1978), where the few technical matters touched on in this paper are discussed, and B. Datta, "Introduction of Arabic and Person Mathematics into Sanskrit I sterature", PBMS 14 (1932), 7-21.

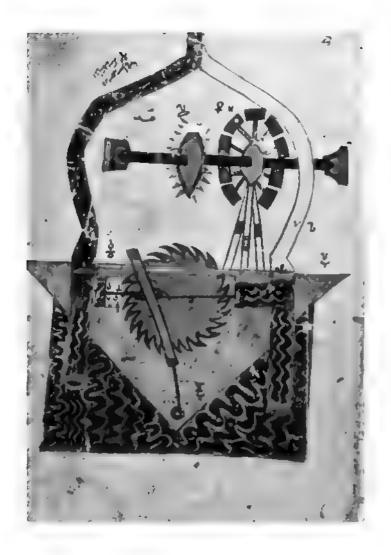


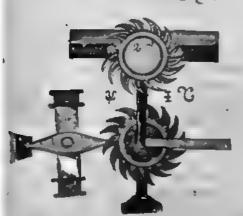
Fig. 7.

The main illustration of the complete machine; it is probable that this is a plan view, rather than an elevation (see Hussan ep. cit. 56-59).

المطرف البريخ فات دوا وة يهمنع وبنطبق دواحة آوا لمرآيمذ ببالآبهن آبوب فسمينل يريح آماأدني فع نضيب أ انطفت دها وا م وانت المادورخ ددادة ورصعدللاء حوة ل انوب م الدة بتيلاف ف يحمون دراغاه موسكا فدطول الانبوب في برخ آخره فالنف قالنف كته وكأنهلن وعل البريخ و وَأَنْبِرِبُ عليه لاونية وان عليها _ وظلمه من الي انبوب غليط فرونين وفية دواده عليناس والتغييطينه بالقدوم الطعف الاحتركان بيهاتث وفليه فدوع ويتزك فيعانيه سمن بريخ أاليحص وعلرج أعل حالات نامنات ويرثن وعرج انوبيو ومن اعل السنلعق معها المجعة وشله مغندهلي وسؤجانيوخ قيصه ف عندنغطة وركة تداجينت في طلة طري تضيب موكناك ينطقب البريخ الآعرين فاوية سريس الشناروق وضعفن ليسط بأنب خربى آلىھىردۇق تىلىبىرىت فى ئىلغۇپلىرى قىنىغىپ آ تبن المعة غرائسهم ف يُسازُ المُدَّمَع المائس بريح طول بن وال وارتضمن انوب سمالل يرزع أومق عامال مدوي الدح الما من برج أسيد انوب روارض في انهيب لاما الى بيخ ت

Fig. 6.

A drawing of one of the two cylinders - the ting at the end of the connecting rod is attached to the side of the slot-tod. مى الجورى اوس الصندوق بدور على كتيبة و عب القوص جلعه بدور بها الجوروع قل دايوالغرص ديد الجانث بإوزائ عن الصندوق وعلى القرص في داخل الصندوق و وعل الدندا جات و هي ارجة عن جاب الصندوق من وعلى وح الفرص وتلاً مناصب منعجمه في عند سهد واحد في الموطوفية فنه فيت مناص عند ذاوية عن الصدوق والطرف الخرف



سب بده سه زواب عندن طراح فالموالة الموادية والموادية والموادية في الموادية في

وشَيْ مَارَقِهِي وَمِن جِهِوْ أَلْجِهِوْ بَرِهِ وَعَوْمَ فَآنَ وَهُو النَّرِيُّ الْ نَلْمَةُ مَنْ وَبَهِلَ مِن حِنْ وَهُ وَمُوعِلَيْتُمِلُومَاكُ وَبُرِيَّعَهُ وَمِن وَمَا يَعْجَى بِعُورِدِعَ مُورَةٍ وَمِنْ َمِالْجِهُمْ Figs. 5, 6, and 7 (V.5, Figs. 139, 140, 141)

These illustrations are of the second of the alternative designs of the well-known slot-rod pump.

Fig. 5.

The two mething cogwheels, the upper one deteen from a paddle-wheel, the lower one having the stot-rod on its face. The orientation of this sketch is the same as in Topkapi 1472, whereas in Oxford Graves 27 it is turned through 90 degrees. The orientation shows here is almost certainly correct. The cogwheels are shown disengaged, otherwise the filestration is good

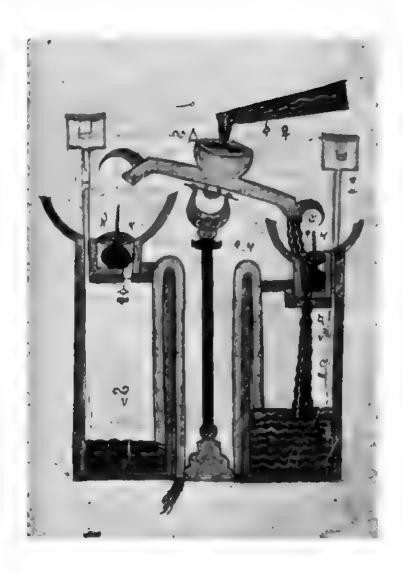


Fig. 4.

(IV. 10, Main illustration, Fig. 133).

Musical automaton. The whittles are at either eide, at the top, air-pipes lead into them from the two tanks. The water runs into one side from the balanced supply pipe, enusing the whistle to sound, until the float in the chamber at the top of the time rises. The vertical rod on top of the float causes the supply pipe to tilt and ducharge into the other tank. A siphon evacuates the first tank. The cycle repeats itself as long as water flows into the system



Fig. 3. (Addendum to IV.4, Fig. 125)

A fountambend having three possible shapes. It is supplied from two tanks, with a switching system similar to that described for Fig. 4 below. Three concentric pipes enter the fountambend, the two inner ones from one tank, the nater one from the other. Water from the innermost pipe emerges so a straight jet; it emerges from the second pipe as a 'tent' - the water impunges on a convex plate and descends as a curved sheet. After change-over it emerges from the entermost pipe as a number of curved jets.

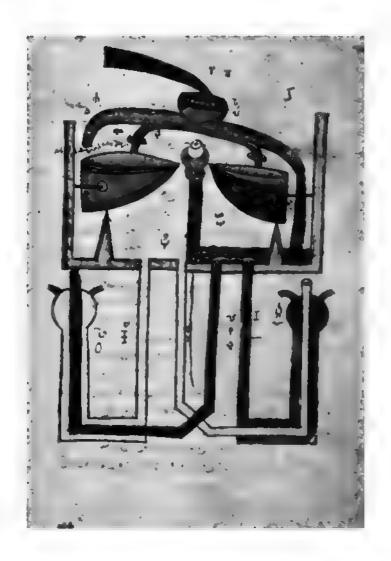
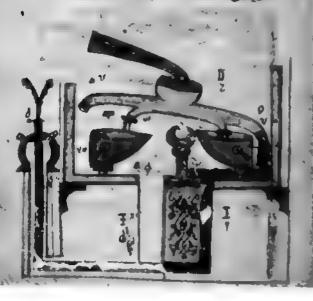


Fig. 2. (JV.2, Mem illustration, Fig. 122)

This is a doubled version of IV.1. One fountsinhead emits a single jet when the other is discharging several. When they change ever, the situation is reversed. Again, the rade attached to the tippingbuckets are emitted. فيدن إضراركم علوه المندمات من المابقة الطال المندلك ويرس كوف فنهت الويد مرالا بودن المحدث باللان مليماً من ويرس كوف فنهت المورض المابية المنت مليماً مطوع في من ويضا المنت المورض ويضا المنت ال



Illustrations

(The numbers in parentheses give the Category, Chapter, and Figure Nos. from Hill)

Fig. 8 (IV. 1, Main illustration, Fig. 121)

A fountain made to alternate by bleeding water from the man supply pipe, which is free to oscillate about an axle, into one or other of the tipping-buckets. As shown here, the discharge is into the right-hand side. When the tipping-bucket fills, it tilts and a vertical rod soldered to ats rear face pushes the supply pipe, causing it to tip towards the left. The vertical rods are not shown in this illustration but appear in the parallel illustration in Topkapi 3472

The fountamhead emits a strught jet when supplied from the left-hand tank, and several curved jets when supplied from the right.

the end of Chapter 10 of Category IV. The first part describes a woodwind instrument having 'fingers' that are raised and lowered in succession over its holes by came fixed to the axle of a water-wheel. There is no illustration for this instrument. The second part of the addendum describes the device shown in the illustration mentioned above. This is a rocker-arm consisting of two flume-beam swapes joined at right angles, and oscillating about an axle located at the joint. The oscillation is produced by the 'bleeding' of water through a narrow pipe from the main supply channel into whichever of the flumes is temporarily horizontal; when the scoop at the end of the flume fills, this side tilts and the other flume comes to the horizontal and its scoop begins to fill, and so on, Al-Jazari says that this device was not only used for fountains and musical automata, but that it was incorporated in many different machines.

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 47-64 in English, 129-165 in Arabic.
- Dound R. Hill, The Book of Knowledge of Ingenious Mechanical Devices. An annotated translation of al-Jasuel's work. (Doedrocht, Reidel, 1974).
- 5 Sotheby, Spring Islamic Soler, catalogue for suic on 3rd April, 1978, 122-127
- E. Wiedemann, and F. Hauser, 'Über die Uhren in Bereich der Islamischen Kultur', Novu Acta Abh. der Kaiserl. Leop. Deutschen Akademie der Naturforscher 100, Hulle 1915, 1-168.

The colophon is on page 293, after the end of VI. 5. On page 294 the letters of the 'secret' alphabet are given with their equivalents from the normal Arabic alphabet; the few lines of explanatory text are in a different handwriting from the rest of the manuscript - it is a badly written naskhi. There are three illustrations on page 295. The largest of these is in the centre of the page and is the main illustration of H.I. i.e. Fig. 80. It is clearly by a different draughtsman than the one who drew the illustrations for the main part of the manuscript; it is badly drawn and would be almost useless for explanatory purposes. Lower down, to the right and left of the page are two small, crude sketches of devices similar to those described by the Banu Musa. indeed the one on the right can be identified as their Model 79. Above either sketch there are passages describing these two devices (there is no text relating to the al-Jazari device). These descriptions are not in the words of the Bano Mūsā. The handwriting is different again, a somewhat better naskhi from that on page 294, but not as good as as that of the main manuscript. At the bottom of the page there is the start of a passage in Farsi, which continues on page 296. This passage, in yet another naskhi hand, is part of a treatise on weighing; at the bottom of the page there is a drawing of a balance with five pans. The contents of page 294 appear in most of the sl-Jazari manuscripts, and this page was probably added to supply an obvious omission. Pages 295 and 296, however, are quite extraneous.

Summarising from the foregoing tabulation, the only absolutely complete chapters are: III,1. - pitcher for dispensing hot and cold water; III,2. - pitcher for dispensing water; IV, 1 to 6. - fountains; IV, 9 and 10. - musical automata; V,1. - pump; VI,2. - protractor; VI,3. - combination locks. All the illustrations are included in these fourteen chapters with, of course, all the main illustrations. There are also another five main illustrations which appear in incomplete chapters, namely: I,9., Fig. 76 - monkey candle-clock; I, 10., Fig. 78 - candle-clock of the doors; IV, 7 and 8., Figs. 130 and 131 - musical automata; VI,5. Fig.173 - water-clock of the sailor. Half of the illustration of the door, VI, 1., Fig. 141, remains. This fine miniature was originally on one full folio, and it seems likely that the other demifolio is lost for good. Fourteen of the dispersed main illustrations were published as plates in Hill, op. cit., so we now have a record in two documents of 33½ of the original 50 main illustrations.

There are three chapters on water-raising machines, namely V, 1, 2 and 4, for which the text is complete although there are no illustrations.

In Hill, p. 238, Plate XXXII shows a device for which there was no description in the manuscripts that were available to me when I made the translation. There is, however, an addendum, to the text in the manuscript under review and in Topkapi 3472; in both cases this addendum occurs at

Category		Pages in new numbering	Original contents	Ōmissions		
	Chapter			Illustrations	Text	
17	Intro- duction	212	Text only	None	All except last two lines	
	1 to 10	212 to 245	10 Chapters Figs. 120 to 133, Pl. 32		y is complete, with all the except for the following text: end of chapter 7, start of chapter B	
;	1	245 to 248	1 Section Fig. 134	134*	None	
	2	248 to 250	l Section Fig. 135	135*	None	
	3	250, 251	2 Sections Fig. 136	136*	End of S.1, start of S.2	
	4	251 to 253	1 Section Fig. 137	137*	None	
	5	253 to 260	3 Sections Figs. 138 to 141°	None (This chapter	None is complete)	
VI	1	261 to 264, 269 to 273	3 Sections Figs. 142 to 148	Half of 142*	Introduction, start of S.l (section 2 is complete but is misnumbered as section 1)	
	2	273 to 277	3 Sections Figs. 149 to 152	None (This chapter	None is complete)	
	3	277 to 286	2 Sections Figs. 153 to 166	None (This chapter	None is complete)	
	4	287 to 290	2 Sections Figs. 167 to	172*	End of S.2	
	5	291 to 293	1 Section Fig. 173	. Поде	Last paragraph	

	15	Pages in new numbering	Original contents	Omissions		
Category	Chapter			Illustrations	Text	
	1	170 to 175	2 Sections Figs. 103, 104*	None (Chapter	None is complete)	
	2	175 to 183	2 Sections Figs. 105 to 108	None (Chapter	None is complete)	
	3	183 to 188	2 Sections Figs. 109 to 111	111*	Middle of S.2	
	4	188, 189, 265, 266	I Section Fig. 112*	None (Chapter	None is complete)	
	5	266, 267	2 Sections Fig. 113	113*	Most of the chapter	
	6	267, 268, 190 to 193	2 Sections Figs. 114, 115	114, 115*	Last few lines of S.2	
	7	194 to 196	2 Sections Fig. 116	116*	Start of S.1, middle of S.2	
	8	196 to 201	2 Sections Fig. 117	117*	End of S.2	
	9	202 to 207	4 Sections Fig. 118	118*	Start of S.1, end of S.4	
	10	208 to 211	2 Sections Fig. 119	119*	Start of S.1, end of S.2	

	-	Pages		Omissions		
Category	Chapter	in new numbering	Original contents	Illustrations	Text	
1	9	108 to 110	2 Section Fig. 76*	None	All S.1 except last two lines	
	10	IIO to 113, 130, 131	2 Sections Figs. 77, 78*	None	End of S.2	
ΕI	1	114 to 117	2 Sections Figs. 79, 80	80*	All S.1 except last three lines	
	2	117, 118	1 Section Fig. 81	81.	Middle of Section	
	3	119 to 129, 132 to 139	5 Sections Figs.82 to 86	82*	End of S.1	
	4	139 to 145	3 Sections Fig. 87	87*	None	
	5	146 to 155	3 Sections Figs. 88 to 93	88*	AB S.1, start of S.2	
	6	156 to 159	2 Sections Figs. 94 to 97	94*, 97	Start and end of S.2	
	7	160 to 162	3 Sections Fig. 98	98*	All S.1, centre of S.3	
	8	162, 163	2 Sections Fig. 99	99*	End of S.2	
	9	164 to 167	2 Sections Fig. 100	100*	Title, end of S.2	
	10	168 to 170	2 Sections Figs. 101, 102	102*	Start of S.1, middle of S.2	

Category	Čbapter '	Pages in new numbering	Original contents	Omissions	
				Illustrations	Text
Cover		1	-	_	~
Intro- duction		2 to 4	Same	-	-
	1	4 to 10, 69, 70, 11 to 30	10 Sections. Figs. 1 to 33	10, 11, 13,	End of S.1, centre of S.2, start and end of S.3, first few words of S.4, most of S.6 - only the start remains, all S.7, start and end of S.8, start and end of S.9
	2	30 to 36	5 Sections Figs. 34 to 40	34°, 39, 40	Most of S.1 - only the start remains, first few words of S.2, last few lines of S.3, all S.4, most of S.5
	3	59, 60 37 to 45	6 Sections, Figs. 41 to	41*, 42	All S.I. all S.2
	4	45 to 68, 71 to 76	15 Sections Figs. 48 to 59	48*, 51, 52, 59	End of S 1, last few lines of S.5, all S.6, start of S.7, end of S.12, start of S 13, end of S.15
	5	77 to 82	3 Sections Figs. 60 to	60°, 62,	Start of S.1, middle of S.3
	6	82 to 95 (86 is a duplicate of 85)	6 Sections Figs. 63 to 70	63*, 66, 67	Most of S.1 - only start remains, most of S.3 - only start remains, and some lines at the end, all S.4
	7	98, 96, 97, 99 to 103	3 Sections Figs. 71 to 74	74*	Last part of S.3
	8	104 to 107	, 3 Sections Fig. 75	75*	Start of S.1, most of S.3 - only the start remains

715, or December 1315. This is therefore the third oldest known copy of al-Jazari's work, being pre-dated by Topkapi Ahmet III 3472 and Topkapi H. 414 The list of Mas given by Hassan (op. cit. 60-62) brings up-to-date the the list in Hill 3-6. Of these fourteen Mss I have now examined the originals of eight, namely: Bodleian Library, Oxford, Graves 27 and Fraser 186; University of Leiden Or. 117 and Or 656; Bibliothèque Nationale, Paris. Fonds Arabe 2477 and 5101, Suppl. Pers. 1145 and 1145a. I have also seen pages from Hagis Sophis 3006. I have photocopies of Topkapi Ahmet III 3472 and Chester Beatty Library, Dublin, No. 4187. I have yet to examine. therefore, Topkani Hazine H 414 dated 672/1274, Topkani Ahmet III 3350 dated 863/1459, and Topkapi Ahmet III 3461, date unknown. Hassan assesses the first of these three as a very good copy, the second as inferior with regard to the illustrations, and the third as uneven, with some sections poorly written and illustrated but most of it of good quality. Leaving aside the question of completeness, it seems that the 715/1315 manuscript can be ranked among the best. The calligraphy is excellent, the illustrations are very fine, and the text, though not without errors, is free from major blemishes.

The manuscript has Persian pagination, added at some time after the copy was made. Unfortunately, this pagination is unreliable; some pages are unnumbered, some are out of order, and in certain cases the lengths of the lacunae indicated by the gaps in the numeration do not match the lengths of the missing text. The expedient was therefore adopted of numbering the pages (i. e. denifolios), starting with the cover, and then sorting the pages so numbered into order. This produced the following sequence: 1 to 10, 69, 70, 11 to 36, 59, 60, 37 to 68, 71 to 95, 98, 96, 97, 99 to 113, 130, 131, 114 to 129, 132 to 189, 265 to 268, 190 to 264, 269 to 296.

In the following analysis this new pagination is used, and the illustrations are given the Figure Nos. from Hill. In the right-hand column the abbreviation 'S' is used for Section. Al-Jazari provided one main illustration for each chapter and numbered them from 1 through to 50; these are marked with an asterisk.

Notice of an Important al-Jazari Manuscript

DONALD HILL*

This notice refers to a manuscript of al-Jazari's book on machines entitled The Book of Knowledge of Ingenious Mechanical Devices, or A Compendium on the Theory and Practice of the Mechanical Arts. It had previously been thought that the manuscript of this work dated 715/1315 had been completely dispersed; see, for example, Hill op. cit. p. 5, and Ahmad Y. al-Hassan in Vol. I, No. I of this journal. Happily, this assumption proved to be incorrect, since about two thirds of the original manuscript, the property of the Hagop Kevorkian Fund, was included in Sotheby's Spring Islamic Sales on 3rd April 1978 in London. As reported in "The Times" of 4th April 1978, the manuscript was purchased by Messis. Spink and Son of St James's, London for a little over £ 160,000. I would at the outset like to express my sincere gratitude to these two highly respected and responsible companies for the courtesy and co-operation that they have extended to me in the furtherance of my researches. Sotheby's gave me access to the manuscript before it was sold, and sent me a number of colour transparencies of the illustrations. I had fruitful discussions with members of the staff of Spink and Son, who provided me with a complete black-and-white photocopy of the manuscript. I am also very grateful to both companies for having given me permission to publish this paper, and to include in it, as I saw fit, any of the material that they so generously provided.

Some time ago a number of the illustrations were removed from the manuscript and found their way into various public and private collections. In my book I published twenty-one of these illustrations, these being all that I was able to trace. There are, however, $66\frac{1}{2}$ illustrations missing from the manuscript sold by Sotheby's, so clearly a number remain undiscovered. Most of the lacunae in the manuscript can be accounted for by the removal of these illustrations, since either the accompanying demifolios of text or the surrounding text were removed with the illustrations.

The manuscript is written on thick polished paper, 314 mm. by 219 mm. to the page, in very fine noskhi script with 21 lines to the page. The colopbon on page 207a (Persian paguation – see below) gives the name of the scribe as Farkh ibn 'Abd al-Laţif and the date of his copy as the end of Ramadān

^{* 3} Amey Drive, Great Bookham, Surrey, England. I wish to express my gratitude to the Royal Society for awarding me a grant in 1978/79 to assist me in my work on medieval Arabic technology

"Much has been said about the composition of (books on) the art of medicine, and the part of it which is on therapy is dealt with far more than is necessary, (while) the theoretical part (is dealt with) far less than is necessary".

It is possible that the concentration of theoretical matter and the dearth of description of practical procedures rendered it less useful and so less popular than al-Majūsi's book. And hence, it never diffused to the West like the other book. The same fate seems to have befallen another kunnash written within 50 years of K. al-Mi'a and contemporary with al-Majūsi's book, perhaps for the same reason. Al-Mucalajat al-buqrativya is a large system of medicine in 10 magilat compiled by Abū'l-Hasan Ahmad al-Tabari,19 the court physician to Ruku al-Dawla (932-976). This book has a similar arrangement of subject matter to K. al-Mi'a and deals with all the classical topics of medical theory. Diseases are likewise set out in the usual head-to-toe arrangement. The book is heavily biased towards theoretical discussion and is of high intellectual calibre. Relatively little attention is paid to matters of practical importance and it could not have had much appeal for the average practitioner. The author explains in the introduction to the book that be has compiled it in order to salvage medicine from the hands of the ignorant and the superficial, and to return it to the tradition of the ancients he so admires. The result is not unlike K. al-Mi'a, except that it is perhaps less lucid and complete. This book likewise did not claim the attention of the Latin translators, nor was its author apparently known in the Latin West. In recent times, its fourth maggia, which is on ophthalmology, was studied by Hirschberg,51 and some of its sections on diseases of the skin were translated into German by Mohammed Rihab.62 Otherwise, it has remained relatively unknown.

Despite these considerations, the question with regard to al-Masibi's book must remain largely unanswered. It must be said in conclusion that the omission of this book from the mediaeval list of translations deprived the West of an important compendium, equally as valuable as al-Majūsi's Kāmil al-ṣinā'a and of the same calibre as Ibn Sīnā's Canon.

^{47.} Some meagre facts about al-Tabari's life are to be found in IAU, I 521 See also GAL I, 257. 51, 422

⁵⁰ There is a complete manuscript of this work in the Bodleian Library, Oxford, Marsh 158.

⁵¹ J. Hirschherg, Geschichte der Augenheilkunde bei den Arabern (Leipzig, 1908), pp. 107-114.

^{52.} Mohammed Rihab, "Der arabische Arat af Tabari Übersetzung unzelder Abschnitte aus seinen Hippokratischen Behandlungen" "Sudhoffs Archw, 19 (1927), 123-168

territories. If they translated only what was available to them in Spain, then the choice of book was judged dependent on its being present there. This raises the further question of why K. al-Mi'a was not available in Spain. In fact, as was noted earlier none of al-Masibi's other books were translated into Latin either, nor does he himself seem to have been known to the Latin West. This is indeed a puzzle. Why, for instance, should "Ali b. al-"Abbās al-Majūsi's kunnāsh. Kamil al-nnā'a have been translated into Latin and not K. al-Mi'a?44 These writers are quite comparable to each other: both were Persigns and wrote their books in Persia within 50 years of each other. Thus, the problem of geographical diffusion should have been the same for both. The books are comparable in scope and style. Al-Majūsī's book is a large twovolume encyclopaedia on the whole of medicine, theory and practice. Like K, al-Mi'a, it discusses every aspect of medicine and classifies its subjectmatter in the same thorough way. The accounts are of the same order of lucidity and precision. Kamul al-sinā a is likewise written with great authority. However, there is a difference between the two in the amount of space given to practice as opposed to theory. In this sense, Kāmil al-sināca is the more belanced, for half of it is on theory and half on practice, whereas, K. al-Mi'a is mainly devoted to theory, as has been shown above. This is in line with al-Masihi's pupose in writing the book, for he says in his introduction:

فاقتصى هد الدم تحسب ما هو موجود عليه في نصبه اما في حسله هانه يرثب ويسهن وينجمي واما في خواء النحري منه فاء شمم ويصبح واما في العلاجات فانه تحتصر ويفرب فقلت تهدد الشرائط كلها وبدات الوسع والفاقة فيها فحرح أصبح وأثم وأسهر واصحو ما لمكن .

"This science, by its present nature, requires that it should be arranged in its entirety, simplified, and summarised. As to its theoretical part, this should be made complete and corrected; and as to its therapeutic part, this should be condensed and made more accessible. So I fulfilled all these conditions to the utmost of my capacity, and (the book) emerged more correct, complete, and easy to use, and as short as possible."

And further on in the introduction, he adds this:

48 'Ali b al-'Abbāa sl-Mojūsī l'ved and worked during the reign of the Persian roler, "Adud al Dawla (949-982). Very little is known of his life (see 14U, I, 236, al-Qifti, op. rit., p. 232 GAL, I, 237, SI, 423). His book, Kāmil al-Şinā'a, also known as al-Kuib al Malaki (because it was dedicut ed to 'Adud al-Dawla), was translated into Latin by Constantine the African as Liber Pantegni in the 11th century, and by Stephen of Antioch as Liber Regius in 1127, and enjoyed great faint suid popularity in mediaeval Europe. (See Leelerc, op. cit. 11, 359 and H. Schipperges, Die Assimilation for arabichen Michigan durch des laterinische Mittelalter, Sudheffs Archir. Beihefte, Heft 3, Wiesbaden. 1964, p. 35).

hyenas, and tigers, as many other kunnashat did, nor does it mention poisonous substances or medicines, as was also usual.

Comment

It should be clear from the foregoing description of contents that K. al-Mi'a is a large, comprehensive work which attempts to systematise the whole of medical theory. The major part of the book is devoted to theoretical considerations, and only a small part deals with practical procedures. There are no quotations from other medical authorities, a practice common to many kunnāshāt, where a quotation from an Arabic or Greek physician was often added either to lend support to the writer's opinion or to provide additional information on the subject under discussion. There may have been other reasons also. The general style of the book is authoritative and it may be that the author's sense of his own authority made the inclusion of the sayings of others unnecessary. Be that as it may, it is easy to see why such scholars as Lectere and Sarten saw K. al-Mi'a as a model for 1bn Sinā's Canon. Its encyclopaedic range, extreme systematisation, and authority are indeed reminiscent of the Canon.

In a sense, it may have even been preferable to the Canon. For, the scholarship of the Middle Ages which was so inclined to favour rigid classifications and compact systems might well have welcomed the relative brevity of K. al-Mi'a. Furthermore, al-Masihi's book is written in a lucid and didactic manner that would have made it of the greatest use to the mediaeval pedagogic tradition. It is extraordinary therefore to observe that al-Masihi's encyclopaedia was not known to the Latin West.

This of course raises the unresolved question of why certain Arabic works and not others were translated into Latin. From the point of view of subject matter and form. K. al-Mi'a should have been ideal for the Latin mediaevalists. Its omission from their translations is difficult to explain. Of course, it is known that the bulk of translation from Arabic into Latin was carried out in Spain, and therefore the choice of material for translation must have been dictated in part by the availability of books in Toledo and other Spanish centres of translation. We do not know what efforts were made by the Latin translators, if any, to obtain books from elsewhere in the Islamic

^{67.} Such quotations have been of the greatest value to modern scholarship. For example, the al-Jazzār's hook, Zôd al-Musājir provided Daremberg during the last century with important fragments of Rufus' medical writings which be incorporated vito his Oenvies de Rufus d'Ephèss (ed. C. Daremberg and E. Ruelle, Pens, 1879). *Ali b. Rabban al-Taberi's Firdaws al-Juha (ed. by M. Z. Siddiqi, Berlio, 1928) contains a rich vanety of quotations from Greek, Arabic, and Indian sources Pacudo-Thábri's K. al-Dhakhira fi "dm al-Jubb, (ed. by G. Sobby, Cairo, Government Press, 1928), ulso transmits many quotations from others.

on the uterus and on pregnancy. This is followed by a book "on the treatment of diseases special to men" and concerns inflamations and ulcers of the genital organs. But it also includes something on what may be termed "sexual medicine". This is concerned with the ill effects of sexual over-indulgence and not with ways of increasing pleasure, as is to be found in the comparable sections of some other kunnāshāt.

The head-to-toe diseases end with goot and sciatica. The books after that are on external, or skin diseases. This includes the conditions affecting the hair such as alopecia and splitting of hair, and the disorders of the complexion like vitiligo, and the scars of smallpox and ulcers, as well as other skin diseases. Such a section on external diseases was a standard component of all kunndshāt. It also included a certain amount on cosmetics; such matters as the dyeing and curling of hair, the removal of unwanted hair and remedies for purifying the complexion and changing its colour. The external disease part of K. al-Mi'a, however, has very little cosmetic emphasis and no directions for the dyeing or curling of hair. Book 99 is on fractures and dislocations. It is a short chapter and describes the general treatment of the body when a fracture takes place; this consists of evacuation and blood-letting in order to prevent the seepage of humours from the fracture site. There are some directions on how to correct dislocations and fractures and on binding the affected part.

But it is unlikely that such brief directions as are given would have been of much use to an orthopoedic practitioner. What is more likely is that, as this was a routine inclusion for most kunndsh't, it was included here for the sake of completeness and does not necessarily imply that the author had ever practised any of the procedures he describes or that he intended them for practical purposes.

The last book is on another standard inclusion of kunnāshāt, namely, the bites of venomous animals: these include the snake, scorpion, tarantula, and wasp; there is also a chapter on the bites of rabid dogs, again a favourite subject with Arabic physicians. Snake and scorpion bites are treated, as might be expected, with the theriac, since theriacs were originally made up as anti-dotes, and it was only later that their use became widespread as universal panaceas. The book does not deal with the bites of large animals, such as lions.

^{45.} In Arabic literature, this phrase includes a number of related topics: the place of cortus in health; disorders associated with the performance of cortus such as impotence and primpism, genorthoes and nocturnal emission. The remedies in such sections often included numerous approximates. Some books added chapters with a strongly grotic flavour on such subjects as ways of increasing sexual pleasure and sexual positions.

^{46.} The theriacs were a group of compound medicines said to have been devised by the Greek physician, Andromachus, as antidotes against pousous of all types. By Galen's time, they were in use for other conditions as well, and later still, they became universal pausoceas. See G. Watson, Theriac and Matherdatum (London, the Wellcome Rictorical Medical Library, 1966)

For example:

"Book 65: The treatment of diseases occurring in the organs of sensation and motion, that is to say the treatment of spasm, tetanus, flaccidity, numbness, and tremor".

"Book 79: the treatment of gastric evacuations, that is to say the treatment of cholera, dysentery, and lientery".

In general, the head-to-toe disease section of K. al-Mi'a is relatively short and relegated to a place of secondary importance. All chapters on disease are short and contain a cursory account of causes and symptoms. This is unlike the practice employed in many kunnāshāt of the time, where the head-to-toe diseases were given a place of pre-eminence as being the main subject matter around which the other principal subjects of medical theory were arranged. The reason for this departure in al-Masihī's book is evident from the fact that he devotes considerable space to the theoretical principles underlying the causes and mechanisms of disease, symptoms, and therapy. Hence, when he comes to the description of actual disease entities, he is very brief on their specific features, having already explained their general characteristics at length.

The account of epilepsy is a typical illustration:

$$(f. 282, 1.4 - 1.11)$$

قد يكون من آمة مخصوصة عائداع ويكون من مشاركة المعدة وبعمن الإطراب كالرجل او اليد او مشاركة الرحم لحساه بأن يصمد من كل واحد من هذه الإعصاء ما يسد ساهد بطول الدماع علمات الصرع عام كان يصمد من بعض الاطراف فيسمي في وقت النوبة قبل ظهورها أن يشد مون ذلك ددوسع برماءد شدا محكما الى أن شقطع النوبة ثم يظل دوضع بالفقط والحرفان والمعرفيون وصل البلادر ويبرك حتى يستمط

"(Epilepsy) may occur from a maledy specific to the brain, or it may occur in association with the stomach and some of the extremities, such as the leg or the hand; or because of association with the womb in women. Thus, something ascends from each of these organs which obstructs the apertures of the ventricles of the brain and so epilepsy occurs. If it ascends from one of the extremities, it will be necessary at the time of the fit and before it happens to bind (the part) above that place with a firm, tight bandage until the fit is stopped. Then the part should be painted with pepper, castor, euphor-bium, and anacardium honey, and left until it blisters".

It will be readily seen that there is no clinical description here. The rest of the chapter is concerned with therapy, which is given in some detail.

The list of diseases described goes down through the body in descending order. After the books on diseases of the urinary tract, there is a short section

significance, (this is to be differentiated from prognosis, which is the subject of book 54), the periods of disease meaning the four stages of disease as classified by Greek and Arabic physicians' commencement, increase, culmination, and decline; and the three cornerstones of mediaeval disease theory: coction, crisis, and critical days. The subjects are dealt with in characteristically detailed and lucid manner, and the accounts are exactly in line with the earlier Greek teaching and with the other Arabic books on the same theme

There are three books on the preservation of health. These include the healthful regimen to be adopted at various ages. Attention is to be paid to the diet, sleep, movement and rest, baths, massage, psychical events, and the ambient air - in other words, to the six non-naturals. This matter was a regular component of Arabic kunnāshāt, and was also treated as a separate subject, as the many Arabic tracts on hygiene testify. Book 59 is on the principles of the treatment of diseases, and contains a clear statement of the physician's function with regard to disease and its management:

فالطبيب فاعل كالممين الطبيعة بأنا يقرب منها الدواء وعبر دامن داخل أو حدرج على ما ينبعي في الوقت والمقدار فهو يحصر المحصولات ما تتقوى به فتستمين به في دفع المرض ولدلك صارت اطبيعة قد تعلع وتريل كثيرا من الأمراض من دول دواء أو طبيب ولسن يقدر الدواء والا الطبيب يوالة المرض البتة مني حارث القوة وهجرت

"The physician acts as an assistant to nature, in that he brings to it medicine and other things either internally or externally, in the correct amounts and at the correct times. For he sids (nature) to attain what strengthens it and assists it in repulsing the disease. In this way, nature repulses and eliminates many diseases without either medicine or physician, nor can either medicine or physician eliminate a disease once the strength has collapsed and become impotent".

Thus, here is a clear adherence to the Hippocratic attitude with regard to the importance of nature and to its standing as the real physician. There is then a detailed and highly systematic account of the things which have to be taken into account when deciding on the correct treatment. It is only at this point in the work that practical directions as to the management of specific diseases are given, but even then, there is little emphasis on therapeutic detail. The next series of books represent the head-to-toe disease section of the book. There is an unusual tendency to classify some diseases according to functional and pathological considerations rather than on the basis of pure anatomical site.

44. Queță b. Luqu, Ishaq b. Imran, the Sina, Ibe al-Mulran, and many others wrote seperate tracts on hygiene.

The function of air is to be a cooling agent for the heart, which is conceived of as a furnace wherein the innate heat burns. The lung therefore acts as a bellows to cool the heart. Thus,

(f. 216b, 1.10 - 1.14)

"The lung expands and contracts with the expansion and contraction of the chest. When it expands, its cavities fill with air, and when it contracts, the smoke of the heart which has been expelled to it is expelled to the exterior. For respiration is the means whereby the heart obtains the sir with which it is fanned and (hence) its heat remains moderate and pure, and from which is created the animal spirit by whose agency the life force and the innate heat reach the rest of the body".

These ideas on respiration are very similar to the ideas expressed by Aristotle and Galen, in particular the concept of the bellows and the burning furnace wherein combustion takes place, and hence the need to expel 'the smoke of the heart'.'3 The next 9 books deal with 'pathology', for they concern the pulse, the utine, and facees, and their features in health and disease.

The book on the pulse is complicated and detailed. Pulse lore was a most important aspect of the Arabic medical system. Arabic physicians routinely described 10 kinds of abnormal pulse. These went under certain names, such as the "mouse-tail pulse" and the "gazelle-like pulse", and their patterns were intricately described. This seems to have been a theoretical artifice more than anything else, and it is doubtful whether anyone actually ever felt most of what was described. Of no less importance was the subject of the urine. Al-Masihi goes into the matter of uroscopy at length and in great detail, with great emphasis on its pre-eminence in the art of medicine. He explains how urine is formed from the watery part of blood and stresses that its examination will give information about many internal conditions. The different kinds of pathological urine are described, which, like the kinds of pulse, were common to all Arabic medical writing.

The following books deal with several important subjects: on the auticipation of illnesses by warning signs, which was a review of signs of prognostic

⁴³ There is a similar description in Aristotle's De Respiratione, transl by W.S. Hett, Loch Classical Library, (London, Hememann, 1957), p. 479, and at greater length in Galen's On the Usefulness of the Paris, ep. cis., 1, 316.

latter survives only in Arabic translation.41

The subsequent books have detailed discussions on the signs of psychical ailments, on secretions evacuated from the body, and on fevers. The book on fevers is devoted to the theoretical understanding of the nature and differentiation of fevers. He defines fever as a contranatural heat; the site of this heat in the body determines the type of fever it is, as follows:

(f. 194a, 1.15 - f. 194b, 1.2)

فشى كانت في لارواح كانت حتى يوم رهي سقفي ادا في يوم واحد وإدا في نوبة واجدة إن يقست ا اكثر س يوم واحد ومنى كانت في الإخلاط كانت حتى المقوية وحتى المقوية مبا ذئم، وهي التي مادي، محصورة في الدروق ومنها دات افتراق وأو بب وهي التي ماديها حارجة عن ندرول ومنى كانت في الأعصاء كانت حتى الذق

"When the heat is in the spirit, it is an ephemeral fever; it goes either in one day or in one paroxysm. If it stays for longer than one day, and when (the heat) is in the humours, then it is a putrid fever. Putrid fever may be continuous, and that is when its matter is confined to the veins, or it may have periods and paroxysms, and that is when its matter is outside the vein. When (the heat) is in the organs, it is a hectic fever."

His account of fevers follows this pattern and makes the subject, which must have posed the physician of the time the greatest diagnostic difficulties, seem simple and straightforward. Book 41 is on the signs of diseases of various parts of the body. The next book gives an account of the signs of the temperaments. This describes the signs of a hot, cold, wet, dry temperament, and compounds of these (i. e. hot-dry, cold-wet, etc.), and how the temperament may be diagnosed from the colour, the facial expression, the touch, and the actions. The temperaments of organs are also included. There is a section on the indications from the facial features, the teeth, the nails, and the skin as to the temperament (for example, a hairy chest indicates a hot temperament of the heart). This science, (physiognomy, Arabic: al-firāsa), was a most important subject in Arabic medicine. Al-Rāzi has a large section on it in his K. al-Manṣāri, and several Greek works on the subject were available in Arabic translation from the time of Hunayn b. Ishāq. 43

Book 44 is on respiration and forms a compact and interesting account of the physiology of respiration of the time. There is a reiteration of the doctrine of spirits and a discussion of their entry and elaboration in the body.

^{41.} This tract has been translated from the Arabit by M. C. Lyons as On the Cohesine Couses, in Corpus Medicorum Grantorum Supplementum Orientale, 11, (Berba, Akademie-Verlag, 1969).

^{42.} Notably, the book on physiognomy of the Greek cophist, Polemo, which survives only in Arabic translation as K. Istimus fill-firesa. The material here is very similar to that in K. at Mi'a.

and uring are also listed here. Book 32 continues an account of drugs classified according to their qualities, degrees, and special effects, that is, under "heating medicines in the first degree", there follows a list of substances; under "those medicines which attract the humours", another list of substances, and so on.

Book 35 discusses the classification of discases, their causes, and their signs. As if by way of introduction, al-Masīḥī explains something of the nature of all diseases:

وإن الأمراض واسباب واعراضها كيها أمور حارجة من الطاح وعرض صدعة الطب هو ارائها كمهة عنى القصد الأول قات الذي يقصد إلى ارائته او لا هو المرض لأنه هو الذي يضر بالفدن إلا أنه لا يرول الأ يروان السبب الذي تحدثه

"Diseases, their causes, and their symptoms are all contranatural matters. The purpose of the art of medicine is to remove them all, in order of priority. For (although) that which it is intended to remove first is the disease, because it is what is harmful in fact, (yet) it will not be removed unless the cause which has brought it about is removed (first)".

There then follows a classification of diseases according to the four primary qualities with examples to illustrate each type, and according to the compounds of the primary qualities, and whether these are accompanied by matter or not. As to the causes of disease, he classifies them and explains these in this way:

وأساب الإمراض ثلاثة احتاس احدها حسى الإسباب النادئة والثاني حسن لأسباب السابقة والثالث جسس الإحباب الواصعة والإساب النادئة هي التي تؤثر في المدن وهي حارجة عمد صل حرارة الشبس القوية التي تولد الحمى واما الإساب التي تؤثر في البدن من داخل هما كان بينه ودن المرض سبب آخر فهو سب مابق وما كان منها ليس بينه وبين المرضى سبب آخر فهو سبب واصل

"The causes of disease are of three kinds: the first is that of the immediate causes; the second is that of the antecedent causes; and the third, that of the connecting causes. The immediate causes are those which affect the body (but) are external to it, like the strong heat of the sun which gives rise to fever. As to the causes which affect the body from inside, if there is a connection between them and the disease, then it is an antecedent cause. But if there is no (causal) connection between the disease and one of them, then that is a connecting cause"?

This classification is in fact very similar to the Galenic classification of the types of causes, as explained in his tract De Cousis Contentius. The

Books 30 to 34 are concerned with the faculties of medicines and their classification. The subject of medicines was of the utmost importance to mediaeval physicians. Here is a clear exposition of the theoretical approach to the use of medicines in terms of their qualities and their special actions, whether purgative, diuretic, emetic, and so forth. The author encourages the use of "empirical medicines", (mujarrabāt), but stresses that where possible, only one drug should be used at a time. These mujarrabāt are of some interest; many books were devoted to this subject during the Arabic period, including those by al-Kindī, al-Rāzī. Ibn Sīnā, Ibn Zuhr, Ibn sl-Tilnidh and many others. Sarton¹⁷ was very impressed with the tradition of mujarrabāt, and held that it represented the earliest example of an experimental method in medicine. But in fact, the mujarrabāt were nothing to do with the experimental method but were rather medicines which had been found to work by experience. Many of them had obvious magical associations, particularly in the later writings of the 14th century and onwards.

The book on simples classifies them in alphabetical order, using the earlier type of Arabic alphabet (which follows the Hebrew order). Under each medicinal herb, there is a definition of its properties according to degrees from 1 to 4. Thus, a medicine is described as 'cooling in the first degree' and drying in the fourth degree,'. Its special effects and properties, diuretic, purgative, binding, etc. are then listed. For example,

"Opum is cold in the fourth (degree), dry in the second; efficacious m hot, inflamed swellings, especially of the eye; causative of lethargy, anaesthetic; a small amount of it is efficacious in stilling pain and for narcosis; a great deal of it kills."

This system of degree classification was a refinement of the Galenic arrangement whereby drugs were graded according to their qualities and their efficacy. The Arabic physicians broadened and expanded Galen's ideas into a neat and well-ordered system. Parts of animals are also included here as substances with medicinal properties, as for example with the livers of certain animals, which are used as sympathetic medicines in diseases of the liver. The gall, tongues, and secretions of animals, such as their saliva, milk,

^{37.} Sarton, op. cit., \$1, 94.

³⁸ In this, one must agree with Ullmann who takes usue with Sarton in his special section on majorrabil. (Die Medizin, op. cit., pp. 311-3).

³⁹ For a study of the Galenic system of drug classification, see G. Harig, Bestimmung der Intensität im medizinischen System Galens (Berlin, 1974).

^{40.} Al-Majusi devotes a large section of his book (op. cir. above) to this classification of drugs.

al-Mansūri, is almost identical), ³¹ to the extent of repeating Galen's erroneous assertion that there were communications between the right and left ventricles. It was this assertion which was countered by Ihn al-Nafīs two hundred years later, and which earned him the enthusiastic description of "the discoverer of the pulmonary circulation" by certain modern writers. ³⁴ The next book is also Galenic in concept, for it contains a teleological account of the function of organs on the lines of the large work of Galen, On the Usefulness of the Parts of the Body. ³⁵ There is much useful information in this book on the physiology of the time, and a remarkably clear exposition of the role of the vital heat and the elaboration of the animal spirit.

The books that follow may be said to be about the environment on airs and winds, on dwellings, and on waters. Books 12 to 18 inclusive are on dietetics: the principles governing the choice of food and drink which are connected with a study of the temperament, the season, and the preponderant humours; the faculties and qualities of simple foods; and the benefits and properties of wine and other drinks. Book 16 deals with the healthful preparation and cooking of food, and explains that foods are classified as digestible, indigestible, high in superfluities, or low in superfluities, and the like.

The next few books deal with the non-naturals. On the subject of evacuation, there is a lengthy book devoted to blood-letting, its advantages and disadvantages, the indications for blood-letting, and how much blood to remove. It ends with a detailed and fuscinating account of the technique of blood-letting, what instrument to use, what shape incision to make, whether along the length or width of the vein, and what to use to keep the vein patent. Al-Masīhī's contemporary in Spain, Abû'l-Qâsim al-Zahrāwi, also left a long and detailed account of the technique of venesection and its indications. Book 29 is on the signs of psychical origin, such as grief and anger. The observation is made here that anger leads to a yellow complexion, due to an increase in yellow bile. This brings to mind the use in this connection of the English word "choleric" and its obvious humoral origin.

³³ For comparison see Calen's description of the heart in his On Anatomical Procedures, transl. C. Singer, Wellcome Historical Viusenin Publications. (Oxford University Press. 1956), VII.175, 179-188. The anatomy of the heart is given in magala I of the K. al-Manyari. "On the form and appearance of organs".

^{34.} See M Meyerhof, "The al-Nuffs (XIIIth century) and His Theory of the Lesser Circulation" Isis, 23 (1935), 180-20.

^{35.} Transl, by M. T. May, Cornell University Press, 1968.

^{36.} Albucasis on Surgical Instruments, ed and transl by M. S. Spink and G. L. Lewis, (London, Wellcome Institute for the History of Medicine Publications, 1973), pp. 624-655 (on veins), and pp. 174-163 (on afterios).

This extract displays the general style of the book quite well. It also reveals the neat systematisation typical of Arabic writers. This economy of description of the faculties should be compared with the prolixity and disorganisation of Galen's work on the same theme. On the Natural Faculties. 11 The other books on the temperaments, the actions, and the spirits are just as well-ordered and provide a thorough review of the principles of medical theory in readily assimilatible form.

The two books on the like and unlike organs constitute the anatomy section of the work. These terms refer to the classification of the parts of the body into those whose constituents are homogenous, such as fat, bone, cartilage, and so on, and those which are made up of different tissues, such as arms, logs, hands, and so on. This division was common to Arabic anatomy, and derived from an Aristotelian classification of the organs of the body into 'homomerous' and 'anhomeomerous' types. The unlike organs are classified from top to bottom, in the same way as diseases, and in fact represent the internal organs. The anatomical descriptions are exact, as for instance this extract on the heart:

(f. 21b, 1.6 - 1.12)

وانقب صوري الشكل قاملة لى حهة عالي الدن ورأسه المحروط ان جهة أساس البدن وقاعدة القلب موضوعة في وسط الصدر ومن حسيم حهاتها ورأسه المحروط مائل إلى ناحية اليسار والقلب علاق من عشاه كشف محيظ به تشيرا منه إلا صنه فاعدته وفيه تحويمان احدهما في احاب الايمن والأحر في الممانات الأسم وفي التجويف الأيمن الدم أكثر من الروح وفي لأيسر الروح أكثر من الذم ومن لايمن في الايسر منافذ بليفه.

"The heart is cone-shaped, its base being towards the top of the body, and its pointed and towards the lower part of the body. The base of the heart is in the middle of the chest (equally) on all its sides, (but) its pointed head is inclined towards the left side.

"The heart has an envelope made of a thick membrane, which surrounds it but is distinct from it (i. e. not adherent) except at its base. It has two cavities, one on the right side and one on the left. There is more blood than spirit in the right cavity, and more spirit than blood in the left. There are small apertures from the right to the left (cavity)"

This description is interesting in more ways than one. It is modelled on Galenic anatomy, like other Arabic books of the time, (for example, the section on the anatomy of the heart in al-Rāzī's famous kunnāsh, K.

³¹ Translated by A. J. Brock, Lond Classical Library (London, Hernemann), 1928.

^{32.} Cf Aristotle. De Partibus Animalium, 646b, 11-20, in The Works of Aristotle, ed and transf. by W.D. Ross (Oxford University Press, 1910-49). This section includes a discussion on the "homeometrics" parts.

black humour go beyond the nature of blood, because they have reached the limits of combustion. The presence of all these in the body is normal, meaning that blood is the true nutrition that is intended and phlegm is a humour which could be digested so that the body could be nourished by it".

And still on the subject of humours, al-Masihi explains how it is that they cause disease:

"These are the humours which are called the fundamental components of the body. But if they increase over their (normal) amount or their qualities, they become contra-natural due to a pathological cause. It is (then) necessary to bring (the body) back to a state of moderation if (the humours) are in excess in their qualities, and to evacuate it if they are excessive in amount."

In this brief extract, he enunciates the principles of disease causation and therapy which were the essence of the humoral theory followed by himself, his contemporaries, and the Greek physicians before him. As to the other aspects of the humoral theory, the faculties are explained in a systematic manner:

فان للبدر اربع ثموى احداه بصاحبة وهي التي تعمل الاحساس والتعبر والتحريث بالاحتيار والثابة حبراية وهي تعطي حميع البدل الحياة والحرارة العربيرية والتالثة طبعية وهي التي تعطي حماح الناب العداء وتمدع مضولاته والريعة مولدة وهي التي تمد الزرع وتكمل الحس وقد تعد ي صناعه الطب القوة المولدة م القوة الفادية ويسمى جميع دقك الطبيعية

"The body has four faculties, the first is psychic and it is (the faculty) which effects sensation, discrimination, and voluntary motion. The second is animal and it is the one which gives life and the innate heat to the whole of the body. The third is natural, and it is the one which gives the whole of the body nutrition and which expels its superfluities. The fourth is generative, and it is the one which prepares for fertilisation and which completes the growth of the foctus. In medicine, the generative faculty is counted with the nutritive faculty, and the two together are called the natural (faculty)".

The first book is a highly theoretical and philosophical introduction to medicine. The second book presents a lengthy account of the theory of elements and how they enter into the formation of the human body:

$$(f. 6b, 1.17 - f. 7a, 1.12)$$

والاحسام الأولى بانظم اربعة النار والحواه والماه والارض وإعا سميت اجساما أول لاجه لا تتركب ولا تتكون من احساما أول لاجه لا تتركب ولا تتكون من احسام أحر عبرها والله من هده قد يكون إما اولا في المبي وإما من بعد ذلك في اللهم والمبي يتكون من اللهم والرمم من العداه والعداء إما حبوان وإما دائث والحيواب حال نديه كيمان بدن الانسان ودن كليه من الساب والسات يسكون من الارضى وأناه عادن ادن الانسان مركب من الاصطفاعات الأول .

"The elements in nature are four: fire, air, water, and earth. They were named elements because they are not constructed or formed from any other bodies. . . and the (human) body is made up of organs of like parts. Every one of these (organs) exists either in the semen first or in the blood after that. And the semen is formed from blood, and blood (is formed) from food, and food is either animal or plant. The state of an animal's body is like that of man, so, therefore, all of them come from plants; and plants are formed from earth and water. Therefore, the body of man is made up of the primary elements".

He goes on to define the qualities of the four elements as hot, wet, dry, etc. His style is clear, diductic, and detailed. The other sections on medical theory are likewise lucid. The book on the humours, for example, could not have left any student of the art in much doubt as to the nature of the humours in health and disease:

والاحلاط وهي ربعة الدم واحدط الأصفر والحلط الاسود والنص وحصولها كنها في البدن بسبب المداء على أن تخله عداء وهو الدم وبعلها قصولات الله وهي تثلاثة الاحلاط الراقية لأن البلم فلسلة متعدم على الدم لأن الله لأن الله الاسود مجاوران لطرحة الدم لاسهم قد الله الاسود مجاوران لطرحة قد سدرا في حد الاحلاق ووحودها كنها في الله للحلم على أن الدم عو الله الحقيقي المقلمود والبلمم علم عكن أن الدم عو الله مقيقة في به الله في .

"The homours are four: blood, the yellow humour, the black humour, and phlegm. They are all to be found in the body by reason of food, meaning that some of them are food, and that is blood, and some are superfluities of food; these are the three remaining humours, for phlegm is a superfluity which comes before blood because the food has not been digested and has not reached coction yet, so that it stays unripe. The yellow humour and the

and external diseases. The external diseases section here is subdivided into diseases of the scalp, the skin, and the skin colour. Two other topics, which were also very commonly included in medical compendia, although not uniformly so, appear: fractures and dislocations, and venomous bites. Several books are devoted to the subject of medicines both, simple and compound, matter of the highest importance in any medical book.

Subjects of Books in K. al-Mi'a

latroduction to medicine

The elements

The homeomerous organs
The anhomeomerous organs

The usefulness of the parts of the body

The humburs
The temperaments
The faculties
The actions
The apprica

The natural states of the body

Airs and werds Dwellings and waters

Feculties and qualities of foods

Dranks and wines Sleep and waking

Massage

Movement and rest

Barbs
Pargation
Emosis
Venesection
Discress
Peraparation
Gardina

Ciysters

The rigus of psychical origin (grief, soger, etc.)

Faculties of medicines

Simples

Medicines with special properties Causes and signs of disease Psychical ailments

Secretions evacuated from the body

The types of fevers

Swellings

The signs of discouss of various parts of the body

Respiration
The pulse
The surine
The facess

Premonitory signs Periods of disease

Coction Crisis Critical days

Pavourable and unfavourable signs

The represervation of health
Principles of treatment of diseases
The treatment of fevers

The treatment of fevers
The treatment of swellings
The treatment of sicers
Diseases from head to toe

Pregnancy and diseases of the sterus

Diseases special to men Diseases of the hair Sears of pleases

Disorders of skin colour Diseases of the skin

Fractures and dislocations

Bites of venomous aumale

are not properly organised, so that the divisions of the art are not known; there is either too much detail or too little; theory receives too little attention, while practical methods and therapy receive too much. For these reasons, the author has decided to write a book which will remedy all these failings in as synoptic a way as possible.

The result is an encyclopoedia of medicine in which everything is systematised as far as possible. It is organised on a basis of the standard divisions of medicine, (best expressed in Hunayn b. Ishāq's pithy introduction to medicine, al-Masā'il fi'l-iibb). To The descriptions are lucid, well-ordered, and there is indeed an attempt to make each book complete in itself. There is a strong emphasis on theoretical aspects, and indeed the major part of the book is devoted to theoretical principles and discussion. It is only when the 60th book is reached on f. 267b, that is, after two-thirds of the book have been gone through, that practical methods are included in any detail.

The index of "books" is set out soon after the introduction, Each section is named "the book of such-and-such." The subjects dealt with in these books have been listed on the following page. They do not correspond to the actual titles in K. al-Mi'o, where the same subject sometimes has several books devoted to it, but are meant here to convey a general idea to the reader of the contents of the kunnash. In this way, it may be seen that all the standard topics in medicine which were current at the time are covered; all essential aspects of the humoral theory, the naturals; which are the organs, the elements, the temperaments, the faculties, the actions, and the spirits; the nonnaturals, 29 which are six and which may be picked out among the list of subjects early on in the kunnash as air, food and drink, sleep and waking, movement and rest, evacuations (detailed into purgation, emesis, venesection, and the like), and the passions of the soul (the signs of psychical origin); and the contra-naturals, meaning the cause and process of disease. There is a section on 'pathology', that is, coction, crisis, the pulse, and the urine; a section on prognosis; and a section on the preservation of health. All these were standard subjects of importance which were included as a matter of routine in most kunnäshät. Likewise, there is the inevitable classification of diseases from head to toe, 30 and the other two classical subjects, fevers

^{28.} This work, alternatively known as the Isagaoge, was celebrated throughout the Middle Ages. It is actout in a question-and-answer form and aummarises the medical theory of the time using a tigid classification of subject matter which became standard for all medical books thereafter (This important work is still unedited and exists only in manuscript form.)

^{29.} There are several studies on the non-naturals. For example, P. H. Neibyl, "The non-naturals", Bull. Hist. Med., 45 (1971), 486-92, and L. J. Rother, "The six things won-natural, a note on the origins and fate of a doctrine and a phrase", Cho Medica, 3 (1968), 337-47.

^{30.} This was a classification that was universally employed in Arabic medical textbooks and in the Greek medical books of late antiquity.

well written, and provided a wide selection of treatments ¹² It was recommended for use by students in the medical teaching syllabus of the Chahār Maqāla, as was noted above Modern commentators have also been impressed with this book; both Leclerc and Sarton believed it to have been a model for Ibn Sīnā's Canon. ²³ The book survives in at least 29 manuscript copies. The earliest of these is said to be to be dated 400/1010, which, if true, means that it must have been made either during the author's lifetime or shortly after his death. ²³ There are six other early manuscripts, that is, dating from before 1300 A.D. ²⁴ In the centuries that follow, there are manuscripts dating from each century, and a high concentration of very late manuscripts: five are said to be dated between 1233/1818 and 1300/1883. ²⁵ Thus, manuscripts survive from every century beginning virtually from the date of death of the author until the end of the last century This, and the large number of surviving manuscripts is impressive evidence of the popularity and importance of the book.

In the account that follows, only the briefest summary of the book's contents has been given, for it is such a large and comprehensive work that it could (and should) form the subject of a much langer study.

Contents of K. al-Mi'a

K. al-Mi'a is a large work: the British Library manuscript, on which this study is based, contains 376 folios of small script.*6 It is divided into a hundred chapters or "books", (hence the title), and, as the author says in his introduction, each is meant to be a complete work of its own, not dependent on the others for its understanding. The introduction is long and contains an analysis of the problems which beset the writing of medical books:*7 they

- 21 This information is supplied by IAU. 1 328. Amin al-Dawla b al-Tilmidb was a distinguished physician of the 12th century. (d 1165), who was chief physician at the "Adudi hospital in Bagbdad. (For his biography, see IAU. I, 259-76).
 - 22 Lectere, op. etc., I., 356-7; Sarton, op. etc., 1, 678.
- 23 This MS., Istanbul. Nuruosmanye 3557. is described by Dietrich, (A. Dietrich, Medicinalia Arabica, Gottugen Vandenboeck and Ruprecht, 1966, p. 70). The dating is only presumptive.
- 24. The manuscript citations for these are to be found in GAL, 1, 238, SI, 423; and Sergin, op. ct., 111, 325-7.
 - 25. The most recent is MS. Tehran, Danishkada-i Pinishki, 247/1.
- 26. This is MS. Or 6489. It is deted (on f. 194a) as 1105 A. H. (1694 A. D.) and is written in clear, good naskly. It is well preserved but part of the introduction is obliceated and some of the folios of obapter 99 on fractures and dislocations are missing. (See also S. Hamannel, Catalogue of the Archic Manuscripts on Medicine and Pharmacy of the British Library, Cairo, "Les Editions Universitaires d'Egypt", 1975, pp. 88-90).
- 27. This was a common format for introductions to compendia of medicine. There was always some fault with the others which the anthor had decided to rectify in his book. A lengthy critique of other kannāshāt, both Greek and Arabic, is to be found in the introduction to al-Majūst's Kāmil.

b. Muhammad (992-1009). (the father of Abū'l-'Abbās Ma'mūn b. Ma'mūn mentioned above). Al-Bayhaqī 12 also links al-Masībī with this ruler, for he says that the patron of al-Masībī was the king of Khwārizm, Ma'mūn b. Muḥammad, to whom he dedicated another of his works, K. Ta'bir alra'ya ("the interpretation of dreams").

As to his dates, there is the usual difficulty with determining these exactly Wüstenfeld, 14 who describes him as the teacher of Ibn Sinā, gives his date of death as being around 390/1000, though on what evidence is not clear. Sarton 15 gives a similar date, saying that al-Masīhī died aged 40 in 999-1000. Leclerc, 16 likewise, puts his date of death at 1000. (It should be pointed out that all these authorities, presumably following Ibn Ahī Usaybi'a, state that al-Masīhī was Ibu Sīnā's teacher). Brockelmann, 17 however, gives the later date of 401/1010, as does Ullmann, 18 Sezgin 18 cites a manuscript of one of al-Masīhī's works which is dedicated to Abū'l-'Abbās Ma'mūn (1009-1017). If this is indeed the case, and the book was not in fact dedicated to his father (as noted above on the authority of al-Bayhaqī), then the later date will have to be accepted. It is certain at least that al-Masīhī was alive in 1002, for it is known that Ibn Sīnā dedicated a missive to him from Jurjān is that year. 20 From this information, all that can be said is that al-Masīhī was alive in 1002 and died some time after 1009.

Kudb al-Mi'a fi'l- Tibb

Seven works of al-Masilii's survive: the best known is K. al-Mi'a. It was considered by the famous physician Ibn al-Tilmidh, who wrote a gloss on it, to have been of the greatest value because it was exact, not repetitious,

- t3. Zahīt al-Din al-Hayhaqi, To'rikh hukumā' al-Islām, ed. M. Kurd 'Alt, (Damascus, Maţba'at al-Țangi 1946), pp. 88-9.
- F. Wüstenfeld Geschiehte der arabischen Aerzie und Naturforzeher, (Göttingen, 1840), p. 59,
 No. 118.
- 15 G. Sarton, Introduction to the History of Science (Baltimore, Williams and Wilkins, 1927-48), I. 678.
 - 16. L. Leclere, Histoire de la Medecine Arabe, (Paris 1876), 1-356-7.
- 17. C. Brockelmann, Geschichte der grobischen Litteratur, (benceforth. GAL) and Supplement (henceforth. S), (Laiden, Brill, 1937-42), I, 238; SI, 423.
 - 18. Ullmann, op, eit., p. 151.
- F. Sezgin, Geschichte der grabischen Schrifttums (Leiden, Brill. 1967), III. 327, No. 6, Risälu fi tahqiq eti al-misäj mä husoo isa kam aynafuhu, MS. Shehid Ali. 2095/5.
- 20. IAU, II, 19, 1.10-11, lists this among Ibn Sinā's works. "A missive to Ahû Sabl al Masihi on the angle, which he wrote in Jurjân" It may be calculated from Ibn Sinā's autobiography, (The Life of Ibn Sina, ed. and transl. by W. E. Gohlman, (State University of New York Press, 1974), that he was in Jurjân in 1902.

He describes him as a "practitioner" (al-muta(abbib) and a logician (almantiqi), presumably implying by the latter description that he was interested in or had written works on logic. He wrote a famous kunnásh called al-Mi'at magala (more usually known as Kıtâb al-mi'a fi'l-tibb). He died "in middle age" at the age of 40. Ibn Abī Uşaybı'a is able to give more information about him: he praises his skill as a physician and his great learning and stresses his fluency and excellence in the Arabic language, which he wrote with a beautiful band. Ibn Abi Usaybi'a says that he examined a copy of al-Masīhī's book. Fi Izhār hikmat Allāh ta'āla fi khalq al-insān ("On the Revelation of God's Wisdom in Creating Man"), written in his own bandwriting, and was impressed by its excellence of grammar and linguistic precision. He goes on to report what Shaykh Muhadhdhab al-Din 'Abd al-Rabim b. 'Ali said of al-Masibi: he had never known any Christian physician, either ancient or modern, who could express himself as well as al-Masihi. (All this implies that al-Masihi's first language was not Arabic, and since he was a Christian, his mother tongue might well have been Syriac; it also implies that Christians in general did not know Arabic well). Then, Ibn Abi Uşaybi'a says that al-Masihi is said to have been the teacher of Ibn Sina in medicine, and that the latter became proficient in this and in philosophy at his hands, such that he dedicated several books to him.

It is not by any means certain that al-Masihi was indeed Ibn Sinā's teacher. Ibn Sinā himself asserts in his autobiography that he had no teachers in medicine, not that that necessarily rules it out completely. But al-Qifti makes no mention of this claim either. The two men are, however, connected in the Persian 12th-century work, the Chahār Maqāla, where the story is recounted that when both of them took flight from the court of the ruler of Khwariam Abū'l-'Abbās Ma'mūn (1009-1017), they were overtaken by a sandstorm in which al-Masihi died. The Chahār Maqāla extols the virtues of al-Masihi and calls him the successor in philosophy to Aristotle. His book, Kitāb al-Mi'a, is recommended as part of the syllabus for medical students.

Ibn Abī Usaybi'a provides a list of al-Masīhī's books. He begins with K. al-Mi'a fi'l-tibb, considered to be the hest and most famous of his books. There are three other titles of books on medicine, three on philosophy, and one book, Fi'l-Wabā' which he dedicated to the ruler of khwarizm, Ma'mūn

Al-Qifti, Ta'rikk al-hukamā', ed. J. Lippert, (Leipzig, 1903), pp. 408-9.

^{8.} IAU, 1, J27-II

^{9.} Al-Qifti, op.cit., p. 414

^{10.} Ibid. p. 408.

N.zami-i 'Arudi. Chehár Magala, ed. and transi. by E. G. Browne, (Cambridge University Press, 1921), pp. 86-9.

^{12.} Ibid. p. 79.

included sections on medical theory, that is: the nature of humours, temperaments, crisis, coction, and so on Diseases were described in a stereotyped way: cause, symptoms and signs, and therapy. The therapy section was usually the biggest part and often included a number of prescriptions. They also included a section on external or skin diseases, and a section on fevers. Many of them, but not all, also added a usually brief chapter on fractures and dislocations. Many of them also had a section on simple and compound drugs, and on poisons of animal origin or otherwise, and many books included a section on the preservation of health.

Kunnāshāt were used for practical purposes as manuals for medical practitioners and also for the teaching of practitioners and medical students. The relative emphasis on these two functions varied from one kunnāsh to another. For example, some kunnāshāt were no more than pure manuals of medicine, written in a simple, condensed style with a great deal of detail on therapeutics and very little on medical theory; this type was obviously of use to the practitioner. At the other end of the spectrum, was the type of kunnāsh which laid specific emphasis on medical theory, perhaps at the expense of detail on practical procedures, and which favoured a more complicated, intellectual approach; such kunnāshāt were useful for teaching purposes and could also be read by the intelligent and educated layman. Abū Sahl al-Masīhī's kunnāsh entitled Kitāb al-mi'a fi'l-tibb ("The Book of the Hundred on Medicine") is an example of the latter sort.

The study which follows is based entirely on manuscript material, for this worthy and elegant book has never been edited in whole or in part. The 13th-century writer, Nu'mān b. 'Alī al-Rida al-Isrā'ilī, composed a synopsis of it which was edited by Sharafī in 1959.' Despite its prestige and popularity (see below), it was never translated either into Latin or into a modern language. Neither, for that matter, were any other of al-Masīḥi's books.

Abu Sahl al-Masiht's Biography

Abū Sahl 'Isā b. Yaḥya al-Masīḥī al-Jurjānī was, as is revealed by his name, a Christian and a man of Jurjān in Persia. Al-Qiftī says that he was learned in the sciences of the ancients, and famous among his countrymen.

^{4.} This is made clear in the introductions of many of these books, wherein it is stated that both practitioner and student will be easi from the book; a typical example is Ibn al-Jaszán's introduction to his book, Zád al-musajár va que al-hádis.

^{5.} Such a book is the Butlan's Kunnash al-rubban we'l-adyrra, which is a simple manual of diseases and their treatments.

^{6.} Qadri Sharafi, Al-Hawaiki al-nu-maniyya wa'l-maqasad al-fibbiyya, (Hyderabad, 1959). (I have not seen this work). There is a manuscript of the synopsis at the Bibliotheque Nationale, no. 2883.
See M. C. de Slane, Bibliothèque Nationale, Catalogue des Manuscrite Arabes (Paris, 1883-95), p. 518.

A Mediaeval Compendium of Arabic Medicine: Abu Sahl al-Masīhī's "Book of the Hundred"*

GHADA KARMI**

Introduction

The kunnāsh¹ (or compendium) type of book was very popular among Arabic physicians of the mediaeval period and became the commonest form of medical book to be written. It was supposed to be a comprehensive system of medicine in condensed form, so as to acquaint the reader with all the essentials of medicine without overloading him with too much detail. Many kunnāshāt declared this to be their explicit aim to their introductory remarks.¹ As time went on, the kunnāsh became the preferred type of medical work, to the despair of such educational purists as Ibn Ridwān who strongly deprecated the substitution of these derivative works for the original works of the ancients.²

These books were not identical either in arrangement or in content, but they resembled each other in certain important respects: they all included at some point a section on diseases arranged from head to toe; many also

- * Grateful acknowledgement is due to the Wellcome Trust for the History of Medicine which supported the research for this paper
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- 1 The word kunnāsh is sutcreating. It does not appear to be of Arabic derivation, but comes from the Syriac kunnāsha (M. Ulimanu, Wörterbuch der klassischen arabischen Sprache, Val. I (Wiesbaden, 1970), p. 587, 20 A.
- For example, "Ali b. al-"Abbās al-Majūsī (fl. 949-982) writes in the introduction to his kunnāsh, Kāmil al-yīnā"a al-jibbiyya (Cairo, Bulaq, 1294/1877). Vol. I, p. 7, 1 28f, that he has composed his book.
 - "That it might be easy (for physicians) to find one book which contains sil that is necessary (in merheine). I will not leave out anything that might be needed by students and learned scholars."
- 3. Ibn Ridwän was an lith-century physician of Cairo (d.1961) who took a great interest in the medical education of his day For his biography, see Ibn Abi Usaybi'a, "Uyūn al-anbā' fī fabagāl al-afibbā", (henceforth IAU) ed. A. Müller, (Köngsberg, 1884). He wrote a tract on this subject, al-Nöfe fi ksyfkyyat ta'līm yinā'ai al-jibb ("the useful book on the quality of medical education"). The relevant extract is quoted by A. Z. Iskandar in his, "An attempted reconstruction of the late Alexandrian medical curriculum", Med. Hist., 20 (1976), 241

One wonders whether the kunnāsh type of book was not always preferred, almost from the beginning of the translation movement from Greek and Syrac into Arabic. Kunnāshās in Syriac were certainly available before 700 A. D. and came to be written in Arabic from 800 A. D. onwards.

et se l'approprie. Déchaînement d'al-Sijzī qui l'attaque alors avec la dernière véhémence, sans toutefois le nommer. Entre temps al-Qūhī et al-Saghānī étaient entrés en lice et donnaient leurs solutions en 360 H., semble-t-il, celle d'al-Qūhī étant la plus élégante de toutes et autérieure de peu à celle d'al-Saghānī.

La construction de l'heptagone régulier restera une des grandes questions classiques: al-Qühī en fera l'objet de son deuxième mémoire, Ibn al-Layth en donnera une 2° solution (dans sa 3° lettre). Celiu-cj est devenu depuis un géomètre réputé dont al-Birūnī et 'Omar al-Khayyam feront l'éloge." Ibn al-Haytham donne une solution entre 417 H. et 429 H 1° Al-Bīrūnī évoque l'heptagone dans "al-Qānūn al-Mas'ūdī, al-Samaw'al b. Yaḥyā dans Kashf 'uwār al-munajimin.' L'heptagone donna l'élan vers d'autres tentatives; construction de l'ennéagone régulier, construction du polygone régulier de 11 côtés (qu'Ibn al-Layth crut avoir trouvée), du polygone régulier de 13 côtés, division de l'angle en 5 parties égales. Il reste un des multiples témoins de la faveur que la géométrie a connue dans la 2° mortié du 4e siècle, époque où l'on peut voir la première gestation de l'algèbre géométrique d'Omâr al-Khayyām.

^{9.} Al-Birduf, Al-Qónūn al-Mas adī, (Hyderabad, 1954), vol. 1, p. 297 Al-Khayyām, Al-jabr w'al-muqābala Ms. Columbia Univ. Or. Smith 45, 10, pp. 28, 37.

^{10.} Iba Abî Uşaybî"a, "Uyün al-anbā", (Cairo, 1882), vol. 2, p. 98.

^{11.} Al-Biruni, stud p. 297 Al-Semaw'al b. Yahya, Kashf 'usoir al-munagemin, Me Lesden Or.

^{12.} Al-Qānīn al-Mas'ūdī, vol 1, p. 287; von aussi al-Rosā'il al-mutafarrigo fi-l-hay'a (Hyderabad, 1948), 10, p. 22.

^{18.} Al-Samaw'al b. Yuhya, op. cit. f. 21

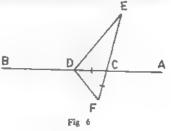
4 Construction du triangle ABD tel que $\widehat{B}=2\widehat{A}$ et $\widehat{A}=2\widehat{D}$ et par suite division du cercle en sept parties égales.

Méthode d'al-Qühi (1er mémoire)

La division d'un segement AB arbitraire en C et D de sorte que $CB \cdot CD = A\overline{C^4}, AD \cdot AC$ $\overline{DB^3}$ a donc été opérée. Al-Qübi a démontré aussi que chacun des segments BD, DC, AC est inférieure à la somme des deux autres. Il peut donc construire le triangle CDE où DE DB et CE - AC.

Je dia que $\widehat{ECD}=2$ $\widehat{EDC}=4$ \widehat{CED} . (Par suite si on circonscrit un cercle

au triangle CDE on aura la division du cercle en sept parties égales). Prolongeons EC en CF tel que CF = CD. On a $BC \cdot CD = \overrightarrow{AC^2} = \overrightarrow{CE^2}$ d'où $BC \cdot CE = \overrightarrow{CE} \cdot CE \cdot CD$. Les triangles BCE et \overrightarrow{DCE} sont semblables. D'où $\overrightarrow{B} = \overrightarrow{DEC}$ et $\overrightarrow{CEB} = \overrightarrow{EDC}$. Mais \overrightarrow{EDC} extérieur au triangle BDE égale 2 \overrightarrow{B} , donc $\overrightarrow{EDC} = 2$ \overrightarrow{CED} . De même $\overrightarrow{ECD} = 2$ $\overrightarrow{CDF} = 2$ \overrightarrow{CFD} . Comme $\overrightarrow{CE} = AC$ et $\overrightarrow{FC} = AD$ alors $\overrightarrow{AD \cdot AC} = \overrightarrow{FE \cdot EC} = \overrightarrow{DB^2} = \overrightarrow{DE^2}$.



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D'où FE = DE = DE = EFD. Les triangles EFD et CED sont semblables d'où EDC = EFD.

Par suite $\widehat{ECD} = 2 \widehat{EDC}$.

IV

L'historique de la découverte peut être présenté ainsi:

En 358 H., ou peu avant, Ibn al-Layth encore inconnu et qui brûle de percer, donne le premier coup de pioche dans la construction de l'heptagone. Il énonce quatre lemmes, ramène la question à la division d'un segment suivant une certaine relation, et réussit cette division, pense-t-il, par l'intersection de cercles et de droites. Or il est en correspondance avec le jeune mathématicien al-Sijzi. Celui-ci découvre la faute, s'efforce en vain de la corriger et finit par recourir à Abū Sa'd al-'Ala' ibn Sahl. Ce géomètre y parvient par les sections coniques. Mis au courant, Ibn al-Layth malheureux, de voir l'occasion lui échapper, apporte à la solution quelques modifications insignifiantes

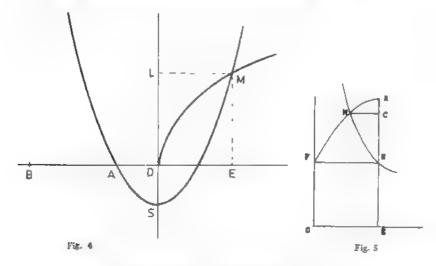
3. Partage du segment AB par les sections coniques, al-Qühi (1er mémoire)

Prenons deux droites perpendiculaires en D et DA = DS (longueur arbitraire). Traçons la parabole d'axe SD, de sommet S et passant par A. Traçons l'hyperbole équilatère de sommets D et A et d'axe AD. Elle coupe le parabole en M dont la projection est E sur AD, et L sur SD. Prenons AB DL aux le prolongement de DA.

Dans la parabole \overline{ML}^{i} SDSL ou $\overline{ED}^{i} = DA \cdot DB$

Dans l'hyperbole ME3 - DE AE ou AB3 = DE EA

Ainsi un segment BE a été divisé dans les conditions voulues.



Methode d'al-Sijzi et d'Ibn al-Layth

Sur le prolongement du côté EB du carré OEBF on prend BA EB. On trace la parabole d'axe AB, de sommet A passant par F. (Done dans l'équation de la parabole y^* - 2 px, 2p = AB). On trace aussi l'hyperbole d'asymptotes OE, OF passant par B. Elle coupe la parabole en M qui se projette en C sur AB. Posons BE = BF - BA - a, M apparteuent à l'hyperbole (a + BC) $(a - MC) = a^*$ d'où aBC = (a + BC) MC.

Comme M appartient à la parabole $MC = \sqrt{A\bar{C}AB}$. Par suite AB est divisé en C suivant la condition voulue.

TIT

Contenu mathématique des mémoires

Pour construire l'heptagone régulier il s'agit de diviser un cercle en 7 parties égales.

- 1. (1) Archimède suivi par al-Qūhī (premier mémoire) et al-Ṣaghānī se propose de construire le triangle ABD où $\widehat{B}=2$ \widehat{A} et $\widehat{A}=2$ \widehat{D} .
- (2) Al-Qühi (2° mémoire) veut construire le triangle ABG où $\widehat{A} = 5\widehat{B} = 5\widehat{G}$.
- (3) Ibn al-Layth et al-Sijn construisent ADE où $\widehat{D} = \widehat{E} = 3 \widehat{A}$.
- Dans une 2º étape, les égalités entre les angles vont céder la place à des égalités entre les côtés.

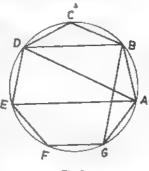


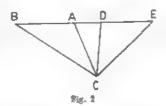
Fig. 1

Archimède et al-Qûhi (1er et 2e mémoires) et al-Şaghâni aboutissent à division d'un segment en trois parties (voir début de l'article). Donnons la méthode d'al-Qûhī (2e mémoire).

Dans le triangle ABC, $\widehat{A} = 5\widehat{B} = 5\widehat{C}$, nous prolongeons BA en ADE de sorte que $\widehat{ACD} = \widehat{ACB}$ et DC = DE. Les triangles semblables EDC et ECA, ADC et DBC donnent:

$$ED EA = \overline{E}C^{1} = A\overline{C}^{1} = \overline{A}\overline{B}^{1}$$

$$DA \cdot DB = \overline{C}\overline{D}^{1} = \overline{D}\overline{E}^{1}$$



Ibn al-Layth (dans mémoire perdu) et al-Sijzī remplaçent la relation angulaire (3) par la divison de AB en deux segments AC et BC tels que

$$\frac{\sqrt{ABAC}}{BC} = \frac{AB}{AB+BC}.$$

Ibn al-Layth indique dans sa 2^n lettre une sutre division de AB en C et D.

telle que $AB \cdot DB = \overline{AC^1}$ $CB \cdot CD \Rightarrow \overline{AC^2}$ $B \quad D \quad C \quad A$

Fig. 3

la course fiévreuse vers le but, les chutes, les arrêts forcés, voire les irrégularités ne vont pas manquer: toutes circonstances qui donneront lieu à une querelle de priorité sur laquelle se grefie pour l'exacerber la vieille "Querelle des Anciens et des Modernes". Dans le brouhaha des revendications contradictoires et des mathèmes qui vont s'élever, nous avons pour interprête et guide précieux sinon impartial, un géomètre attardé al-Shanni qui s'est intéressé à la querelle et en connaît bien les dessous.

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Les mémoires à verser au dossier du procès sont:

- 1º) Une première lettre d'Abūl'-Jūd ihn al-Layth, adressée en 358 H. à Abūl-Ḥusayn 'Ubayd Allāh b. Abmad, dont copie adressée à Abū M. 'Abdallāh b. 'Ali al-Ḥāsib. Cette lettre est perdue mais sou contenu nous est révélé par les lettres 2 et 3 d'Ibn al-Layth, 4 d'al-Sijzī, 8 d'al-Shannī.
- 2°) Lettre adressé par Ibn al-Layth à Abū M. 'Abdallāh b. 'Alī al-Ḥāsih. L'auteur y analyse les solutions d'al-Qühī et d'al-Ṣaghānī et la sienne propre. (Ms Paris 4821, f.37b-46a.)
- 3°) Lettre d'Ibn al-Layth à Abū'l-Ḥasan Ahmad b. Ishāq, plusieurs années après la clôture de la querelle (Ms Caire 7805, f. 117^b 120°.)
- 4°) Mémoire d'al-Sijzī sur la construction de l'heptagone régulier et la trisection de l'angle; (Ms Paris 4821, f.10b-16b; le même que Caire 7805 f.113-117.)
- 5°) Mémoire d'al-Qühī dédié à 'Adud al-Dawla. (Ms Paris 4821, 17b 23b; Caire 7804 f. 222b 225°. La dédicace au roi dans le ms. Caire est très embellie).
- 6º) 2º mémoire d'al-Qûhî dédié à Abû'l-Fawâris b. Adud al-Dawla postérieur au précédent et tout à fait différent. (Ms Paris 4821, f. 1^b 8^a).
- 7º) Mémoire d'al-Saghānī dédié à 'Adud al-Dawla. Il y est fait mention d'un mémoire antérieur présenté au roi à Rayy et dont le mémoire actuel est un remaniement. La date de résolution d'une proposition du mémoire est fixée au 12.X.360 H. (Ms Paris 4821, 23b 28b.)
- 8º) Mémoire d'al-Shannî, Kitāb kashf tamwih Abū'l-Jād (Ms Caire 780, f. 129h-134h). Al-Shannī relate les circonstances de la découverte de la solution, les erreurs d'Abu'l-Jūd et analyse les solutions.

De ces mémoires, C. Schoy a étudié en 1926, la construction de l'heptagone par al-Sıjzī (Isis, 8 (1926), 21-35), et Y. Samplonius, en 1963, celle d'al-Qühî (Janus 50 (1963), 227-249, d'après F. Sezgin, CAS, V, p. 318, 3°).

This is a French version of a paper which appeared in Arabic in JHAS, 1 (1977), 352-384. Its present form makes the results available to a wider circle of readers.

Construction de l'heptagone régulier par les Arabes au 4° siècle de l'hégire

ADEL ANBOURA*

Au 3º siècle H., Thabit h. Qurra traduit un mémoire d'Archimède sur l'heptagone régulier dont le texte gree est actuellement perdu. La solution d'Archimède revient à diviser un segment AB en deux points C et D de sorte

que
$$(AC + CD)$$
 $CD = DB^2$ C $CD + DB$ C C

ce qu'Archimède résout par le procédé de "la règle mobile" et non par la géométrie fixe.2 On sait que la construction de l'heptagone régulier mène à une équation du 3º degré et par conséquent, ne peut résolue par intersection de cercles et de droites.

La question en reste là jusque vers le milieu du 4º siècle H. A cette époque un intense bouillonnement agite la vie scientifique arabe, exalté par la dynastie Bonyide. Quatre géomètres de valeur vont s'attaquer à la construction de l'heptagone. Ce sont:

- 1. Abū'l-Jūd M. b. al-Layth
- 2. Abû Sa'îd Ahmad b. M. 'Abd al-Jalil al-Sijzî'
- 3. Abū Sahl Wayjan b. Rustam al-Qūhī b
- 4. Abū Hāmid Ahmad b. M. b. al-Husayn al-Saghānī!

En coulisse se tient un géomètre éminent dont l'intervention auprès d'Ibn al-Layth et d'al-Sijzi sera décisive: Abū Sa'd al-'Alž' b. Sahl.' Dans

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^{1.} T. L. Heath, A Manual of Greek Mathematics, (Oxford, 1931), pp. 283-286.

^{2.} Ibid. pp. 340-342 3. F Sezgin, Geschichte des grabischen Schriftung, Bd. V (Leiden, E. V Brill, 1974), pp 353-355 (où l'on trouvers toutes références utiles).

^{6.} Ibid pp. 329-334 5. Ibid. pp. 314-321, 403. 6. Ibid. p. 311

^{7.} Ibid. pp 341-342.

The intersection of any circular cone or cylinder with a plane parallel to the base is also a circle. And the line drawn from the vertex to the center of the base passes through the center of the intersection.

The proposition is followed by an example with proof, but no drawing.

References

Yvonne Dold-Samplonius, Book of Assumptions by Agajun (Doctoral Thesis, Amsterdam, 1977).

Max Krause, "Stambuler Handschriften islamischer Mathematiker", Quellen und Studien zur Geschichte der Mathematik, Astronomie und Physik Abt B, vol. 3 (Berlin, 1934), 437-532

Carlo A. Nallino, "Tracte di opere greche giunto agli Arabi per trafila pehievica", A Volume of Oriental Studies Presented to Edward G. Browne, T. W. Arnald and R. A. Nicholson eds. (Cambridge, 1921), 345-363.

Iba al-Oiftl, Ta'rikh al-hukama', Julius Lippert ed. (Leipsig, 1903).

Fust Sezgin, Geschickte des orabischen Schriftsums Band V. Mathamatik. Bis ca. 430 H (Leiden, 1974).

Manfred Ulimann, "Der Werwolf", Wiener Zersschrift für die Kunde des Morgenlandes, 68 (1976), 171 184

with an article in the last two marginal notes (fol. 102v). Affaţūn is never written with an article. Van Ess adds that in general an article with the name of an ancient author is somewhat curious. As the addition "translated from the Greek language" has been omitted in the Istanbul manuscript, its redactor may not have recognized Aqātun as an ancient Greek author. As the name Aqātun occurs, according to Lippert in this same form in all codices of the Ta'rikh al-hukamā' (p. 195), I assume its writing to be correct. This would point to a Greek name like Εκατον. A more probable Greek name would be ²Αγαθων. However, this means three exceptions in one word from the normal rules of transliteration. M. Ullmann has shown that the Greek word λοκανθρώπος (werewolf) became quírub in Arabic by means of a Syrian intermediary, in which 0 was already rendered by f. In our case he also suggested an intermediary, namely Pahlavi (= the Iraman language of Sassanid Persia). D. N. Mackenzie and W. Sundermann agreed with this eventual possibility, and gave more details:

Although one expects g in Pahlavi for γ , k sometimes occurs (hykmien for $\gamma_1 \varepsilon \mu \delta v$). Then ${}^3A\gamma \chi \vartheta \omega v$ could have been rendered by *k ium, which would have to be written in Arabic as *q ium. Because of the ambiguity of some Pahlavi letters, the ending two could have been misread as *n . In this way one could arrive at *q im, Aqâtun. Already C. A. Nallino pointed out that scientific works were translated from Greek into Pahlavi into Arabic. He notes in this context that the extreme ambiguity of Pahlavi writing makes it impossible to read foreign names with certainty. A. Schall comments that the rules in everyday life are not so strict: the correlation $\gamma \sim \tilde{\omega}(q)$ still exists in dialects, especially in names, e.g. (Jordan.) $\tilde{\omega} = \tilde{\omega} = \tilde{\omega} = \tilde{\omega} = \tilde{\omega}$ (priest) is rendered by Goussous, and (Sudan.) $\tilde{\omega} = \tilde{\omega} = \tilde{\omega} = \tilde{\omega} = \tilde{\omega}$ by Abdel Gadir. $\tilde{\omega} = \tilde{\omega} = \tilde{\omega} = \tilde{\omega}$ a rather common Greek name, but no mention of a mathematician of this name has been transmitted to us.

Appendix

Among the pages of the treatise one, fol. 95, does not belong to the text, which after fol. 94v continues on fol. 96v. This page may belong to another treatise of the manuscript, as it contains on one side, fol. 95v, a referential proposition which has no apparent connection with the contents of the Kitāb al-mafrādāt. It is written in the same band as our treatise. Fol. 95r consists of two three-dimensional drawings not belonging to the proposition on fol. 95v. Seemingly they are not of an astronomical nature.

The proposition on fol. 95v reads: Proposition by Muhammad ibn Müsä from the book "On the Sphere", which refers to it:

His name is given as Muhammad ibn Sartaq from Maragha. It is remarked that he has studied this book by Aqatun, has verified and corrected it. The reductor is not otherwise known to us.

To the title of the Bankspore manuscript is added "Thabit ibn Qurra translated the treatise from the Greek language into the Arabic language". This leads to the question of what the original Greek title may have been, and the Greek spelling of Aqatan [On author and title see thesis, Chapter II]. The suppositions were excluded from the thesis, as no definitive answer can be given The hypotheses are laid down in the following.

a. The Title

In the Arabic sources we find the titles Kutāb al-ma'khūdhāt, Kitāb al-ma'qayāt, Kitab al-mafrūdāt. The first of these is connected with the verb akhadha () with basic meaning "to take". This corresponds with the Greek verb λαβτιν. Also the original meaning of ma'khūdhāt, i.e. takings, receipts, returns (commerce) and of λημματα are equivalent. Thus Kitāb al-ma'khūdhāt, refers to the Greek title "Lemmata", e.g. Archimedes.

The second title, Kitāb al-mu'javāt is related to the verb a'taya () is IV) which means "to present, offer". The corresponding Greek verb is \$100 va. Thus Kitāb al-mu'tayāt is the translation of the Greek title \$200 u.c., g. Euclid's Data.

As for the title Kitāb al-mafrādāt: in the case of Thābit ibu Qurra this title is sometimes translated as "Data". As I pointed out above, Data has usually a different Arabic equivalent. Therefore I tried to find another possible Greek title. Mafrādat is a form of the verb farada (, ,) meaning something like "to decide, impose, assume, suppose, postulate". This could be rendered by the Greek verb οπος ιθ2οθα ι (inf. med.), and thus mafrādāt could be a translation of μποθεσείς. To this E. M. Brums objects that nowadays the Arabic word for assumption, supposition, hypothesis is ifitrād. He therefore suggests starting from a more special meaning of farada, namely "to take for granted". This could then correspond with the Greek verb συγχωρεω and we could assume mafrādāt to be a translation of τυγχωρισείς.

This small exposition may have made clear bow difficult it is, if not impossible, to establish the original Greek title.

b. The Author

The author's Greek name, which was arabized into Aqatun can only be guessed at. Some want to explain Aqatun as a misreading of Aflatun (= Plato). According to J. van Ess this cannot be correct as Aqatun is written

Prop. 40 · (= Prop. 43): If in the right-angled triangle ABG with angle ABG right, angle BAG is bisected by line AD, line AE drawn at random, from point E line EZ constructed parallel to line AD, ZB joined cutting AD in T, and ET joined, then AZ: ZT — AE: ET.

Prop. 41 (1) Let in the right-angled triangle ABG, with angle BAG right, from point A to line BG the lines AD and AE be drawn such that angle DAG is equal to angle GAE, then BE: EG = BD: DG.

- (2) Conversely; If BE; EC = BD; DG [and angle BAG be right], then

 ★ DAG = ★ GAE.
- (3): (margin) Let \star EAG = \star CAD, and BD: DG = BE:EG, then \leq GAB = 90°.

Prop. 42 Let in triangle ABG angle B be bisected by line BD and angle G by line GD, then angle A is bisected by line AD.

Prop. 43 is identical with Prop. 40 but has been proved in a different way. Here Propositions 41 and 42 are used, whereas for the proof of Prop. 40 Propositions 38 and 39 are applied.

From these contents the impression is gained that Agâţun made an effort to understand plane geometry. Maybe this was done in a school where this treatise served as a textbook or exercise book. In this case, however, one would suppose more copies of the treatise to be extant. It seems therefore more probable to me that this was a one-man effort. Agāţun worked out new propositions and also, like Pappus, gave some proofs that had been left out in the existing mathematical literature, but no references are added. There may have been a mutual influence between Pappus and Agāṭun, Other mathematicians exercising an influence on our author appear to be Archimedes, Euchd, and Apollonius. Also a connection with Menclaus exists: propositions 33 and 34 contain two special cases of Menclaus' theorem in the plane. Some of the propositions in the Kitab al-mofrādat may be later Arabic insertions [Thesis, Chapter I].

As the treatise is only moderately original, which may be the reason why not many copies seem to have existed, its impact on later mathematics was small. The only connection found is in Ibn al-Haytham. An interesting feature of our copy are the marginal notes. In these notes improvements on the text are made, i. e. some missing words are inserted and some different proofs added. This is done conscientiously and with great care. E.g. in the case of Prop. 6 the addition ends "I had written down this remark before looking at the construction of the proof. So I apologize." The marginal notes at the beginning and the end of the treatise inform us about the redactor.

Prop. 31: If the tangents ED and EA to circle ABTD be drawn, and if an arbitrary line EZ be drawn cutting the circle at Z and B; if AD be joined, if to EZ the perpendicular ZT be drawn cutting AD in Y and the circle in T, and if EY and ZD be joined, then \neq DEY = 2 \neq DZT.

Prop. 32: If to the semicircle with diameter AG the tangents EA and EB be drawn, EB and AG be extended until the intersection point D, if BZ be drawn parallel to AD, DZ and AB be joined intersecting in H, and HT be drawn perpendicular to AG, then T is the center of the circle.

Prop. 33: If line AG of triangle ABG be bisected at D, line BA be extended to E, and ED be joined and extended to Z on line BG, then BE: EA = BZ : ZG.

Conversely, if BE : EA = BZ : ZG, then AD = DG.

Prop. 34: If line BA of triangle ABG be extended from A to E, line BG bisected at Z, and line AG divided at D such that BE: EA = GD · DA, then E, D, Z are collinear.

Prop. 35: Through point D outside line AB let the lines EI) and DZ be drawn both parallel to line AB, then EDZ is a straight line.

Prop. 36: From point E let the lines EZ and ED be drawn cutting the lines AB, AG, AD respectively in Z, T, L and in B, G, D, and let EZ: ZT = EL: LT, then EB: BG == ED: DG.

Prop. 37: In the right-angled triangle ABG, with angle BAG right, let the lines AD and AE be drawn such that angle DAE is equal to angle ABG, and from point B let the perpendicular BZ to AE [cutting AD in T] be drawn and extended to H on AG. Then DAAT + GB·BD = HB·BT + GA·AH; and secondly GB·BD + GA·AH = ABc·DAAT + GB·BD — HB·BT + GA·AH.

Prop. 38 (1): Let the lines AB, AG, AD be of equal length and DG, GB, BD be joined, then * GBA + < GDB 90°.

- (2): Moreover, if AB AG and +GBA + +GDB 90°, then the lines AB, AG, AD are of equal length.
- (3): Also, if AD = AB and ≮ GBA + ≮ GDB = 90°, then the lines AD, AG, AB are of equal length.
- (4): Finally, if AD \perp AG and \star GBA + \star GDB \cdot 90°, then the lines AD, AG, AB are of equal length.

Prop. 39: If in triangle ABC line AD is drawn meeting BG in D such that angle DAG is equal to angle ABC, then

 $BG:GD = BG^{\alpha}:GA^{\alpha} = BA^{\alpha}:AD^{\alpha}.$

- Prop. 20: If in the isosceles triangle ABG, with AB equal to AG, lines AE and AD he drawn, meeting BG at E and D such that BD·DG: DA⁸ = GE·EB · EA⁸, then DA = AE.
- Prop. 21: Let in triangle ABG angle BAG be bisected by line AD, meeting BG at D, then (BA + AG): GB = AB: BD.
- Prop. 22. Let from triangle ABG AB be extended to D and AG to E, let DH be drawn parallel to EB and EZ parallel to DG, then ZH will be parallel to BG.
- Prop. 23: Let in triangle ABG AD be equal to BE and AZ equal to GH, let GE, GD, BZ, BH be joined, GE and BZ intersecting in W and GD and BH in S. If AS and AW be joined and extended meeting BG in T and Y, then BT is equal to GY.
- Prop. 24: Let angle AGB in the right-angled triangle ABG, with angle ABG right, be bisected by line GD, and angle DAE be equal either to angle AGD or angle BGD, then GD > GE.
- Prop. 25: Let angle AGB in the right-angled triangle ABG, with angle ABG right, be divided by line GD such that angle BGD is twice angle DGA, then BG · GA > GD².
- Prop. 26: Let us the semicircle with diameter AD are AB be equal to are BG, let GD be joined, and BE be drawn perpendicular to AD, then GD < ED.
- Prop. 27: If in triangle ABG BG be bisected at D and AD be joined. If from B an arbitrary line be drawn cutting AD in Z and AG in E, and GZ be joined and extended to H on AB, then, if HE be joined, it is parallel to BG.
- Prop. 28; If in the circle-segment standing on line BG are BG be bisected at A, E be taken on the extension of BG, and AG and AE cutting the segment at D be joined, then EA·AD AG*.
- Prop. 29: If through two circles intersecting in A and D, an arbitrary line be drawn cutting one circle in Z and H and the other in B and E, and ZA, AB, ED, DH be joined, then \$ ZAB = \$ EDH
- Secondly, if HD and ZA be extended to K and T on circle ABED, and BK and ET be joined intersecting in L, then BL = LE.
- Prop. 30: If from triangle ABG with angle BAG right, BA he extended to D, and from D, DE he drawn perpendicular to BG cutting AG in Z, then BD · DA = GZ·ZA + ZD².

Conversely: If BD·DA = GZ ZA + ZD1, then < DEB = 900

- Prop. 6: If BG is the diameter of a semicircle, and the chords AG, BD meet in Z, and if BA, GD be drawn meeting in E, then BD DZ = GD DE.
- Prop. 7: Let BG be the diameter of a semicircle, and the chords AG. BD meet in Y. Take Z on BD and E on AG so that BD · DY = DZ² and GA'AY AE², and let EB, ZG be joined meeting in H, then ZH HE.
- Prop. 8: In the equilateral triangle ABG the heights AZ, BD, GE are of equal length.
- Prop. 9: Let ABG be an equilateral triangle, and AD its height. Let from a point E on BD the perpendiculars EZ and EH be drawn to the sides GA and AB, then AD = EZ + EH.
- Prop. 10: Let ABG be an equilatoral triangle, and AD its height. Let from an interior point E the perpendiculars to the sides EZ, EH, ET be drawn, then AD = EZ + EH + ET.
- Prop. 11: If in triangle ABG the line AD be drawn meeting BG at D such that angle BAD be equal to angle AGD, then GB BD = AB².
- Prop. 12: Let in triangle ABC, with AB equal to AG, AD be drawn perpendicular to AB meeting the extension of BG in D. If AB be bisected at E and ED be joined cutting AG at Z, and if through Z, HZ be drawn parallel to AB, then DA'AH = AG'.
- Prop. 13: If in triangle ABG, with AB equal to AG, AD be drawn perpendicular to BG, then 2 DG GB = AG².
- Prop. 14: If in triangle ABG the perpendicular AD to BG be drawn, then $BD^2 DG^2 = BA^2 AG^2$.
- Prop. 15: Let line AB be equal to line AG and line BD equal to line DG, and let both augles BAG and BDG be right, then <ABD <AGD.
- Prop. 16: Let A be the right angle of the right-angled triangle ABG. If BG be bisected at D and AD be joined, then BD DG ~ DA.
- Prop. 17: Let us the right-angled triangle ABG, with angle BAG right, on the extension of AG a point D be taken, from which DE is drawn perpendicular to BG and cutting AB at Z. Let GZ be joined and on it H be taken such that BH* = AB BZ and let DH be joined, then DH* = DE ZD.
- Prop. 18: Let the lines AB and BC meet at B, and on AB point D be taken, such that $AB^1 = AD^2 + BG^2$. Let DC be joined and bisected at E, and AE be joined, then \neq DAE = \neq DGB.
- Prop. 19: If in the isosceles triangle ABG, with AB equal to AG, an arbitrary line AD be drawn cutting BG at D, then BD·DG + DA² = AG².

manuscript 2468,29 (fol. 141r 144v) [Sezgin, p. 135]. An Arabic edition of the latter together with Bankipore 2468,28 (fol. 134v - 141r, Kuāb Arshimidis fill-dava'ir al-mutamassa, has been published by the Osmania Oriental Publications Bureau (Hyderabad-Du., 1947).

In the Aya Sofia manuscript the date of copying is given as ca. A.D. 1230, mentioning as place of copying, sometimes Damascus, sometimes Maragha. At the end of the Bankipore manuscript the date of its composition is indicated as A.D. 1027/1028. In the present copy some of the treatises are dated Mosul A.D. 1234/35. Thus the present copies of both treatises date from the same period. Both are written in Naskhi. The mathematical quality of the treatise is higher in the Aya Sofia manuscript than in the Bankipore manuscript.

The reasons for accepting the title Kitth al-mafradat and Aqatun as its author are laid down in Chapter II of the thesis.

The Contents [Thesis, Chapter III]

Prop.1: If the base BG of the circle-segment ABG he extended in either direction with pieces of equal length, and from the endpoints D and E the tangents EZ and DH he drawn to the segment, then the line ZH connecting the tangential points is parallel to the line ED.

Prop. 2: Assume the two lines DB and DG are tangents to a circle. Let the chord BG connecting the tangential points be extended to E, and let from E a third tangent be drawn, touching at A and meeting DG in Z and BD in T, then TE: EZ = TA: AZ.

Prop. 3: Assume the two lines EG and ED are tangents to a circle, while EB cuts it at H and B. Let DA be the chord through D parallel to EB, and let AG meet BH in Z. Then BZ = ZH.

Remark: There is no drawing in the Aya Sofia manuscript as the room left open for this purpose is too little. Later I discovered that the drawing had been made on a loose leaflet which lies now, on the microfilm, between fol. 87v and fol. 88r.

Prop. 4: Let ABG be an isosceles triangle and AD the perpendicular to the base BG. Assume on AB the points Z, E such that BD¹ = BE BZ. Let ZD be joined, ZH be drawn parallel to BG, and EH be joined, then <EHG = 2 *AZD.

Prop. 5. If AG is the diameter of a semicircle and B the middle of the arc AG; let from D, on the extension of AG, DB be joined cutting the circle at Y, If YE = EB and from the center Z, ZE be drawn until it meets the extension of AB in H, then AH : HB = DZ : ZB.

Some Remarks on the "Book of Assumptions by Aqatun"

YVONNE DOLD-SAMPLONIUS*

Introduction and Conclusion

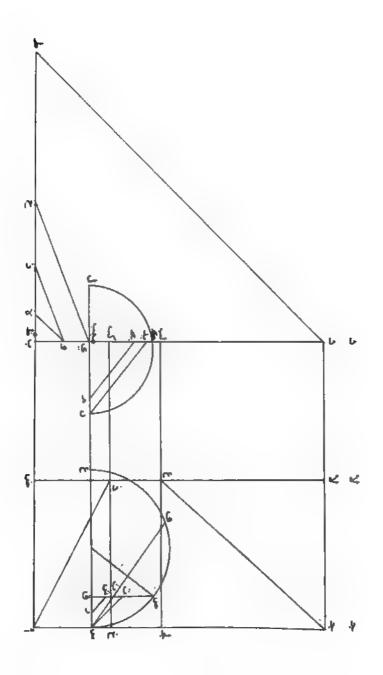
The treatise Kitāb al-mafrādāt li laātun (Book of Assumptions by Agātun) has been treated in full in my doctoral thesis (Amsterdam, 1977). The present paper contains an abstract of this thesis. It consists of the contents of the treatise, i.e. propositions only without either proofs or drawings, along with some remarks describing the manuscript and pointing out several influences. In addition the questions of the original Greek title and putative Greek name of the author are extensively discussed. The offered solution is, however, too vague to have been included an the thesis.

My conclusion is that the treatise contains interesting propositions, but no sensational theorems. Some propositions deal with fundamental properties of triangles, some go in the direction of trigonometry, others could be connected with optics. The author, i.e. Aquitin seems to have been a man with a good knowledge of the mathematical literature, judging from the different influences on his treatise [Thesis, Chapter IV]. He may have lived around the same time as Pappus: on the one hand Aquitin gives two converses to a lemma by Pappus (prop. 41), on the other hand both Pappus and Aquitin prove a lemma related to Apollonius' Conics (prop. 27) and a lemma connected with Euclid's Poissus (prop. 22); these proofs by Aquitin and Pappus are similar but not identical. The treatise was still of value and interest to Arabic mathematicians in the thirteenth century, according to the extensive marginal notes. Yet the sphere of influence apparently was not very large.

Description of the Manuscript [Thesis, Chapter I]

The treatise "Book of Assumptions by Aq\u00e4tun", Kit\u00e4b al-mafr\u00e4d\u00e4t li Aq\u00e4tun, is contained in the Istanbul manuscript Aya Sofia 4830,5 (fol. 89v 102v) [Krause, p. 439]. It consists of 43 propositions dealing with plane geometry. Nineteen propositions, all from the first half, form a separate treatise entitled "Book by Archimedes on the Elements of Geometry", Kit\u00e4b Arshimidis fi'l-uj\u00e4l al-handasiya. This is contained in the Bankipore

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هذا الشكل ويصفح عن السهو القليل إن وقع (١٠) في بعض حساناتها الحزئية فقط ، وإن عثر عبى خطأ في بعض براهيه فيسها (١٠٠) عليه مفيدا الاتعاده (١١٠) فقد (١١١) عنمى عليسا لكثرة المقدمات واختلاط الهندسية فيها بالحساب ، ولا يسكر كثرة التطويل في مقدماتها فإن الوصول ■ إلى المطلوب البرهائي بكثرة المقدمات ح و > بالمتوسطة مع العصمة من العلم بن كانت يكون (١١٠) إليه بالدربة والارتباض ، وأدل عبى < أن > الإصابة في المعقولات بنكتر بالضرورة مقدمات براهيها ومتوسطاتها ، وأعظم فوائد العلوم الرياضية إنما هو ذلك ولقد (١١٠) تتحييزت عن التطويل في مقدمات براهين هذا الشكل مع كونها حقا ضرورية (١١٤) في إفادة التبحة المطلوبة ، ثم إن أشار المحدوم المعم فسأعرص سائر الطرق (١٤٠) ، على رأبه لماقد العالى إن شاء الله تعالى ،

(١١٥)والسيلام(١١٥) .

۱۱۸ - اگاه وقعت ۱۹۰۹ - اگاه مسهده ۱۹۰۱ ایر ادعاده افتر بستاه ورایشهسوند ما ذهبرالیه ۱۹۱۹ - اگام آن فند ۱۹۹۳ - از تاکسته ۱۹۱۹ افتال و طفا ۱۹۱۹ - افتال و صرودیا ۱۹۱۵ - از اظارف ۱۹۹۱ - و انگسته در محده مــــن أحد عشر حزءا ونصفه عشرة أحراء من أحد عشر حرء، من الواحد وإدالـ ٨٨ قسمنا العشرة بأحد عشر قسما يكول كل قسم عشرة أجراء مـــن أحد عشر من الواحد فخط _{ت ك}ي جزآن من أحد عشر حزءًا من ب لا العشرة وسطح ب س (^(۸۹) من سطح ب يكون على هذه النسبة، فمنحرف ١١ ك. ب(٩٠) حزآن من أحد عشر جزءا من مربع أَبِ جَدَ . وَلَأَنْ لَسَةَ مُنْجَرِفُ وَكِي رَاءً ۚ إِلَى مُنْجَرِفُ حَدَّلُ عَ كُنْسَةً قَاعِدَةً بِ كُنَّا إلى قاعدة آب د – وبالمقدار الذي به ب كب اثنان ذ لب د خمسة لأنه(٩١) مثلاه ومثل نصفه فيكون منحرف جدلبع خمسة أجراء من أحد عشر جزءا من المربع الكبير ولأن نسبة مثلث آ_{صر د(۲}۲۰) المساوي لمستطيل _{تح ي (۲}۲۰) إلى مثلث ج_{اع (۱}۲۰۰) كنسبــــة قاعدة ص ذ(٩٠) إلى قاعدة ع 🖟 . وهو مثلان ونصف ، فيكون مثلث حغ 🖟 📗 📟 مثلي ونصف(٩٦) ؛ سَ دَ (٩٢) ومجموعهما ثلاثة أمثال ونصف مستطيل ثم يَ (٩٧) . ولأن مستطيل آلا مركب من صرب صلع المربع الكبير في جرأي اص ــوأحدهما(٩٨) مثل ونصف 🗀 ی 🕡 والأخر ثلاثة أمثال ونصف ح س (۲۹٪ وذلك يساوي مجموع المثلثين < ومنحرف جَعْ ذَا > - قاذًا قصلنا المثلثين من سطح $\overline{
m V}$ فكأنًا قد فصلنا مه سطح صلع المربع الكبير في ثلاثة أمثال و نصف خ س(٩٩٪. فيكون منحوف جع ١٠٠٪ مساويا لضرب ضلع المربع الكبير في مثل وقصف 🗇 🖫 . فمنحرف جَعَ 🚹 (١٠١٦ مثل ونصف سطح ـــ س أي منحرف 1 د كـــ بـ (١٠٣)، فالمقدار الذي به يكون منحرف (١٠٣)، جدل غ خمسة يبقي (١٠١) سطح ع ل كب د (١٠٠) و احداً (١٠٦)، و هو واحد و هو المطلوب.

والمأمول من كرم المخدوم والمنعمأدام الله علوه أن ينعم بالنطر(١٠٧) والتأمل في

الآخر أربعة و 🕫 من هُه من الواحد وهو سطح ع كب الناقي . ولأن سطع خ ص(٣) هو ۱۵٪ ضرب آخ^{(۱۵}٪ فی ا س^{(۱۲}٪ و اح^{(۱۲٪} بساوی تکب وهو واحد وتسعة أجزاء من أحد عشر حزءا من واحد مع زيادة حس(١٩) أي رس – وضع آنور(١٩) هو(٧٠) مثل وقصف ساى مع ثلاثة أمثال وقصف رأس فسرهان(٧١) أشكال أمقالة الثانية من أقليدس يكون ضرب الح (٧٧) في اص (٦٩) يساوي سطح (ض (٦٩) في آس وسطح اصَ في حَسْ (٦٨). ولأن أحد قسمي اص(٦٩) مثل وفصف اس وقسمه الآخر ثلاثة أمثال ونصف ش ع (٦٨) مسطـــع(٧٣) _{احر (}٢٩١) في آس يساوي مجموع ^(٧٣) سطحين أحدهما حِثلاثة أنصاف مربعِ > ١ س – وهو واحد وتسعة أجراء من أحد عشر فيكون تكسيره(٧٤) أربعة و ٢٩٠٠ من ٣٠٢٥ والسطيح الآخر هو(٧٥) ثلاثة أمثال ونصف رس في سَ وهو سطح يكون أحد صلعيه رَسَ والآخر سنة و(٧١) ٢٥ من قد. أما سطع ا مَن أَي رَس فينحل (٧٧) أيصا إلى صرب حزاي اص (٧٨) في رسم (٧٩) أي إلى (٢٩) صرب اثنين وثمانية أجزاء من أحد عشر جزءا من واحد في رأس - فيحصل(٨٠) سطح أحد ضلعيه رَسَ وَالْآخُرِ النَّانِ وَتُمَانِيةَ أَحْزَاءَ مِنْ أَحَدَ عَشْرَ مِنْ وَاحَدَ ﴿ وَإِلَّى سَطِّحَ رَّسَ فِي ثَلَاثَةَ أمثاله ونصف فيحصل ثلاثة مربعات /ركي ونصف مربعه . فحصل لنا ح من > جميع أحزاء يومي (٨١) سطح تكسيره أربعة و ٢٩٠٠ من ٣٠٢٥ من واحد وسطحان آخران مجموعهما سطحٌ أحد ضلعبه رّس وضلعه الآخر ﴿ ضَعَفَ ﴾ أربعة و ٣٠ من ٥٥ من واحد وثلاثة مربعات ونصف مربع رّ س . فادا أضفنا يكون بصفها مساويا لأُجزاء سطح ع ي (٨٧) المستطيل . ولأن(٨٣) سطح ع ي (٨٤) إذا فصل منه مستطيل ع ي (٨٢) یبقی مستطیل س ت و إذا عصل منه مثات اح آ^(۸۵) ببقی منحرف اذکت ب(۸۳) فيكون مستطيل سآب مساويا لمنحرف 1 د ك ب(AV). ولأن بأي واحد وتسعة أجراء

^{77 -} د . ا ص -1 Jed-10 وموالتنال ومو Jr - 11 1 1 1 - 3T بهاده ل دومو 79 - كا ال أس ۸۸ - ك ، ك . ح س ٧٧ - ك ، ل ، ١ح وي د د د ل و تکليم ٧٤ سال كرار الناسخ كتانيًا ١٠٧٠ ل. فوق السطر ۷۷ – کیل سرعت ٧٨ - ل - أص ۲۷- كاتمية ۷۷- كاد كار ينحن ه٧ كانال وهو 57 JED - AT مهاشتال عصل ۱۸۰ شتاک درخ ص وبالاعال أما ٨٨ - ك ، ل . ١ ك ك ب ك ، ل ، ح ب مد ك ، ل ، آ ج ط 74 - L . EU 14 ٧٨ - ١٠ ام كيب، ل ١٠ ١ - ٨٧

ولأن مَى ضعف و ر (²) و نحى ٣٠٧٥ (² أمثال ى حد و يَد نح ٧٢٥ أمثاله وبسبة ر مَّ الله مَن كسسة يد ع^(٢٥) إلى مَن فيكون ر م ٧٧٥ حرءا بالمقدار الذي < به > يكون و ب ٣٠٢٥ يكون و ب ١٠٢٥ وهو ضعف و ب ، وبالمقدار الذي < به > يكون و ب ٣٠٢٥ فيكون ر م ١٤٥٠ .

وقد دكرنا أن ي ل مثل وثلاثة أرباع ب و الواحد ، فسطح ي ن (٩٣) ﴿ فَيَ ى ل هو سطع مى > - الذي هو اثنان - و من (١٤) - وهو ١٤٥٠ (٤٩) من ٣٠٧٥ من الواحد(٤١) - في كلُّ الذي هو واحد وثلاثة أرباع ، فيكون(٤٧) تكسير مأربعة<و> ١٠٢٥ من ٣٠٧٥ من واحد . وهو تكسير مربع كي لأن ضرب نآي في يّ ساوي مربع کی . ولأن س ن ضعف(۱۸) کی و آص و (۴۹) نصف س ف یکون ص ق 😅 بساوي كى ومربعه مربعه ، ومربع من في بساوي سَ في في في في عيكون تكسير سطح سَ فَي في في غ أربعة و ١٠٣٥ من ٢٠٣٥ من واحد.ولأن في ش ثلاثة بالمفدار ٣١٪ الذي به يكون ش ﴿ (٣٠) أربعة وبسة سرر إلى رَقَ كدلك فيكون رَقَ ثلاثة أسباع نَّ سَ و رَ سَ أَرْبَعَةُ أَسْبَاعَهُ . فيكون سطح ع في رَ سَ أَرْبَعَةُ أَسْبَاعٌ عَ فَي قَلْ (٣٥٠) ن س المذكور تكسيره ، وسطح ع بي في ر س هو⁽¹⁰⁾ سطح <u>ع ث لأن ني س ي</u>ساوي سَ ع (٥٥) و س ع (٥٥) مثل س ر ، فسطح ع ث اثبان و ١٤٥٠ من ٣٠٧٥ وسطح رُ ـُـــرُ (٩٧) مربع راس (٩٧) ومطح رَكَ ثلاثة أرباع مربعه . - ولأنا فصلنا سع خبسة [و أنَّ من خمسة [٩٨٠) و أنَّ من أنَّ ﴿ حَمْنِ ﴾ واحد ينقى ع ي من (٩٠) تمامالعشرة أربعة و ٣٠٠ من هـ مَن واحد . فحميم سطح حـى(٦٠) المستطيل يساوي مربع ر سّ -وهو سطح رَحَ (١٧) ـــ وثلاثة أرباع مربعه - وهو سطح ر ٺ ـــ وسطحاً تكسيره اثنان اه آر من ۳۰۲۵ من واحد ... وهو (۲۲) سطح ت ع ـــ وسطحا أحد ضلعيه رَسَ وصلعه

فأقول إن المربع قد انقسم على الجهة المطلوبة وهي أن متحرف الله دي (٣٠) صعف سطح و ع (٣٠) والتحرف اله ع (٣٠) حمسة (٣٠) أمثاله ومنحرف أو دُل ع (٣١) ثلاثة (٣٠) أمثاله ومنحرف أو دُل ع (٣١)

رهان دلك . لأن برط عشرة أمثال برط ويسة دب إلى بو كنسة طاب إلى بو كنسة طاب إلى بو كنسة طاب إلى بو ويسم الله بالم ويان ويسم أمثال بو ويسم الواحد ، ولأن رب هم أمثال بو ويسم ورج هم مثلاً له يكون نسة رب إلى رح كسمة هم إلى هم ويسم (١٨٨) بركون وي تسعة أجراء على (١٩٨) أن وب الواحد أحد عشر جرما،

ميس اللياحن احيم ٥٠

الحمد لله رب العالمين والصلوة والسلام على رسوله محمد وآله أجمعين مسألة (المجمعي مسألة (المجمعي الدين المدين المجمعي الأحراء النظامية عن الإمام الأحل الأوحد العالم شرف الدين ماء الإسلام حجة (الرمان مظفر (الله عمد (المظمر الطوسي أدام الله توفيقه ببلد همدان سنة ست () وستماثة () هيجرية .

عن مربع متساوي الأضلاع كل صلع منه معلوم وأردنا أن نقسمه إلى أربعة (٢) سطوح (٨) أحدها(٩) سطع متواري الأصلاع مستطيل ، في الوسط ، وثلاثة محروات (١٠) تحيط به (١١) من ثلاثة جوانب على (١٧) هذا المثال على وحه تكون السطوح الأربعة بعضها للى بعص حلى حضرة مفروصة معلومة وقد عُينٌ صلع المربع ونسة السطوح . يقال كل صلع من أصلاع المربع عشرة والمطلوب أن يكون السطح المتواري الأضلاع الذي في الوسط نصف المنحرف الذي على أحد (١٣) حانبه والمنحرف الذي غوقة ثلاثة أمثاله والمنحرف الذي على الجانب الآخر مه خصة أمثاله .

مثال دلك : مربع ال حد متساوي الأضلاع وصلع ال عشرة وأردنا العمل المذكور ، فنخرج صلع حال حلى استقامته ويتعلم عليه نقطة . كيفما اتفقت(١٤) ونزيد على خط ب م قسعة أمثاله فيكون خط ب لا عشرة أمثال خط ب م ونصل ط و ونخرج من نقطة " خط م و ويوازي ط د ثم يتعلم نقطة لم على خط ب م ، نقطة لم كيفما وقعت(١٥) . ونجعل ط ر في مثل ب ط ونصل رو ا

۱۰۰۱ ؛ تعقیها ۱۳ و به ثقتی ۱۳ - ۵ مسئلة ۱۰ ك مسعب ۱۰۰۱ كتمها الناسم أولا ۱ مسعد ۱۰ ناقصة و بی ۱۰ ستة ۱۰ ك وحسن مدید ۱۰ كتب أولا احدامت ۱۳ - ۵ وحسن مدید ۱۰ كتب أولا احدامت از ۱۰ - ۵ وحسن مدید ۱۰ كتب أولا احدامت از ۱۰ - ۵ و كتب توق ۱۳ مد ۱۳ مد ۱۳ - ۵ و ت به ۱۳ - ۵ و كتب توق ۱۳ - ۵ و كتب توق ۱۳ - ۵ و كتب تفقه ۱۳ - ۵ و تنقي ۱۳ - ۵ و به كتب و قمت ثم عدل عن ۱۳ - ۵ و كتب تفقت ۱۳ - ۵ و به ۱۳ كتب به ۱۳ - ۵ و به ۱۳ كتب به ۱۳ - ۵ و به ۱۳ كتب به ۱۳ - ۵ و به ۱۳ كتب توقی ۱۳ - ۵ و به ۱۳ كتب توقی ۱۳ - ۵ و به ۱۳ كتب به ۱۳ كتب به ۱۳ - ۵ و به ۱۳ كتب به ۱۳ كتب به ۱۳ كتب به ۱۳ - ۵ و به ۱۳ كتب ۱۳ کتب ۱۳ كتب ۱۳ کتب ۱۳ ک

تقديم

لقد حقتمًا فص شرف الدين الطوسي على مخطوطتين :

الأولى هي مخطوطة حامعة كولومبيا Smith MS. Or. 47 من صفحة ٢٩ إلى صفحة ٣٥ المرابعة وهي مخطوطات مكتبة وهي مخطوطات مكتبة جدمعة كولومبيا ولقد أشرنا بحرف ك إلى هذه المحطوطة

الثانية هي محطوطة ليدن Or. 14 من صفحة ٣٢٣ وحه الى ٣٢٦ ظهر . ومن المعروف من مهارست دورى أن هذه المحطوطة قد تُسخت في القرن السابع عشر وسنشير ها محرف ل . وسسين في تحقيقا لحمر عمر الحيام أصلها ، ويكفينا الآن أن نقول إن المحصوطتين ترحمان إلى نفس الأصل على من المؤكد أن محطوطة كولوميا هي أقرب إلى الأصل عالمنالية

ـ ١ - باستشاء ثلاثة أحطاء في له نحد كل أخطاء له مع كثرتها في لـ والعكس غير صحبح .

ـ ٢ ـ ينةص ل خمس كلمات محدها في ك بيما ينقص ك كلمة واحدة موحودة في ل

ــ ٣ ــ كل ما يجب إضافته إلى ك ص كلمات وعبارات حتى يستقيم المغى يحب أيضه إضافته إلى ل .

والمخطوطتان تحتويان على أخطاء عديدة زادها الحلط بين حروف الرسم الصدسي واستعمال تقس الحرف ظ للدلالة عنى تقطتين مختلفتين في الرسم

واستعملنا الرموز التالية في التحقيق :

> ما بينهما كلامنا

📗] نقترح حذف ما يسهما

| ائتهاء صفحات ك

💻 💎 انتهاء صفحات ل

وأعلب النص عير منقوط وثقد قمنا بتنقيطه دول الإشارة إلا إدا تعددت الاحتمالات فأثنتنا نص المخطوطة في أسفل الصفحة ، وثقد أعدنا الرسم حتى يوافق النص . est égal au rapport de la base $B\Delta$ à la base ΠD , suivant la quantité qui rend $B\Delta$ égal à deux, alors ΠD est cinq, car il est égal à deux fois et demie celuici; on a donc le trapèze $CD\Pi\Omega$ cinq parties de onze parties du grand carré. Puisque le rapport du triangle AXZ, qui est égal au rectangle WJ, au triangle $C\Omega^{ij}$, est égal au rapport de la base ΔZ à la base Ω^{ij} , qui est deux et demi, le triangle $C\Omega^{ij}$ \mathcal{L} is to donc deux fois et demie AXZ, et leur somme est trois fois et demie le rectangle WJ.

On attend de la générosité du Seigneur Bienfaiteur - que Dieu perpétue son Emmence - qu'il examine et médite cette proposition, et pardonne les petites négligences, seulement si elles ont lieu dans certains de ses calcula particuliers.

S'il rencontre une erreur dans certaines de ses démonstrations, qu'il nous avertisse, cela sera utile à la question qu'il pose, car nous aurions été aveuglé par la multiplicité des premisses, et par le mélange des prémisses géométriques à l'anthmétique; et qu'il ne blâme pas la longueur excessive de ces prémisses, car atteindre l'éobjet d'une recherche démonstrative, par la multiplicité des prémisses et des propositions intermédiaires, tout en se préservant de l'erreur, si on s'en préserve, cela se fera par l'habitude et par l'exercice. Et j'indique qu'atteindre le but dans les sciences théoriques augmente nécessairement les prémisses de leurs démonstrations, et leurs propositions intermédiaires. Ce sont là les plus grands enseignements des sciences mathématiques.

Certes, J'ai évité de m'étendre sur les prémisses des démonstrations de cette proposition. bien qu'elles soient véritablement nécessaires pour mener avec profit au résultat cherché.

Si par la suite le Seigneur Bienfaiteur en exprime le désir, j'exposerai les différentes méthodes à son émment jugement critique, si Dieu le veut.

Que la paix soit.

^{1.} Littéralement: denx fois plus un demu

^{2.} Littéralement si cela est.

est le carré de RS, et la surface RV est trois quarts de ce carré. Mais comme on a séparé SO égal à cinq plus vingt-cinq cinquante cinquièmes f d'unité, il reste de dix entiers OJ égal à quatre plus trente cinquante cinquièmes,

Le rectangle WJ tout entier est égal au carré de RS, qui est la surface RW plus les trois quarts de son carré, qui est la surface RV plus une surface dont la mesure est deux plus mille quatre cent emquante trois mille vingt emquièmes d'unité, qui est la surface VO et une surface dont un côté est RS et l'autre côté est quatre plus trente emquante cinquièmes d'unité, qui est la surface $O\Delta$ restante.

Puisque la surface WX est le produit de AW par AX et que AW est égal à $B\Delta$ qui est un plus neuf parties de onze parties d'unité, augmenté de SW, soit RS, et que le côté AX est une fois et demie BJ plus trois fois et demie RS, alors, par la démonstration des propositions du $Livre\ II$ d'Euclide, on a le produit de AW par AX égal à la surface AX par AS plus la surface AX par WS. Puisque l'une des deux parties de AX est une fois et demie AS, et que l'autre partie est trois fois et demie SW, la surface AX par AS est égale à la somme des deux surfaces, dant l'une est trois demies du carré de AS qui est un plus neuf parties de onze parties, et sa mesure est donc quatre plus deux mille neuf cent trois mille vingt cinquièmes; l'autre surface est trois fois et demie RS par AS, qui est une surface dont l'un des deux côtés est RS, et l'autre est six plus vingt-cinq cinquante cinquièmes.

Quant à la surface AX par RS, elle se décompose également en les produits des deux parties de AX par RS. soit en le produit de deux plus huit parties de onze parties d'unité par RS — on obtient donc une surface dont un côté est RS, et l'autre est deux plus huit parties de onze parties d'unité; et en la surface de RS par trois fois et demie lui-même, on obtient trois carrés / de RS plus la moitié de son carré.

On obtient donc de toutes les parties de WX une surface dont la mesure est quatre plus deux mille neuf cents trois mille vingt enquièmes, plus deux autres surfaces dont la somme est une surface dont l'un des côtés est RS, et l'autre côté le double de quatre plus trente cinquante cinquièmes d'unité, plus trois carrés de RS et la moitié de son carré. Si on additionne le tout, on a la moitié égale aux parties du rectangle WJ. Puisque si de la surface WB, on sépare le rectangle WJ, il reste le rectangle SB, et si on en sépare le triangle AWZ, il reste le trapèze $AZ\Delta B$, on a alors le rectangle SB égal au trapèze $AZ\Delta B$. Puisque BJ est un plus neuf parties de onze parties, et que sa moitié est dix parties de onze parties d'unité, et que si on divise les dix en onze parties, chaque parties sera dix parties de onze parties d'unité, alors BJ est deux parties de onze parties de BC est dans la même rapport; alors le trapèze $AZ\Delta B$ est deux parties de onze parties du carré ABCD; mais puisque le rapport du trapèze $AZ\Delta B$ au trapèze $CD\Pi\Omega$

ahaissons la perpendiculaire UQ et marquons le point Ξ sur UQ peu importe où il se trouve et posons ΞT égal à une fois plus un tiers $Q\Xi$, et joignons TS; menons de Ξ la droite ΞR parallèlement à elle. Posons SW égal à SR. Menons $W\Delta$ parallèle à AB. Posons ensuite $D\Pi$ deux fois et demie $B\Delta$. Menons $\Pi \setminus \text{parallèle}$ à AB. Posons AX une fois et demie BJ, augmenté de trois fois et demie $J\Delta$. Menons $X\Psi$ et menons ensuite AZ, $C\Omega$. Je dis alors que le carré a été divisé de la manière cherchée, c'est-à-dire que le trapèze $ABZ\Delta$ est deux fois la surface $Z\Omega\Pi\Delta$, le trapèze $AZ\Omega C$ est son quintuple, et le trapèze $CD\Pi\Omega$ est son triple.

Demonstration.

Puisque BI est dix fois BE, et que le rapport de DB à BF est égal au rapport de IB à BE, on a donc DB dix fois BF, on l'appelle alors l'unité. Puisque GB est 55 fois BY₁, et GH 45 fois celui-ci, on a le rapport de GB à GH égal au rapport de 55 à 45, et le rapport de BF à FG est égal au rapport de 55 à 45.

On a donc FJ égal à neuf parties, étant donné FB, l'unité, onze parties. Puisque MJ est le double de FB, et que ΣJ est 3025 fois $J\Theta$, et que $\Gamma\Sigma$ est 725 fois celui-ci, et que le rapport de NM à MJ est égal au rupport de $\Gamma\Sigma$ à ΣJ , on a NM 725 parties, suivant la quantité qui rend MJ egal à 3025. Mais < MJ> est le double de FB; on a alors NM égal à 1450, suivant la quantité qui rend FB égal à 3025.

Mais on a indiqué que JF est une fois plus trois quarts BF, l'unité. Donc la surface JN par JL est la surface de MJ qui est deux plus MN qui est mille quatre cent cinquante trois mille vingt cinquièmes d'unité, par JL qui est un plus trois-quarts; sa mesure est donc 4 plus mille vingt-cinq trois mille vingt cinquièmes d'unité, qui est la mesure du carré de KJ, car le produit de NJ par JL est égal au carré de KJ. Puisque SP est le double de KJ et que UQ est la moitié de SP, on a UQ \blacksquare égale KJ, et leurs carrées sont égaux. Le carré de KJ est égal à SQ par QO; on a donc la mesure de la surface SQ par QO 4 plus mille vingt-cinq trois mille vingt cinquièmes d'unité. Puisque $Q\Xi$ est trois suivant la quantité qui rend ΞT égal à quatre, et que le rapport de SR à RQ est le même, on a donc RQ trois septièmes de QS, et RS est ses quatre septièmes. On a donc la surface OQ par RS quatre septièmes de OQ par QS, dont on a rappelé la mesure; et la surface OQ par RS est la surface OV, car QV est égal à SW et SW égale SR, donc la surface OV est deux plus mille quatre cent cinquante trois mille vingt cinquièmes, et la surface RW

¹ Littéralement 1450 de 3025 de l'unité, formulation difficilement intelligible on français. Nous avons adopté, dans ce cas comme dans les autres semblables, des traductions équivalentes à celle doonée ci-dessus, quitte à changer les chifires en mots.

Traduction

Au nom de Dieu Clément et Miséricordieux. Grâces lui soient rendues, et bénédiction à Muhammed son prophète, et à toute sa famille.

Problème posé par Shams al-Din, Prince des Princes de al-Nizāmiyya, au très illustre et unique Imām, Sharaf al-Din, gloire de l'Islam, figure de l'Histoire, Muzafar bin Muhammed al-Muzafar al-Tūsi, que Dieu perpétue sa réussite.

Dans la ville de Hamadan, l'année six cent six de l'Hégire.

Au sujet d'un carré dont chacun des côtés est connu, et qu'on veut partager en quatre surfaces. L'une, au milieu, est un rectangle, et trois trapèzes l'entourent de trois côtés, de sorte que les quatre surfaces sont les unes aux autres dans un rapport donné connu. Que le côté du carré et le rapport des surfaces soit déterminé: disons que chacun des côtés du carré soit dux; te qu'on cherche est que le rectangle qui est au milieu soit la moitié du trapèze qui est sur l'un de ses côtés, que le trapèze qui est au-dessus de lui soit son triple, et que le trapèze qui est sur l'autre côté soit son quintuple.

Exemple: le carré ABCD a des côtes égaux, et le côté AB est dix, et on veut la construction indiquée.

Prolongeons le côté AB jusqu'à un point E quelconque, et ajoutons à la droite BE neuf fois elle-même: on a douc la droite BI dix fois la droite BE Joignons ID, et menons du point E la droite EF, parallèle à ID. On marque un point Y sur la droite BE — peu importe où se trouve Y.

Posons YG 54 fois BY, et GH 45 fois BY: joignous GF. Menons du point H une droite parallèle à la droite GF, qui est la droite HJ. Menons cusuite du point J la droite JS, parallèle à AB, et prolongeons SJ jusqu'au point L, de sorte que la droite JL soit égale à BF plus ses trois-quarts.

Posons JM deux fois BF, et marquons ensuite le point Θ , posons la droite $\Theta \Sigma$ 3024 fois la droite $J\Theta$, et posons ensuite la droite $\Sigma \Gamma$ 725 fois la droite $J\Theta$.

Joignons la droite ∑M. et menons la droite ℂN parallèle à celle-ci. Traçons sur le diamètre NL un demi-cercle, et posons ensuite la droite SO cinq fois plus cinq parties de onze parties de la droite BF. Puisque le diamètre SO est plus grand que le diamètre NL, on peut donc mener du point S dans le cercle SO une corde, SP, égale au double de KJ.

Partageons l'arc SP en deux parties égales, au point U. Du point U

1. Littéralement preuve du temps.

dans ce type de problèmes de construction géométrique à la règle et au compas, mais traité par un algébriste, deux traductions successives: une traduction algébrique du problème géométrique, qui ramène à une équation algébrique; une traduction géométrique du problème algébrique, destinée à répondre au problème initial par une construction (l'intersection d'un cercle et d'une droite).

Cette notable différence entre la solution des problèmes de construction géométrique traités par les algébristes, et l'étude des mêmes problèmes par les géomètres - le célèbre problème de la trisection de l'angle, par exemple - tient à cette double traduction. Elle n'exprime pas seulement de nouveaux rapports entre algèbre et géométrie, mais encore elle infléchit le sens même du terme d'analyse dans un débat célèbre sur l'analyse et la synthèse.

Mais une telle démarche n'apparaît pas pour la première fois chez all'usi; elle est déjà survie par ses prédécesseurs, al-Khayyām par exemple, pour traiter de problèmes plus difficiles que celui d'al-Tusi, comme la division d'un quart de cercle en deux parties en un point, sous certaines conditions; ceci fers l'objet d'une prochaîne étude.

Préface à la Traduction

Le texte que nous présentons ainsi que sa traduction a été établi à partir de deux manuscrits:

- 1. Smith MS. Or. 47, Columbia University, pp. 29-35. Vraisemblablement copié au XIIIème siècle.
- Leiden Or. 14. ff. 3237 326°. Copié au XVII tema siècle à la demande de Golius. Voir le catalogue de Dosy.

Les deux textes renvoient au même archétype pour les raisons suivantes:

- (I) Sur 116 accidents, on en trouve seulement 3 dans le manuscrit de Columbia qui ne soient pas dans le manuscrit de Leiden, la réciproque n'est pas vraie: des dizaines d'accidents figurent simplement dans ce dernier.
- (2) Il manque au manuscrit de Leiden cinq mots que l'on trouve tous dans le manuscrit de Columbia; tandis qu'il manque à ce dernier un seul mot qui figure dans le premier.
- (3) Ce qu'il faut ajouter pour établir le seus du texte est nécessaire dans les deux cas.

Enfin, plusieurs accidents sont provoqués par l'usage d'une même lettre pour désigner deux points différents de la figure géométrique.

Nous avons indiqué les pages du manuscrit de Columbia par / et celles du manuscrit de Leiden par 📕 .

Mais pour achever l'analyse, il faut encore pouvoir placer la droite 3 Il est donc nécessaire de procéder à une deuxième construction pour obteuir un segment de longueur l'ielle que

$$h = \frac{525}{11^4}$$

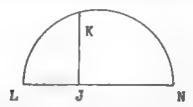
On détermine alors l comme moyenne géométrique entre les deux longueurs l_{i_1} l_{i_2} telles que:

$$l_1 \cdot l_2 = \frac{525}{115}$$
 , l_1 et l_2 rationnels.

Al-Tüsi fait pour l1 et l2 le choix suivant:

$$l_1 = JL = \frac{7}{4}$$
 $l_2 = JN = \frac{300}{121}$.

On retrace le cercle de diamètre LN et on obtient le segment JK de longueur L en utilisant la puissance du point J par rapport au cercle.



Telle est, nous semble-t-il, la voie de l'analyse qu'a suivie al-Țūsi. Elle nous permet de comprendre comment il a choisi les valeurs numériques particulières rencontrées dans la synthèse du problème, ainsi que les étapes successives de cette synthèse. On saisit en effet les raisons des différentes constructions et on comprend l'ordre de leur enchaînement.

Rien dans cette analyse ne peut surprendre: les notions et les techniques auxquelles elle fait appel sont parms les plus élémentaires rencontrées dans son Traité sur les Equations.

Ansi, après avoir tout d'abord suivi la voie d'une analyse algébrique pour étudier les inconnues x, y, z, t, il procède par une technique partout utilisée dans son Traité: les exprimer toutes au moyen des transformations affines d'une seule inconnue u. La traduction par des constructions géométriques des éléments de l'analyse algébrique donne ensuite la solution du problème géométrique posé.

Si l'hypothèse que nous venons de développer est juste, on rencontre

d'où
$$y = \frac{80}{11} - \frac{7}{2} \mu$$
.

D'autre part

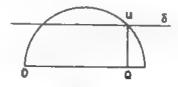
$$AX = 10 \quad y = \frac{30}{11} + \frac{7}{2} u,$$

d'où
$$AX = \frac{3}{2} BJ + \frac{7}{2} J\Delta$$
.

Il est donc clair que la solution du problème revient à le détermination de u.

S,
$$\frac{100}{11} \iff xy = \frac{100}{11} \iff (\frac{40}{11} - \frac{7}{2}u)(\frac{80}{11} - \frac{7}{2}u) = \frac{100}{11}$$
, d'où $(\frac{7}{2}u)^n - \frac{60}{11}(\frac{7}{2}u)^{-1}\frac{525}{11^2}$ 0, avec $\frac{7}{4}u < \frac{20}{11}$, d'où $\frac{7}{4}u = \frac{60 - \sqrt{375}}{11}$.

On a done retrouvé par l'analyse précédente la plupart des valeurs numériques d'al-Tūsī. Mais la résolution algébrique de l'équation du second degré obtenue conduit à un nombre irrationnel, et ne pouvait par couséquent constituer une réponse au problème de construction posé. L'analyse exige done que l'on détermine les deux racines de l'équation par des moyens pour ainsi dire constructifs: l'intersection d'un demi-cercle et d'une droite. Le cercle a nécessairement pour diamètre un segment SO de longueur $\frac{60}{11}$ (somme des tacines) et la droite δ doit être telle que sa distance à la droite SO ait pour carré $\frac{525}{112}$ (produit des racines).



Mais si l'on tient compte de la condition $\frac{7}{4}u < \frac{20}{11}$, on constate que seule la racine QS convient pour le problème.

Seul, il est vrai, l'examen de la voie de l'analyse suivie par al-Tusi peut éclairer les raisons de ce choix et de cet enchaînement. Et de fait la lecture de la conclusion de sa réponse est convameante: le mathématicien y reconnaît l'importance de l'analyse, particulièrement dans ce type de problèmes arithmético-géométriques; il y justifie son silence par des raisons de circonstances, à savoir la recherche délibérée de la brièveté dans sa correspondance.

Al-Tüsī considère en effet que l'analyse est nécessaire pour parvenir au résultat cherché et. plus généralement, qu'elle seule produit "les plus grands enseignements dans les sciences mathématiques". Aussi déclare-t-il à son correspondant que, bien qu'il passe outre et n'expose pas cette analyse. Il se tient à sa disposition pour la lui communiquer, s'il en exprime le désir.

Pour nous, cependant, le résultat est le même : le texte ne nous offre aucune information sur l'analyse suivie par le mathématicien. Il ne nous reste qu'à tenter de reconstituer cette analyse à l'aide des seules notions en possession du mathématicien. Reprenons donc le problème d'al-Tūsī et posons:

$$\begin{array}{lll} S_1 = \text{le rectangle} & Z\Omega \triangle \Pi \\ S_2 = \text{le trapèse} & AB\triangle Z \\ S_3 = \text{le trapèse} & CD\Pi\Omega \\ S_4 = \text{le trapèze} & AZ\Omega C \end{array}$$

tels que Posons

$$\begin{split} S_2 &= 2 \; S_1 \quad , \quad S_4 = 5 \; S_1 \quad , \quad S_4 = 3 \; S_1 \; , \\ \Delta \Pi &= x \quad , \quad \Delta Z = y \; , \qquad \Pi \; D = z \quad , \quad \triangle B = t \end{split}$$

On a immédiatement:

$$S_{z} = \frac{1}{11}(A, B, C, D) = \frac{100}{11}$$

$$S_{z} = \frac{2}{11}(A, B, C, D) \iff S_{z} = (B, J, S, A)$$

$$BJ = \frac{2}{11} \quad , \quad BD = \frac{20}{11} \quad ,$$

$$S_{z} = \frac{5}{2}S_{z} \iff D\Pi = \frac{5}{2}B\Delta.$$

avec

Soit $J\Delta = u$, une incopnue auxiliaire, on a

$$t = \frac{20}{11} + u \qquad z = \frac{50}{11} + \frac{5}{2} u$$

$$x = 10 - t - z = \frac{40}{11} - \frac{7}{2} u$$

$$S_4 = 3 S_1 \iff \frac{(10 - v)(10 + x)}{2} = 3 v y$$

On a done
$$(W,J) = \frac{1}{2} (W,X) = (A, W, Z)$$
.

Mais $(W,B) = (W,J) = (B,S)$
et $(W,B) = (A,W,Z) = (B,\Delta,Z,A)$

Mais $(B,S) = \frac{2}{11} (A,B,C,D)$,

d'où $(B, \Delta, Z, A) = \frac{2}{11} (A, B, C, D)$.

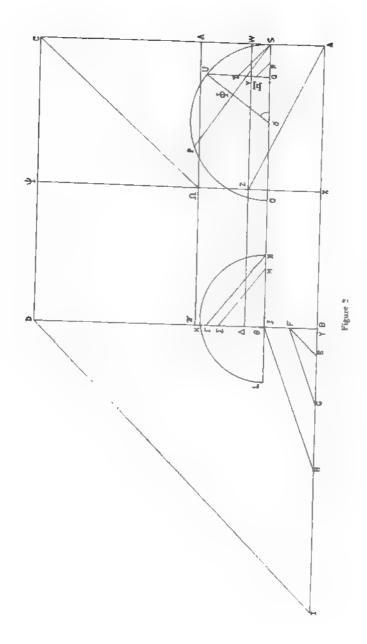
D'autre part les trapèzes (B, \triangle, Z, A) et (D, C, Ω, Π) ont des bases égales et leurs hauteurs $B\Delta$ et $D\Pi$ sont dans le rapport $\frac{2}{5}$.

Done
$$(D, C, \Omega, \Pi) = \frac{5}{11} (A, B, C, D)$$
.
On a $(A, Z, \Omega, C) = (A, \Psi) - [(A, X, Z) + (C, \Omega, \Psi)]$
Mais $\{C, \Omega, \Psi\} = \frac{5}{2} (A, X, Z)$,
d'où $(A, Z, \Omega, C) = (A, \Psi) - \frac{7}{2} (W, J)$
 $= ACAX - \frac{7}{2} ACWS$
 $= AC (\frac{3}{2} AS + \frac{7}{2} WS - \frac{7}{2} WS) = \frac{3}{2} ACAS$
 $= \frac{3}{2} (B, S) = \frac{3}{11} (A, B, C, D)$.

Finalement, si un retranche du carré (A, B, C, D) les trois trapèzes, il reste le rectangle (Ω, Π, Δ, Z) qui est donc $\frac{1}{11}$ de (A, B, C, D).

L'exposé d'al-Tūsi, aiusi que le montre le précédent résumé, est strictement synthétique. A aucun moment, ou presque,¹ le mathématicien ne dévoile les raisons pour lesquelles il a choisi les valeurs numériques particulières des différentes constructions. Il n'explique pas davantage l'ordre d'enchaînement de ces constructions.

1 On a $S_1 = \frac{1}{11}(A, B, C, D)$. On a également dès le départ le pourt J défins par $BJ = \frac{2}{11}BD$, et tel que le rectaugle $\{A,J\}$ soit les $\frac{2}{11}$ du carré; douc $\{A,J\}$ est égal au trupèze S_2 cherché.



$$JN \Rightarrow JM + MN = \frac{300}{121}BF$$

Mais $JN \cdot JL = JK^3$, puissance de J par rapport au cercle de diamètre NL.

On a
$$J\bar{K}^{1} = \frac{300}{121} \times \frac{7}{4} \bar{B}\bar{F}^{2} - \frac{525}{11^{2}} \bar{B}\bar{F}^{3}$$
.

Mais comme SP=2KJ, U est le milieu de \widehat{SP} . UQ , SO, l'égalité des triangles rectangles $Sa\Phi$ et UaQ donne $UQ=S\Phi=\frac{1}{2}SP$ d'où UQ=KJ

On a SQ-QO UQ^3 puissance de Q par rapport au cercle de diamètre SO,

d'où

$$SQ \cdot QO = \frac{525}{11^4} \bar{B} \bar{F}^a$$

D'après la construction de R, on a

$$RQ = \frac{3}{7} QS$$
 et $RS = \frac{4}{7} QS$.

d'où

$$OQ \cdot RS = \frac{4}{7} \cdot \frac{525}{11^3} \, \overline{BF}^{\,2} \,.$$

Mais

On

$$OQ \cdot RS = OQ \cdot QV = (O, V)$$

car

$$QV = SW = SR$$

d'ob

$$(0,V) = \frac{4}{7} \cdot \frac{525}{11^6} \ \overline{BF}^{\epsilon} \ .$$

et

$$(W,J) = (W,R) + (R,V) + (V,0) + (O,\Delta)$$

 $(O,\Delta) = OJ \cdot J\Delta = OJ \cdot RS \text{ avec } OJ = \frac{50}{11}BF$,

d'où

$$(W,J) = R\bar{S}^{1} + \frac{3}{4}R\bar{S}^{2} + \frac{4}{7}\cdot\frac{525}{11^{2}}B\bar{F}^{1} + \frac{50}{11}BF.RS$$

$$\frac{7}{R\bar{S}^{2}} + \frac{300}{2}R\bar{E}^{2} + \frac{50}{2}RERS$$

 $= \frac{7}{4} R \bar{S}^{1} + \frac{300}{11^{11}} \bar{B} \bar{F}^{1} + \frac{50}{11} BF RS.$

D'autre part on a

$$(W,X) = AX \cdot AW \quad \left(\frac{3}{2} AS + \frac{7}{2} WS\right) (AS + WS)$$

$$= \frac{3}{2} \overrightarrow{AS^2} + 5 AS \cdot WS + \frac{7}{2} \overline{WS^2}$$

$$= \frac{3}{2} \left(\frac{20}{11} BF\right)^0 + 5 \frac{20}{11} BF \cdot RS + \frac{7}{2} \overline{RS^2}$$

$$= \frac{600}{11^2} \overline{BF^2} + \frac{100}{11} BF \cdot RS + \frac{7}{2} \overline{RS^2} = 2 (W,J)$$

Traçons ΣM et ΓN // ΣM , N sur JS.

Posons
$$SO = 5 BF + \frac{5}{11} BF = \frac{60}{11} BF$$
.

Traçons le demi-cercle de diamètre SO et menons de S dans ce demicercle une corde SP égale à 2 JK, ce qui est possible car SO > LN.

Soit U le milieu de SP , UQ _ SO.

Soit E arbitraire sur UQ et T tels que

$$\Xi T = \left(1 + \frac{1}{3}\right) Q \Xi$$
 avec Ξ ct T sur QU .

Traçons TS et $\Xi R//TS$, R sur SO. Plaçons W sur AC tel que SW = SR. De W menons $W\Delta //AB$, Δ sur BD.

Soit Π sur BD tel que: $D\Pi = \begin{pmatrix} 2 + \frac{1}{2} \end{pmatrix} B\Delta$. Par Π on mêne $\Pi \wedge I/AB$, A sur AC.

Soit X sur AB tel que:

$$AX = \frac{3}{2}BJ + \left(3 + \frac{1}{2}\right)J\Delta$$

et

Soit Z l'intersection de ΔW et $X\Psi$ et Ω l'intersection de $X\Psi$ et $\Lambda\Pi$, on a

le rectangle $Z\Omega \Delta \Pi$

le trapèze $ABZ\Delta$ tel que (A,B,Z,Δ) $2(Z,\Omega,\Delta,\Pi)$ le trapèze $AZ\Omega C$ tel que (A,Z,Ω,C) = $5(Z,\Omega,\Delta,\Pi)$ le trapèze $CD\Pi\Omega$ tel que (C,D,Π,Ω) = $3(Z,\Omega,\Delta,\Pi)$

Démonstration :

BF est l'unité.

La construction de J donne $\frac{BF}{FJ} = \frac{11}{9}$.

$$d'_0 h = \frac{9}{11} BF + BJ - \frac{20}{11} BF$$
.

La construction de N donne MN $\frac{725}{3025}$ $MJ = \frac{1450}{3025}$ BF,

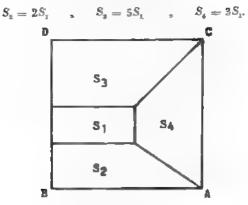


Figure 1

Il s'agit donc d'un problème de construction géométrique à l'aide de la règle et du compas. On peut penser, au premier abord, que ce problème de construction est totalement indépendant des réalisations algébriques d'al-Tūsī, telles qu'il les expose dans son Traité sur les Equations, et cette impression peut se trouver corroborée par l'exposé purement synthétique du mathématicien.

Toute la question est de savoir dans quelle mesure et en quel sens les notions et les instruments d'al-Tūsi algébriste ont pu trouver leur rôle dans l'étude d'un problème somme toute traditionnel, et, qui plus est, de circonstance. Seule une réponse à cette question permettra à l'historien qui ne se contente pas d'une simple description de classer ce mémoire dans l'oeuvre d'ul-Tūsi. Mais avant d'esquisser cette réponse, résumons d'abord la solution d'al-Tūsi, en évitant, autant que possible, de nous écarter de son texte et de son style.

Soit ABCD un carré tel que $AB=10,\,E$ un point arbitraire sur AB [voir figure 2].

On construit I tel que: BI=10 BE. Jougnons ID et de E menons EF // ID. F sur BD. On a $BF=\frac{1}{10}$ AB, d'où BF=1.

Soit Y un point arbitraire sur BE, G et H tels que YG 54 BY, GH = 45 BY. Joignons GF et menons HJ//GF. On a $BJ = \frac{20}{11}$ BF ou $BJ = \frac{2}{11}$ BD. Soit Θ arbitraire sur BD, Σ et Γ tels que: $\Theta\Sigma = 3024$ $J\Theta$ et $\Gamma\Sigma = 725$ $J\Theta$.

'Un problème arithmético-géométrique de 'Sharaf al-Din al-Tusi

ROSHDI RASHED*

L'œuvre strictement mathématique qui nous est parvenue de Sharaf al-Dîn al-Ṭūsī¹ se compose d'un *Traité sur les Equations* et de deux mémoires. Le *Traité*, nous l'avons montré ailleurs, le et l'un des ouvrages les plus importants dans l'histoire de l'algèbre classique: on pense y reconnaître les débuts de la géométrie algébrique.

Des deux mémoires, le premier, consacré à l'étude de l'asymptote à une branche d'une hyperbole équilatère, se révèle être une proposition de son précédent Traité. Nous considérons ailleurs sa situation dans un classement de l'œuvre du mathématicien.

Dans le deuxième mémoire, que nous présentons ici, al-Ţūsī étudie un problème arithmético-géométrique. Oeuvre de circonstance – il s'agit d'unc réponse à une question posée par le Directeur de la célèbre école de Bagdad: al-Niẓāmiyya –, c'est là le dernier écrit mathématique d'al-Ţūsī. D'Hamadān – l'ancienne Ecbatane – al-Ţūsī expédiait à son correspondant la réponse à la question que voici:

Soit ABCD un carré tel que AB = 10. On veut décomposer ce carré en quatre surfaces S_1 , S_2 , S_3 , S_4 , telles que:

S, soit un rectangle dont un côté est porté par BD.

 $S_{\rm e},~S_{\rm a},~S_{\rm a}$ soient des trapèzes obtenus en joignant les deux autres sommets du rectangle aux points A et C.

Soient S_a le trapèze de base AB, S_a le trapèze de base BC et S_a le trapèze de base AC. On veut aussi:

" C. N. R. S., Paris.

1. Sur l'ocuvre de Sharaf al-Din al-Tuei, voir que études:

"Résolution des Equations numériques et Algèbre, Sharaf al-Din al-Tusi. Viète". Archive for History of Exact Sciences, 13 (1974), 244-290.

"Recommencements de l'Algèbre aux XIème et XIIème Siècles" dans J. E. Murdoch and E. D. Sylla, The Cultural Context of Medieval Learning (Dordrecht, Reidel, 1975), pp. 33-50,

"L'Extraction de la Racine nieme et l'Invention des Fractions Décimales (XIème - XIIème Siècles)". Archine for History of Exact Sciences, 18 (1978), 191-243, et particulièrement les pages 208-213. Voir également l'article "Tusi. Sharaf al-Din", par A. Anbouba, in Dictionary of Scientific Biography (New York, Scribner's, 1970-1976).

2. Voir notre édition critique de ce Truité et sa traduction française, à paraître.

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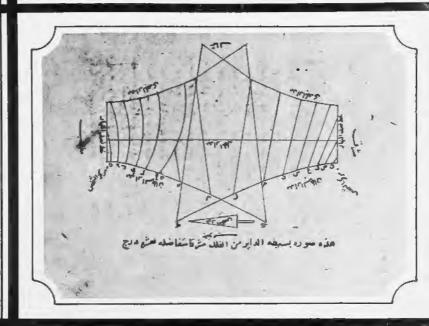
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